



SUPPLEMENT
TO THE
SEVENTY-FIFTH ANNUAL REPORT
OF THE
REGISTRAR-GENERAL
OF
BIRTHS, DEATHS AND MARRIAGES
IN ENGLAND AND WALES.

PART I.—LIFE TABLES.

Presented to both Houses of Parliament by Command of His Majesty.



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REPORT TO THE RIGHT HONOURABLE HERBERT L. SAMUEL, M.P.,
PRESIDENT OF THE LOCAL GOVERNMENT BOARD, &c., &c.

SIR,

I HAVE the honour to submit to you the following Report which forms Part I. of the "Supplement to the Seventy-Fifth Annual Report of the Registrar-General." The present volume is the sixth of a series, the first number of which dealt with the mortality in the ten years 1851-60, and was presented to Parliament in 1864. This volume relates entirely to Life Tables, Tables I. and II., for males and for females, respectively, being based upon the mortality experienced in England and Wales as a whole during the ten years 1901-10, and Tables III. and IV. upon the mortality in the same area during the years 1910-12. The presentation of the latter tables, relating to a period of only three years, is a departure from the usual practice of this Department, which has been, for the past thirty years or so, to present tables based upon the mortality experience of an entire decennium. There are two reasons for this innovation: (1) that, given a sufficiently wide basis, a more definite measure of mortality is obtained by dealing with the data for a short period of time than with the data for a long period—a consideration perhaps of special significance when the progressive decline of the death-rate in recent years is borne in mind, and (2) that the enumeration of the population in 1911 and of the deaths in 1910-1912 by single years of age instead of by quinquennial or decennial age-periods as formerly has furnished material of far more value than was previously available for the purpose of Life Table construction.

During 1910-12 also, marital condition has for the first time been distinguished in tabulating the deaths of females, and it has, therefore, been possible to prepare Life Tables for the three sections of the female population of England and Wales, single, married, and widowed. The results are given in Tables V., VI., and VII. Unfortunately, the death registers do not contain information as to the marital condition of males, and a similar investigation in the case of that sex is, therefore, impracticable.

For the decennia 1881-90, and 1891-1900, Life Tables were constructed relating to "Selected Healthy Districts," the criterion of healthiness being a death-rate not exceeding a certain limit. At that time, however, deaths were tabulated only by registration areas, and were not corrected by the distribution of the deaths of persons occurring away from their homes. Owing to this lack of correction for transferable deaths a district whose true death-rate would fall within the limit of healthiness

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might be excluded owing to the inclusion within it of a large institution receiving patients from without; while, on the other hand, other districts might have fictitiously low death-rates owing to the non-inclusion of the deaths of residents occurring elsewhere, and would thus be included among the selected healthy districts. Such tables were doubtless of interest as furnishing a contrast between the mortality conditions of the country as a whole and those of the healthiest parts of it, but suffered from the defect, in addition to that already noted, that the healthy districts even where successfully selected represented no defined class of area. It is, in fact, obvious that life must be more prolonged in those districts where deaths are comparatively few, and it has not been deemed worth while again to prepare tables for the purpose of presenting this superiority in life table form.

Under the system of tabulation adopted since 1911 we are able to obtain a knowledge of the numbers of deaths grouped by ages in the sanitary areas (county boroughs, urban districts, and rural districts), these numbers being corrected by the transference of the deaths of persons occurring away from their homes. I have accordingly thought it advisable to discontinue the arbitrary selection of "Healthy Districts," and to prepare instead a set of Life Tables based upon the mortality in the years 1911-12 in London, in the aggregate of County Boroughs, in the aggregate of Urban districts, and in the aggregate of Rural Districts, groups of districts which represent approximately varying degrees of urbanization. The results are given in Tables VIII.-XV.

In the past the Life Tables published from this Office have been prepared by members of my staff. The construction of Life Tables, however, involves work of a highly technical nature for which it appeared desirable to obtain the advice of an expert skilled in such work. I determined, therefore, to have recourse to the services of an Actuary, and I was so fortunate as to secure those of Mr. George King, F.I.A., F.F.A., who has been Vice-President of the Institute of Actuaries, and is the author of the Institute of Actuaries Text Book (Part II.), and of many papers bearing on actuarial matters. The Report which follows, together with the Appendices and the Life Tables themselves herewith submitted for your consideration, are the work of Mr. King. Special reference may be made to Part IV. of the Report (p. 26), which contains a short method of constructing abridged Life Tables—a method which should, I think, prove of great service from the public health point of view.

This is not the first occasion on which I have been indebted to Mr. George King for expert assistance in the business of my Department. His work in connexion with the Report on Ages and Conditions, Vol. VII., of the Census of 1911, was of high merit, and I feel sure that the value of these Life Tables, the construction of which has involved a great amount of labour, will be generally recognised.

I may add that the original intention was to include the result of other investigations in Life Table Construction, which have already been commenced, in this volume. Owing, however, to the many extra duties thrown upon the Department by the outbreak of war and the consequent necessity of postponing work which is not of a pressing character, it has been decided to suspend these investigations for the present, and to publish the contents of the present volume, which were ready for press by themselves.

I am,
Sir,

Your obedient Servant,

BERNARD MALLET,

Registrar-General.

REPORT ON LIFE TABLES

BY

MR. GEORGE KING, F.I.A., F.F.A.

15, Wallbrook, London, E.C.,

31 August, 1914.

To BERNARD MALLET, Esq., C.B.,

Registrar-General,

Somerset House, W.C.

SIR,

1. Following on the invitation which you gave me to examine certain of the returns of the Census of 2nd April, 1911, and to prepare graduated tables therefrom, and on my consequent report of 25th April, 1913, which appeared in the volume "Census of England and Wales, 1911, Vol. VII., Ages and Conditions as to Marriage, &c.," you were good enough to ask me to prepare the decennial life tables to be published in accordance with the custom which has prevailed for many years past after each census, and I have now the honour to submit my report.

PART I. INTRODUCTORY.

The report is in four parts, namely:—

- I. Introductory.
 - II. Construction of the Life Tables.
 - III. Some of the more important deductions derivable from the annexed Life Tables, and
 - IV. A short method of constructing abridged Life Tables.
2. On the present occasion a set more extended than usual was decided on, and your instructions were to prepare life tables as follows:—
- (1) Life tables for England and Wales, for males and females, respectively, based upon the two Censuses of 1901 and 1911, and on the deaths of the ten years 1901 to 1910.
 - (2) Life tables for England and Wales, for males and females, respectively, based upon the Census of 1911 alone, and on the deaths of the three years 1910 to 1912.
 - (3) Life tables for England and Wales, for females only, according to marital condition, single, married, or widowed, based upon the Census of 1911, and on the deaths of the three years 1910 to 1912.
 - (4) Sectional life tables, for males and females, respectively, for:—
 - (a) The Administrative County of London,
 - (b) The aggregate of County Boroughs,
 - (c) The aggregate of Urban Districts,
 - (d) The aggregate of Rural Districts,these sectional tables to be based upon the population (as estimated by your Department) in the middle of each of the years 1911 and 1912, and on the deaths in each of these two years.
3. There were, therefore, fifteen life tables in all to be prepared.

4. In constructing the tables it was desirable that a method should be employed, simple in theory, easy in application, and which would produce curves of smooth graduation, and curves which would adhere closely to the original data; and I had several conferences with yourself, Sir, and with Dr. Stevenson, the Superintendent of Statistics, and the method finally adopted is fully set forth later on in this report. Moreover, in accordance with your wish, all the statistics made use of in the preparation of the tables are given in Appendix I hereto, and all the mathematical formulas employed are demonstrated in Appendix II. It will, therefore, be possible for anyone who so desires to check every figure in the various columns of the life tables and to apply the principles and methods in investigations of a similar kind.

5. The most important of the four desiderata above mentioned is, that the mortality curves should adhere closely to the original data. It is admitted that the earlier national life tables prepared by the late Dr. Farr, while much in advance of anything that had been produced previously, yet involved certain theoretical errors which, at the older ages especially, gave an under-estimate of the rate of mortality. From English Life Tables 5 and 6, which were prepared respectively by the late Mr. A. C. Waters and by Mr. F. Finch, both of your Department, these theoretical errors were eliminated, with the result that their tables were much more trustworthy, although still showing mortality too low at the advanced ages. There remained room for improvement, and it is not derogatory to these pioneers to say that tables can now be produced more accurate than theirs. This is partly due to the fuller statistics now available, but also it is partly due to the greater knowledge to which we have attained and to the improved processes which in consequence can be applied.

6. It cannot be denied that even now the national statistics are defective. The public has not yet been sufficiently educated to lead to exact ages being always given at the census enumerations and in the records of deaths; and, especially at the older ages, say, from 80 onwards, there appears to be a tendency to make exaggerated statements of age. It is quite likely that, as a result, even the most recent tables may show an unduly light mortality at the advanced ages, but to what extent this is the case we cannot say. Although the same misstatements may occur, and in the same proportions, in the ages given at the census enumerations and in registering the deaths, yet, if on both occasions the ages are equally exaggerated, the result is to understate the rate of mortality. For instance, if after age 80 a considerable number of persons return their ages as five years greater than they really are, and if in registering the deaths the same misstatements occur, the life table shows an unduly favourable mortality, because the rate of mortality increases with the age, and therefore, if, when persons are really aged 80, say, they give their age as 85, we get the lower rate of mortality at age 80 recorded against the age 85. I cannot help thinking that this is the case to a certain extent, but to what extent we have at present no means of judging. Therefore, in constructing the present life tables, no correction has been attempted to counteract the possible misstatements of age. An unbiassed position has been assumed, and the effort has been to construct the tables absolutely in accordance with the facts as recorded, and to allow those who are interested in the subject to pursue further investigations and to make such corrections as, in their opinion, may be thought necessary. In saying this, it is not intended to cast doubt upon the accuracy of the tables as now presented. In my own mind I feel sure that up to, say, age 85 or 90, they do really represent the mortality prevailing, while above these rather advanced ages they may be accepted without much hesitation. For practical purposes any errors which exist are of trivial importance, and we may rest assured that the present tables are safely to be trusted.

7. With these preliminary observations, I now proceed to explain in sufficient detail the method of construction of the various life tables presented.

PART II. CONSTRUCTION OF THE LIFE TABLES.

(1) Life tables for England and Wales based upon the censuses of 31st March, 1901, and 2nd April, 1911, and the deaths of the ten years 1901 to 1910. English Life Tables No. 7.

8. The last preceding National Life Tables are known amongst actuaries by the name of English Life Tables No. 6, and were based upon the Censuses of 1891

and 1901 and the deaths of the ten years 1891 to 1900, and it was your wish to construct a set of new tables on as nearly as possible the same plan from the records of ten years later date. The new tables may therefore be called, not inappropriately, English Life Tables No. 7.

9. The new tables, for males and females, respectively, were prepared on identical lines, and are based on the population in 1901 as given in the volume "Census of England and Wales 1901 Summary Tables," and on the population at the Census of 1911 given in the Volume VII. already mentioned relating to that Census, and on the deaths of the ten years 1901 to 1910. The population figures for 1901 are reproduced in Table 1 of Appendix I., and those for 1911 in Table 2, and the deaths of males are given in Table 3, and of females in Table 4.

10. The populations of 1901 were supplied for each year of age for each of the first five years of life, and thereafter for the quinquennial age intervals 5 to 9 last birthday, 10 to 14, &c., up to 95 to 99, and, lastly, one group for age 100 and over.

11. The populations of 1911 were supplied for each year of age throughout life, and to bring them into harmony with the population of 1901 they were grouped into quinquennial age periods 5 to 9 last birthday, 10 to 14, &c., up to 95 to 99, and, lastly, the one group for 100 and over.

12. To obtain the mean population from the two censuses, the method of the late Mr. A. C. Waters was applied, and thus was found the mean population for each of the first five years of life, and then for quinquennial age periods, and, lastly, for the period age 100 and over; and this last group was divided into 100 to 104, and 105 and over, in the same proportions as existed among centenarians enumerated at the Census of 1911. The method of Mr. Waters for obtaining the mean population is demonstrated in Appendix II., Section 1. In applying this method it was assumed that at each of the censuses the enumerations were made one-fourth of a year after January 1st. The following tables give the mean populations, for males and females, respectively, derived as above:—

Males.

Ages last birthday.	Populations.		
	31 March, 1901.	2 April, 1911.	Mean.
0 ...	399,875	395,110	398,048
1 ...	363,424	374,109	368,644
2 ...	366,824	395,919	380,483
3 ...	363,161	388,669	375,174
4 ...	362,077	382,306	371,670
0 to 4 ...	1,855,361	1,936,113	1,894,019
5 .. 9 ...	1,738,993	1,847,295	1,790,172
10 .. 14 ...	1,670,970	1,747,631	1,707,589
15 .. 19 ...	1,607,522	1,654,895	1,630,664
20 .. 24 ...	1,472,644	1,502,652	1,487,708
25 .. 29 ...	1,328,288	1,455,783	1,387,895
30 .. 34 ...	1,157,666	1,375,872	1,258,688
35 .. 39 ...	1,034,459	1,261,432	1,139,388
40 .. 44 ...	897,484	1,075,076	979,663
45 .. 49 ...	759,955	926,102	836,767
50 .. 54 ...	636,254	768,231	697,298
55 .. 59 ...	497,498	608,005	548,580
60 .. 64 ...	410,447	477,151	441,379
65 .. 69 ...	282,403	365,896	320,914
70 .. 74 ...	195,465	236,868	214,612
75 .. 79 ...	113,096	127,466	119,782
80 .. 84 ...	52,137	56,403	54,138
85 .. 89 ...	14,915	18,457	16,551
90 .. 94 ...	2,687	3,739	3,171.5
95 .. 99 ...	322	505	406.14
100 .. 104	31	36.167
105 & over	5	5.833
Total.	15,728,613	17,445,608	16,529,426.640

Females.

Ages last birthday.	Populations.		
	31 March, 1901.	2 April, 1911.	Mean.
0	396,932	386,618	392,556
1	364,371	368,709	366,681
2	368,586	393,376	380,273
3	366,966	388,682	377,243
4	364,492	380,885	372,327
0 to 4	1,861,347	1,918,270	1,889,080
5 " 9	1,748,298	1,849,501	1,796,226
10 " 14	1,670,770	1,752,057	1,709,502
15 " 19	1,638,621	1,681,726	1,659,826
20 " 24	1,648,278	1,673,066	1,661,096
25 " 29	1,496,221	1,623,277	1,555,775
30 " 34	1,273,665	1,501,303	1,379,119
35 " 39	1,110,924	1,351,838	1,222,318
40 " 44	953,138	1,157,535	1,047,657
45 " 49	813,233	999,487	899,313
50 " 54	692,749	834,449	758,303
55 " 59	555,079	670,426	608,434
60 " 64	480,226	542,803	509,330
65 " 69	347,270	440,918	390,496
70 " 74	250,868	316,685	281,254
75 " 79	151,384	182,463	165,761
80 " 84	76,631	87,761	81,800
85 " 89	24,046	32,221	27,814
90 " 94	5,515	7,821	6,576.726
95 " 99	868	1,185	1,014.050
100 " 104	} 99 {	87	90.669
105 & over		5	5.211
Total	16,799,230	18,624,884	17,650,790.656

13. The deaths corresponding to the populations of the two censuses are given in Tables 3 and 4 of Appendix I., for each of the first five years of life, and then in groups, quinquennial to age 24 last birthday, and decennial 25 to 34, &c., as far as 75 to 84, and, lastly, a group for ages 85 to 99, with a further statement of the deaths of centenarians by years of age for the calendar years 1901 to 1909. For young children extended information is given in Table 7 of Appendix I., for the calendar years 1894 to 1912 inclusive. We there have the births in each calendar year, and also the deaths in each of the first five years of life.

14. To obtain in quinquennial age groups the deaths for the ten years 1901 to 1910, the groups in the decennial periods 25 to 34, &c., up to 75 to 84, and also the group 85 to 99, were sub-divided in the proportions existing among the deaths for the three years 1910 to 1912 given in Table 5 of Appendix I., and the deaths of centenarians in the year 1910 were divided into the groups 100 to 104, and 105 and over, in the proportions existing for the nine years 1901 and 1909.

15. Having thus, for the population and the deaths respectively, the quinquennial age groups 5 to 9, 10 to 14, &c., as far as 100 to 104, graduated quinquennial pivotal values were obtained of the populations and of the deaths for ages 12, 17, &c., down to age 97 inclusive by the formula demonstrated in Section 2 of Appendix II. Then, by dividing the deaths by the population we have the graduated pivotal values of the central death-rate, m_x , called sometimes the "mean annual death-rate," at quinquennial age points from 12 to 97 inclusive, and hence the rate of mortality, q_x , by the formula $q_x = \frac{2 m_x}{2 + m_x}$. See definitions in paragraphs 25 to 28.

16. The intervening values of the rate of mortality were derived by Osculatory Interpolation, the formula of interpolation being demonstrated in Section 3 of Appendix II. There are several functions, such as p_x (the probability of living a

year), $\log p_x$, q_x (the probability of dying in a year), $\log q_x$, and $\log (q_x + 1)$, any one of which might be made the subject of the interpolation without appreciably affecting the general results, and that one should be adopted which will give the smoothest curve. On the present occasion $\log (q_x + 1)$ was chosen as on the whole the best. The interpolation gives the values of $\log (q_x + 1)$, and hence of q_x , to seven places of decimals from age 17 to age 92 inclusive, and beyond these limits we have the pivotal values at ages 12 and 97.

17. It remained to complete the table at the infantile and youthful ages from 0 to 16 inclusive, and at the old ages from 92 to the extremity of life.

18. For the young ages recourse was first had to the births in the years 1896 to 1910, and to the deaths in the years of age 0 to 1, 1 to 2, &c., up to 4 to 5, in each of the calendar years 1897 to 1910 inclusive, as given in Table 7 of Appendix I. It was assumed that half of the sum of the births in the years 1896 and 1897 took place on 1st January, 1897, and, similarly, for the years 1898 to 1910. Then, for the purpose of the life table, the number aged exactly 0 is the sum of the assumed births on 1st January of the years 1901 to 1910: the number aged exactly 1 is the sum of the assumed births on 1st January of the years 1900 to 1909, less the sum of the deaths aged 0 to 1 in the years 1900 to 1909; the number aged exactly 2 is the sum of the assumed births on 1st January of the years 1899 to 1908, less the sum of the deaths aged 0 to 1 in the years 1899 to 1908, and the sum of the deaths aged 1 to 2 in the years 1900 to 1909; and so on for the numbers living aged exactly 2, 3, and 4. We have also the deaths in each year of age 0 to 1, 1 to 2, &c., up to 4 to 5, in the years 1901 to 1910, and dividing these deaths by the numbers living as found above, we obtain the rate of mortality derived from the records of births and of deaths without reference to the censuses. The following figures for males may be given as an example of this process:—

Exact Ages.	Numbers Living derived as above.	Deaths.	Rate of Mortality. q_x
0	4,743,220	664,467	.1400877
1	4,062,694	159,264	.0392016
2	3,868,334	59,879	.0154793
3	3,779,262	36,748	.0097236
4	3,711,011	26,668	.0071862
Total ...	20,164,521	947,026	

19. These figures, however, do not correspond with the enumerations at the censuses, as it is found that the living derived as above exceed the numbers enumerated. Ten years ago for English Life Table No. 6, it was assumed that the total of the numbers in the first five years of life enumerated at the censuses was correct, but that they were wrongly distributed. They were therefore redistributed, the total being left unchanged, and a similar course has now been followed for English Life Table No. 7. Continuing the illustration, for the males, the mean population for each of the first five years of life is given in the table in paragraph 12 above, and the total amounts to 1,894,019. This is the population living during each year of age, and not at each point of age. From this we must find the sum of the numbers living at exact ages 0, 1, 2, 3, and 4. In the first year of life it cannot be assumed that the deaths are uniformly distributed over the year of age, as the rate of mortality during the first few months of life is much heavier than afterwards. According to Table 8 of Appendix I. there were in the years 1910 to 1912, 164,033 deaths of male infants under 1 year of age, of whom 120,629 died aged less than six months, and 43,404 aged over six months, the ratios being, under six months .7353947, and over six months .2646053. Applying these ratios to the deaths of male infants in the years 1901 to 1910 there were 48,865 deaths per annum in the first six months of age. After the first year it may be assumed without any serious error that the deaths are equally distributed over each year of age, so that half of the deaths in each year of

age may be assumed to have taken place in the first six months of the year. From these considerations we have the following table:—

Mean male population aged 0 to 5 living in the ten years 1901 to 1910	1,894,019
Add deaths per calendar year under six months of age in the years 1901 to 1910	48,865
Add half deaths per annum aged 1 to 2	7,963
" " " 2 to 3	2,994
" " " 3 to 4	1,837
" " " 4 to 5	1,333
	1,957,011

20. This number, 1,957,011, may be assumed to be the sum of the mean numbers, based upon the enumerations at the censuses, aged exactly 0, 1, 2, 3, and 4. By the births and deaths alone the corresponding number is 2,016,452, the ratio between these two totals being .97052199. Applying this ratio to the numbers living derived from the births and deaths alone as shown in paragraph 18 above, we have the following results:—

Exact Ages.	Adjusted Numbers Living derived as above.	Deaths.	Rate of Mortality.
0	4,603,399	664,467	.1443427
1	3,942,934	159,264	.0403923
2	3,754,303	59,879	.0159494
3	3,667,857	36,748	.0100189
4	3,601,617	26,668	.0074045
Total	19,570,110	947,026	

21. To make English Life Table No. 7 comparable to No. 6, this adjustment of the rate of mortality was applied, but probably it has the effect of overstating the mortality among young children, and this point is taken up more fully later on in this report. (See paragraphs 35 to 43.)

22. Having thus the rate of mortality for each of the years of age 0 to 4, and the rates for ages 12, 17, and 18, previously calculated, it remained only, by interpolation, to find the rates for ages 5 to 11 and 13 to 16 inclusive. The given values are those of a function at unequal intervals, and Lagrange's method of interpolation enables the missing terms to be supplied. This method of interpolation is demonstrated in Section 4 of Appendix II. The values of q_x used in applying the formula were those for ages 3, 4, 12, 17, and 18.

23. To complete the table at the old ages the function $\log p_x$ was employed. The values of $\log p_x$ for ages 89, 90, 91, 92, and 97, had already been calculated, and from them a fourth difference was formed, and the table was completed by summation of differences.* It is thus provided that the actual original data were used in their integrity down to age 92, with a pivotal value beyond at age 97, and it is only after these extreme ages that an artificial method was adopted. Theoretically the table never comes to an end, but practically the probability of living a year becomes evanescent at about age 110 for males and 114 or 115 for females. With a

* These values may be written $u_0, u_1, u_2, u_3,$ and u_4 , the first four of which supply three differences. Then,

$$u_5 = u_0 + 8\delta + 28\delta^2 + 56\delta^3 + 70\delta^4,$$

$$\text{whence } \delta_4 = \frac{1}{70} \left\{ u_5 - (u_0 + 8\delta + 28\delta^2 + 56\delta^3) \right\}$$

radix of 1,000,000 at age 0, only two remain alive at age 105 in the case of males, and one at age 108 in the case of females.

24. English Life Tables No. 7 are annexed hereto in Table 1 for males and Table 2 for females. For ages 0 to 4 inclusive the adjusted census figures were adopted, as explained in paragraphs 18 to 21, but an alternative construction was also effected from the births and deaths alone. The following are the rates of mortality thus derived, and for comparison the adjusted census rates which have been adopted are placed beside them.

English Life Table No. 7.

Rates of Mortality, q_x .

Age.	Births and Deaths alone.		Adjusted Census Rates.		Age.
	Males.	Females.	Males.	Females.	
0	.1400877	.1141159	.1443427	.1174346	0
1	.0392016	.0365787	.0403923	.0376425	1
2	.0154793	.0148335	.0159494	.0152649	2
3	.0097236	.0097657	.0100189	.0100498	3
4	.0071862	.0072661	.0074045	.0074774	4
5	.0052679	.0053811	.0054248	.0055339	5
6	.0038701	.0040107	.0039788	.0041174	6
7	.0029024	.0030633	.0029745	.0031346	7
8	.0022831	.0024561	.0023280	.0025009	8
9	.0019389	.0021149	.0019645	.0021406	9
10	.0018049	.0019740	.0018175	.0019867	10
11	.0018249	.0019763	.0018293	.0019809	11
12	.0019507	.0020735	.0019507	.0020735	12
13	.0021431	.0022258	.0021413	.0022238	13
14	.0023711	.0024020	.0023690	.0023997	14
15	.0026122	.0025794	.0026107	.0025779	15
16	.0028523	.0027443	.0028517	.0027437	16
17	.0030860	.0028912	.0030860	.0028912	17

The adjusted census rates necessarily differ from the rates derived from the births and deaths alone up to age 4, and as they indicate the curve which must be joined on to the ordinary curve at age 12, therefore from 4 to 12 the two sets of rates must also differ. From ages 12 to 17 they differ to an inappreciable extent in order to complete the smooth junction of the two curves.

25. The annexed tables comprise various columns which it may be well to explain. The first function arrived at in constructing life tables from census returns and records of deaths is the "central death rate," which has also been called the "mean annual death rate," and is represented by the symbol m_x . It is the ratio of deaths to population in the year of age x to $x + 1$. That function has not been tabulated. It was obtained for quinquennial age points, and from it at these age points the values of the rate of mortality, q_x , were derived, the rate of mortality being the ratio of the number of deaths in the year of age x to $x + 1$ to the number entering on the year.* Throughout all the tables of this Report the rate of mortality, q_x , is the fundamental function. The arithmetical complement of q_x is p_x , the probability of living a year, and p_x is the ratio of the number completing the year of age x to $x + 1$ to the number entering on the year. The column l_x gives the number surviving according to the life table to exact age x . The first value in the column is called

* The term "rate of mortality" is here used as has been customary among actuaries. In the reports of the Registrar-General the terms "rate of mortality" and "death rate" have been used indifferently to denote the "central death rate" as defined above.

the radix of the table, and for English Life Tables Nos. 7 and 8 the radix is that for age 0, that is, it is the assumed number of simultaneous births. The other life tables annexed start at later ages.

26. The column d_x shows the deaths in the year of age x to $x + 1$ among the l_x persons who enter on that year of age. The column L_x , which in former publication of the General Register Office was called P_x , shows the population, or the years of life lived, in the year of age x to $x + 1$, and T_x , formerly called Q_x , shows the population, or the years of life lived, above the moment of age x . The column \hat{e}_x , formerly called E_x , gives the complete expectation of life, or the total future lifetime which on the average will be passed through by persons aged exactly x , and there is a further function, not tabulated, but used in Part IV. of this report, e_x , which is the curtate expectation of life, or the number of years which on the average will be completed by persons aged exactly x .

27. The complete expectation of life, \hat{e}_x , and the curtate expectation of life, e_x , are closely connected, the latter giving the number of years completed on the average, while the former includes the fraction of a year passed through in the year of death. It is usual to assume that that fraction is one-half of a year, so that $\hat{e}_x = \frac{1}{2} + e_x$. Throughout the greater part of life this equation is accurate to two places of decimals, but there is a theoretical error, introduced by the assumption thus made that the deaths are equally distributed over each year of age; and writing $\frac{1}{2} + e_x = \hat{e}_x$ rather overstates the complete expectation of life. This overstatement is with very close approximation equal to $\frac{d_{x-1} + d_x}{24 l_x}$. At birth, if we did not make a correction, the complete expectation of life would be overstated by about '03 of a year, and in the annexed tables the necessary correction has been made by taking the true proportion of deaths in the first six months of life. From age 2 to nearly age 80 the assumption is correct to two places of decimals that $\hat{e}_x = \frac{1}{2} + e_x$. At age 1 and at age 80 the overstatement is about '01, at age 90 about '02, and at age 95 about '03, but it has not been thought worth while to make any corrections.

28. It will be noticed above that as regards the population, L_x or P_x , as regards the total population aged x and upwards, T_x or Q_x , and as regards the complete expectation of life, \hat{e}_x or E_x , the notation has been changed from that formerly used in the Reports of the Registrar-General. The reason is that the notation which had been used in the General Register Office differed from that which had been employed by actuaries for very many years, and that the actuaries' notation has at various International Congresses of Actuaries been adopted as the universal notation to be employed throughout the civilized world. It has therefore been thought desirable on the present occasion to bring in the universal notation and abandon the old notation of the General Register Office, but with this explanation no confusion will arise.

29. For English Life Table No. 7, and also No. 8 to be discussed presently, the fundamental function q_x , the rate of mortality, and consequently the complementary function p_x , the probability of living a year, are given to seven places of decimals, and for the other life tables to five places of decimals. Theoretically these columns never come to an end at the old ages, but q_x rapidly approaches the limit unity and p_x the limit zero. They are tabulated exactly as calculated up to the point where the numbers in the column of living, l_x , cease to contain integers. The columns l_x , d_x , L_x , and T_x , are tabulated to the nearest integer only, it not having been thought necessary to introduce fractions. The complete expectation of life \hat{e}_x equals $\frac{T_x}{l_x}$, and up to age 90 this ratio gives practically exact values as explained in paragraph 27. Above age 90, however, through the omission of fractions in l_x and T_x the values of \hat{e}_x produced by division would not be exact. At these old ages, therefore, \hat{e}_x was specially calculated by carrying out l_x to four places of decimals, so that up to the oldest ages in the tables the values are correct, except that no adjustment has been made for the error involved in the assumption that $\hat{e}_x = \frac{1}{2} + e_x$. Anyone wishing to make a correction can, however, do so from the formula given above. The following is an extended statement of the values of q_x for ages above 100.

English Life Table No. 7. Extended Table of q_x .

Age.	Males.	Females.
100	·4496864	·4054393
1	·4912033	·4270731
2	·5459793	·4528570
3	·6129410	·4834460
4	·6883137	·5192339
105	·7658671	·5602347
6	·8381651	·6059796
7	·8985845	·6554565
8	·9432962	·7071198
9	·9721936	·7589957
110	·9882578	·8088858
1	·9958124	·8546504
2	·9987645	·8945169
3	·9997050	·9273439
4	·9999443	·9527690
115	·9999919	·9711948

(2) Life Tables for England and Wales, males and females, respectively, based upon the Census of 1911, and on the deaths of the three years 1910 to 1912. These tables are designated English Life Table No. 8.

30. The population enumerated at the Census on 2nd April, 1911, was available for every year of age, including the oldest centenarian. The details are given in Table 2 of Appendix I. The corresponding deaths for the years 1910 to 1912 are given in Table 5 of Appendix I. The central point of the three years 1910, 1911, and 1912 is 1st July, 1911, and it was therefore necessary to bring the corresponding population down to that date. Quinquennial groups were formed of the population enumerated for age period 0 to 4 last birthday, 5 to 9, &c., as far as 95 to 99, with a final group for age 100 and over, and each group was compared with the corresponding group of the Census of 1901, given in Table 1 of Appendix I, and the ratio of the increase or decrease in that group during the ten years was ascertained. There was an increase in all the groups except the last, fewer centenarians having been enumerated in 1911 than in 1901. The rate of increase or decrease in each group was calculated for the ninety days from 2 April to 1 July, 1911, by multiplying the logarithm of the decennial rate by $\frac{1}{10} \times \frac{90}{365}$ or '02465753. This gives the adjusting factor. The number recorded at the census at each age was then multiplied by the appropriate adjusting factor for its own quinquennial group, and the census population at each age was thus found brought down to 1st July, 1911.

31. In my report on the "Graduation of the Ages," given in Vol. VII. of the Census of 1911, it was explained that the most accurate results in graduating the numbers would be obtained by quinquennial grouping for the age periods 4 to 8, 9 to 13, &c., and in constructing English Life Table No. 8 this age grouping was adopted, and groups obtained as far as that for age 99 to 103. This differs from the grouping used in constructing English Life Table No. 7, where it was for ages 5 to 9, 10 to 14, &c., but for that Table we were restricted to that particular grouping, because none other was available for the Census of 1901.

32. The deaths in each of three years 1910 to 1912 were supplied age by age down to age 99, and then for 100 and over; but for 1912 the ages at death of centenarians were given, and the centenarian deaths of the three years were divided into the groups 100 to 103 and 104 and over, in the proportions which prevailed in 1912. The deaths were then grouped for age intervals 4 to 8, 9 to 13, &c., down to 99 to 103 to correspond with the population groups.

33. Having thus, for the population and the deaths respectively, the quinquennial age groups 4 to 8, 9 to 13, &c., as far as 99 to 103, graduated quinquennial

values of m_x were obtained for ages 11, 16, &c., to age 96 inclusive, in the way already explained in paragraph 15, and, hence, the corresponding values of the rate of mortality, q_x , were calculated, and the table was filled in from age 16 to age 91 by osculatory interpolation. At the old ages a fourth difference of $\log p_{88}$ was formed from the values of q_x at ages 88, 89, 90, 91, and 96, and the table was carried to the end by summation of differences. The following is an extended table of the values of q_x for ages above 100:—

English Life Table No. 8. Extended Table of q_x .

Age.	Males.	Females.
100	·4160478	·4188895
1	·4707252	·4503632
2	·5394855	·4863315
3	·6191855	·5268432
4	·7039925	·5715861
105	·7863101	·6198317
6	·8585865	·6704237
7	·9154100	·7218280
8	·9549468	·7722519
9	·9789754	·8198301
110	·9915490	·8628504
1	·9971266	·8999802
2	·9991892	·9304418
3	·9998139	·9540941
4	·9999660	·9713958
115	·9999952	·9832617

34. The rate of mortality for each of the first six years of life, not five as for English Life Table No. 7, was calculated from the births in the years 1904 to 1912, and from the deaths in the three years 1910 to 1912, on exactly the same principles as were used for English Life Table No. 7, and then, taking the values of q_x at ages 4, 5, 11, 16, and 17, the intervening value were supplied by Lagrange's method of interpolation.

35. For children under age 6 the rates of mortality derived from the births and deaths alone were adopted, and the adjustment to bring them into harmony with the census enumerations was not made. This course was followed because it is submitted that the births and deaths give more trustworthy results at these ages than do the censuses, and it may be well here to set out in a little detail the reasons for this opinion.

36. Dealing first with English Life Table No. 7, Males, in paragraph 18 there is a table showing the living at exact ages 0 to 4 derived from the births and deaths, and the deaths in each of these years of age, and we have to pass to the populations in years of age 0 to 1, 1 to 2, 2 to 3, 3 to 4, and 4 to 5, and to do so we must deduct from the numbers living at exact age x the deaths in the first half of the year x to $x + 1$. For ages 1 to 4 we may take, without important error, half of the deaths, but for age 0 we must allow for the much greater mortality that occurs in the first half of the year. In paragraph 19 we have the ratio ·7353947 for deaths under six months, and adopting this ratio for age 0, and half the deaths for the other ages, we have the following results, taking them for one year instead of for ten years as in paragraph 18:—

Births and Deaths alone. Males.

Age.	Living.	Deaths.	Half year's Deaths.	Population.
0	474,322·0	66,446·7	48,864·6	425,457·4
1	406,269·4	15,926·4	7,963·2	398,306·2
2	386,833·4	5,987·9	2,994·0	383,839·4
3	377,926·2	3,674·8	1,837·4	376,088·8
4	371,101·1	2,666·8	1,333·4	369,767·7

37. From the table in paragraph 20 we have the corresponding modified census figures as follows:—

Modified Census Figures. Males.

Age.	Living.	Deaths.	Half year's Deaths.	Population.
0	460,339·9	66,446·7	48,864·6	411,475·3
1	394,293·4	15,926·4	7,963·2	386,330·2
2	375,430·3	5,987·9	2,994·0	372,436·3
3	366,785·7	3,674·8	1,837·4	364,948·3
4	360,161·7	2,666·8	1,333·4	358,828·3

38. Lastly, in paragraph 12 are given the mean populations derived from the Censuses of 1901 and 1911 without modification.

39. Comparing the three estimates of population thus arrived at, we have the following figures:—

Populations. Males.

Age.	Births and Deaths alone.	Censuses alone.	Censuses Modified by Births and Deaths.
0	425,457	398,048	411,475
1	398,306	368,644	386,330
2	383,839	380,483	372,436
3	376,089	375,174	364,948
4	369,768	371,670	358,828

40. Going through the same process for the females, and noting that for the first year of life the ratio of deaths under six months is ·7129334, we have the following figures:—

Births and Deaths alone. Females.

Age.	Living.	Deaths.	Half year's Deaths.	Population.
0	457,003·9	52,151·4	37,180·5	419,823·4
1	403,838·8	14,771·9	7,386·0	396,452·8
2	386,084·8	5,727·0	2,863·5	383,221·3
3	377,830·7	3,689·8	1,844·9	375,985·3
4	371,355·6	2,698·3	1,349·2	370,006·4

Modified Census Figures. Females.

Age.	Living.	Deaths.	Half year's Deaths.	Population.
0	444,089·0	52,151·4	37,180·5	406,908·5
1	392,426·4	14,771·9	7,386·0	385,040·4
2	375,174·1	5,727·0	2,863·5	372,310·6
3	367,153·2	3,689·8	1,844·9	365,308·3
4	360,861·1	2,698·3	1,349·2	359,511·9

Populations. Females.

Age.	Births and Deaths alone.	Censuses alone.	Censuses Modified by Births and Deaths.
0	419,823	392,556	406,909
1	396,453	366,681	385,040
2	383,221	380,273	372,311
3	375,986	377,243	365,308
4	370,006	372,327	359,512

41. It will be noticed from the tables of populations above that, for ages 0 and 1, the populations given by the births and deaths alone largely exceed the mean populations derived from the two Censuses of 1901 and 1911, and consequently those for the Censuses modified; whereas for ages 2, 3, and 4, the populations derived from the births and deaths alone correspond with remarkable accuracy with the mean populations enumerated at the two Censuses. This feature is repeated when we come to deal with English Life Table No. 8 and the Census of 1911 alone. The following are the male populations derived from the births and deaths alone, and these populations compared with the census populations brought down to 1st July, 1911:—

Births and Deaths alone. Males.

Age.	Living.	Deaths.	Half year's Deaths.	Three Times Population.	Population.
0	1,361,932	164,033	120,629	1,241,303	413,768
1	1,214,346	41,577	20,788	1,193,558	397,853
2	1,190,872	15,916	7,958	1,182,914	394,305
3	1,178,218	9,639	4,820	1,173,398	391,133
4	1,155,804	6,895	3,447	1,152,357	384,119

Populations. Males.

Age.	Births and Deaths alone.	Census brought down to 1st July, 1911.
0	413,768	395,525
1	397,853	374,502
2	394,305	396,335
3	391,133	389,077
4	384,119	382,708

and, similarly, the following are the figures for the females:—

Births and Deaths alone. Females.

Age.	Living.	Deaths.	Half year's Deaths.	Three Times Population.	Population.
0	1,309,772	127,925	91,202	1,218,570	406,190
1	1,199,240	38,288	19,144	1,180,096	393,365
2	1,180,101	15,598	7,799	1,172,302	390,767
3	1,170,375	9,387	4,694	1,165,681	388,560
4	1,149,554	6,732	3,366	1,146,188	382,063

Populations. Females.

Age.	Births and Deaths alone.	Census brought down to 1st July, 1911.
0	406,190	386,905
1	393,365	368,983
2	390,767	393,668
3	388,560	388,971
4	382,063	381,168

42. If the total populations for ages 0 to 4 last birthday enumerated at the Censuses came out nearly the same as the corresponding totals calculated from the births and deaths, and if the Censuses showed a deficiency in the population of young infants and a consequent excess in the populations of children aged from 2 to 4 last birthday, then it would be reasonable to assume that, as regards total numbers, the Census enumerations were correct, but that only the ages were wrongly given, the children under two years of age being returned as over two. That is the assumption which was made formerly (although Dr. Farr in his paper in the Philosophical Transactions of 1859 does not mention the point, he having used for his table for healthy districts the births and deaths alone for young children), but when the above statements are examined it is found not to be supported by facts. In each of the two tables relating to males and females, respectively, for the two Censuses of 1901 and 1911, and in each of the two similar tables for the single Census of 1911 there is a great deficiency in the infants enumerated in each of the first two years of life, and there is no corresponding excess in the young children aged from 2 to 4 last birthday, the number of such children being in close agreement with the numbers estimated from the births and deaths. It is true that emigration disturbs a little the statistics based upon the births and deaths, and the effect of that disturbance is cumulative with increasing age. The number of infants alive under one year of age should closely agree with the calculated number derived from the births and deaths, there having been no time for emigration to tell, whereas the number of children alive in each of the succeeding four years of age should progressively be a little less—the difference being an increasing one—than the number calculated from the births and deaths. It is, however, seen that the Census returns do not comply with these conditions, and the conclusion seems to be inevitable that a large number of infants under two years of age escaped enumeration at both the Censuses of 1901 and 1911, more especially so in 1911, although why that should be it is difficult to understand. Is there any other explanation? This is a matter that is well worthy of investigation before the next census comes to be taken.

43. These considerations lead to the conclusion that greater accuracy in the rates of mortality for the first five years of life is secured by depending upon the statistics derived from births and deaths, and therefore that course has been followed in the construction of English Life Table No. 8.

44. The method of construction employed for the new tables does produce mortality curves which are of smooth graduation. This is proved if we take out the differences of successive orders of the column of q_x . Using English Life Table No. 8, Males, as an example, and retaining only five decimal places in q_x , and omitting the decimal point, the following table gives the differences of the third order.

It will be seen that for the first five years of life the differences are large, which was only to be expected, but they are regular. From age 5 onwards as far as age 75 they are very small, and, such as they are, they can be accounted for mainly by the

irregularities caused by omitting the succeeding decimal places. In fact, it would be difficult to imagine a curve of smoother graduation, unless it were a curve really of the third order with a constant third difference, which, of course, is not the case with mortality curves. From age 75 onwards the differences become larger, but still they are cyclical in character, and follow a regular law, as can be seen when we carry out the process of differencing further.

English Life Table No. 8. Males.

Age.	3rd Difference of q_x .		Age.	3rd Difference of q_x .		Age.	3rd Difference of q_x .	
	Positive.	Negative.		Positive.	Negative.		Positive.	Negative.
0		4965	40	—	—	80	12	
1		1270	1	1		1	7	
2		185	2	—		2	9	
3		97	3		1	3	12	
4	—	—	4	—	—	4	77	
5	1		45	—	—	85	7	
6	—	—	6	2		6		102
7	—	2	7	2		7		127
8	—	—	8	5		8		146
9		2	9		2	9		65
10		3	50	—	—	90	5	
1		3	1		1	1	74	
2		1	2	2		2	137	
3		6	3	1		3	202	
4		4	4		2	4	261	
15	7		55	2		95	307	
6		2	6	—	—	6	321	
7		3	7	4		7	276	
8		2	8	—	—	8	160	
9		2	9		2	9		47
20	2		60		1	100	314	
1	2		1	8		1	584	
2	4		2	5		2	758	
3	1		3	8		3	756	
4	—	—	4	2		4	542	
25		2	65		3	105	182	
6	2		6	5		6	177	
7		1	7	3		7	405	
8	2		8	4		8	447	
9		2	9	11		9	347	
30	2		70	3		110	208	
1		2	1		5	1	98	
2	—	—	2		7	2	33	
3		1	3		8			
4	—	—	4	9				
35		1	75	13				
6	2		6		9			
7	2		7		8			
8	1		8		11			
9		1	9		6			

If from age 75 onwards we obtain the fifth difference, the following are the results :—

English Life Table No. 8. Males.

Age.	5th Difference of q_x .		Age.	5th Difference of q_x .		Age.	5th Difference of q_x .	
	Positive.	Negative.		Positive.	Negative.		Positive.	Negative.
75 ...	23		90 ...		6	105 ...		131
6 ...		4	1 ...	2		6 ...		186
7 ...	8		2 ...		6	7 ...		142
8 ...	13		3 ...		13	8 ...		39
9 ...		23	4 ...		32	9 ...	29	
80 ...	7		95 ...		59	110 ...	45	
1 ...	1		6 ...		71			
2 ...	62		7 ...		91			
3 ...		135	8 ...		60			
4 ...		39	9 ...		3			
85 ...	84		100 ...	96				
6 ...	6		1 ...	176				
7 ...	100		2 ...	212				
8 ...		11	3 ...	146				
9 ...		1	4 ...		1			

These fifth differences are smaller than the third, and, from the fairly regular changes from positive to negative, and *vice versa*, it is seen that they also follow a law. From age 91 onwards the law becomes manifest, except in so far as it is disturbed by neglecting the more remote decimal places. At that part of the table $\log p_x$ has a constant fourth difference, and all the functions depending upon it must therefore follow a definite law and be of smooth graduation. Carrying on the column of q_x indefinitely and to a sufficient number of decimal places, it would be found that all the orders of differences would become infinitesimal. English Life Table, No. 8, Males, has been used as an illustration, but all the fifteen tables constructed are of a very similar character in this respect.

45. The mortality curves also adhere accurately to the original data. Hitherto it has not been possible to prove that this condition has been fulfilled in the construction of national life tables, because the data were not given in a form to render the calculations feasible. Now, for the first time, in English Life Table No. 8, we have the populations and the deaths for each year of age, and from the final mortality table we can ascertain the expected deaths, and compare them with the actual. To obtain the expected deaths, seeing that the data consist of populations and not of the numbers living at the commencement of the year of age, we must form a column of m_x , the central death rate, from the column of q_x , and then multiply three times the population at each age brought down to 1st July by the corresponding m_x , three times the population being taken because there are deaths for three years. That has been done for English Life Table No. 8 for both males and females, and the following comparison of the actual and the expected deaths in each case shows how very closely the final tables adhere to the original facts. For the first five years of life the census figures have not been adopted in calculating the expected deaths for reasons above explained, but the populations have been taken from the estimates derived from the births and deaths. There having been no graduation of these figures, the expected and the actual deaths as far as age 5 agree exactly. Also, the formula to derive m_x from q_x breaks down at the other extremity of life, and therefore for ages 104 and over the expected deaths have been taken as exactly equal to the actual, but here the deaths are very few in number.

English Life Table No. 8.
Comparison of Actual with Expected Deaths.

Ages last birthday.	Population as on on 1 July, 1911.	Actual Deaths.	Expected Deaths.	Deviation, Expected less Actual.	
				Positive.	Negative.
<i>Males.</i>					
0 to 3	1,597,058	231,165	231,165	—	—
4 " 8	1,878,823	22,345	23,441	1096	—
9 " 13	1,768,267	10,211	10,294	83	—
14 " 18	1,676,267	13,073	12,937	—	136
19 " 23	1,529,538	16,706	16,563	—	143
24 " 28	1,469,229	18,196	18,264	68	—
29 " 33	1,400,431	21,213	21,204	—	9
34 " 38	1,300,096	25,812	25,785	—	27
39 " 43	1,123,739	29,071	29,027	—	44
44 " 48	948,806	33,169	33,210	41	—
49 " 53	804,168	38,603	38,478	—	125
54 " 58	640,706	44,117	44,097	—	20
59 " 63	506,430	50,465	50,241	—	224
64 " 68	383,388	55,465	55,623	158	—
69 " 73	268,875	58,191	57,901	—	290
74 " 78	148,627	48,879	48,842	—	37
79 " 83	66,129	32,210	32,247	37	—
84 " 88	24,269	16,761	16,758	—	3
89 " 93	5,405	5,158	5,195	37	—
94 " 98	778	856	884	28	—
99 " 103	59	87	92	5	—
104 and over	6	7	7	—	—
All Ages.	17,541,094	771,760	772,255	1553	1058
				+495	
<i>Females.</i>					
0 to 3	1,578,883	191,198	191,198	—	—
4 " 8	1,877,233	22,119	23,016	897	—
9 " 13	1,771,238	10,466	10,550	84	—
14 " 18	1,695,731	13,059	12,827	—	232
19 " 23	1,667,756	15,229	15,231	2	—
24 " 28	1,652,490	17,488	17,507	19	—
29 " 33	1,528,954	19,805	19,791	—	14
34 " 38	1,395,151	23,019	23,005	—	14
39 " 43	1,207,377	25,223	25,186	—	37
44 " 48	1,025,521	27,949	27,997	48	—
49 " 53	870,115	32,017	31,938	—	79
54 " 58	704,602	36,998	36,956	—	42
59 " 63	570,080	43,080	42,817	—	263
64 " 68	460,335	51,198	51,394	196	—
69 " 73	348,248	61,489	61,220	—	269
74 " 78	210,885	57,426	57,455	29	—
79 " 83	100,824	42,473	42,410	—	63
84 " 88	41,694	24,808	24,756	—	52
89 " 93	10,862	9,023	9,052	29	—
94 " 98	1,750	1,928	1,988	60	—
99 " 103	153	235	244	9	—
104 and over	7	6	6	—	—
All Ages.	18,719,889	726,236	726,544	1373	1065
				+308	

46. Examining the above tables, it is seen that in the case of males the final life table gives 495 more expected deaths than actual out of a total number of 771,760. The deviation is, therefore, very small and of no importance, but looking at the top of the table it is seen that that excess of expected deaths arises at the ages 4 to 8, where recourse was had to Lagrange's method of interpolation.

Evidently too much weight is given to the comparatively heavy mortality at ages 4 and 5. It might be possible to devise some method of interpolation that would avoid this small error, but in practice it is of no importance. In the case of the females similar remarks apply. There the expected deaths are only 308 in excess of the actual out of a total number of 726,236 deaths. We could hardly wish for a more close agreement.

(3) Life tables for England and Wales, for females only, according to marital condition, single, married, or widowed, based upon the Census of 1911, and the deaths of the three years 1910 to 1912.

47. These tables have been prepared from the Census of 1911, and the deaths of the three years 1910, 1911, and 1912. At the Census of 1911 the enumerations showed the marital condition of females, but not so at the Census of 1901 in suitable age groups, and therefore it was not possible to bring down the figures of the Census of 1911 to 1st July for the increase of the population as was done for English Life Table No. 8. Hence there is no doubt a very slight over-statement of the rate of mortality, because the population had slightly increased between 2nd April and 1st July, and the larger population on 1st July, had it been available, should have been used as a denominator to obtain the central death rate at the pivotal quinquennial points of age. In this respect the tables for the marital condition of females differ from English Life Table No. 8, but in every other respect the construction has been identical. Age groups with central ages 11, 16, 21, &c., were used, giving the pivotal values at these ages. For single women the earliest pivotal value that could be formed was that for age 11, and that gave, by osculatory interpolation, the values of q_x for each year of age from 16 onwards. It was found that at age 16 the rate of mortality so derived was almost identical with that by English Life Table No. 8, and, therefore, for age 15 the rate of Table No. 8 was adopted, so that the table for the single women starts at age 15. For the married women and widows, the earliest pivotal point that could be obtained was that for age 26, and by osculatory interpolation we get the values of q_x from age 31 onwards. Using then these values at ages 33, 32, 31, and 26, the values for ages 27 to 30 were supplied by a third difference, and the third difference was used to continue the table to age 25. The radix of all the three tables was taken as 100,000 at age 25, the table for the single women being carried back from that radix to age 15.

48. At the very old ages anomalies presented themselves, because the numbers supplied by the data when separated into the three marital conditions were too small to give any good results. Therefore, each table was completed by its own data as far as age 96, and for age 96 onwards it was carried on by a constant fourth difference of $\log p_{95}$, the constant fourth difference selected being -00047 , that being the constant which arises from combining all the females. The fourth differences at ages 93 and 94 were arbitrarily adjusted so as to run into this constant, it being thought that thereby a smoother curve would be produced. It was, however, found that no great advantage resulted from this adjustment, and it would have done just as well to start the constant fourth difference at age 93.

(4) Sectional Life Tables, for males and females, respectively, for—

- (a) The administrative County of London;
- (b) The aggregate of County Boroughs;
- (c) The aggregate of Urban Districts;
- (d) The aggregate of Rural Districts.

49. The data for the construction of the eight sectional tables under this head are given in Tables 9 to 12 of Appendix I. The populations were estimated in your Department as in the middle of each of the years 1911 and 1912, corrections having been made for changes in boundaries, and the sum of these estimates was taken as the assumed population on 31st December, 1911. The estimates were given for quinquennial age groups 0 to 4 last birthday, 5 to 9, &c., up to 80 to 84, with a last group 85 and over, and this last group was subdivided into quinquennial groups 85 to 89, &c., up to 100 to 104, and a final group, 105 and over, in the proportions which were enumerated in each section at the Census of 1911.

50. The deaths for each section in the two years were given for each year of age throughout life, and were grouped for quinquennial age periods to correspond with the populations as above. They will be found in Tables 11 and 12 of Appendix I.

51. Starting with the age group 5 to 9, pivotal quinquennial values were formed for the populations and the deaths at ages 12, 17, &c., as far as age 97, and hence the pivotal values were derived of the central death rate m_x , and the rate of mortality q_x , and by osculatory interpolation, exactly as in the case of all the tables already discussed, the final values of q_x were formed from age 17 to 92 inclusive.

52. At the old ages the function $\log p_x$ was used, and from the values at ages 89, 90, 91, 92, and 97 a fourth difference was formed, and each of the tables was thus completed from the actual experience as far as age 97. At the still older ages anomalies were met with which were produced by the paucity of data, and all the eight tables were completed by assuming a constant fourth difference of $\log p_x$ equal to $-.00050$, that being approximately its value for the whole of England and Wales. This method is of course empirical, but at these extreme ages any little error in the assumption is of no practical importance, and in the absence of data some reasonable method must be employed to bring the tables to a convenient end.

53. Because, before 1911 the births and deaths were recorded by registration areas and not by administrative, it was not possible to obtain the births and deaths for the individual sections at the ages of early childhood, and without this information there is no method by which the tables could be carried back to age 0 with trustworthy results. It was therefore determined to start all these eight tables at age 12, and the missing values for ages 13 to 16, inclusive, were supplied by a third difference calculated from the values for ages 12, 17, 18, and 19.

54. In the statistical tables of Appendix I. it has not been thought necessary to include the populations of the several sections as enumerated in 1911, although these were used to subdivide the estimated populations above mentioned. They will be found in Volume VII. of the "Census of England and Wales," pages 5 to 14, except as regards centenarians, particulars of whom were supplied specially.

PART III.—SOME OF THE MORE IMPORTANT DEDUCTIONS DERIVABLE FROM THE ANNEXED LIFE TABLES.

55. From the fifteen life tables annexed, accompanied as they are by a large mass of statistics, many deductions may be derived, but it is not intended here to go into this matter with any elaboration. The opportunity is, however, taken to examine the progression of the national death rate by means of the new tables now presented and of tables based upon former censuses.

56. There are various methods of comparing life tables. When two tables start at the same age with the same radix, then, by looking at the numbers living from age to age, a judgment can be formed as to the comparative rates of mortality. We may see, for instance, how many reach age 50 by each of the tables, and, comparing these numbers, we shall know which of the two tables shows up to age 50 the heavier mortality. Again, we may look at the expectations of life and see which of these tables shows the heavier mortality over the whole remainder of life above a given age. Such comparisons are useful as showing the cumulative results of the action of mortality up to a given age, or for the whole of the remainder of life after a given age, but they suffer from the disadvantage of giving no indication of the ways in which these cumulative results are attained. Thus, in a particular section, one table may show a heavier mortality than the other, whereas in a succeeding section the relative positions of the tables may be reversed. It is well, therefore, to employ a method which compares the tables section by section. We may use the probability of living five years or ten years at various points of age, such as ages 10, 15, 20, &c.; or, if from the probability taken to, say, five decimal places we omit the decimal point, we have the number of a given age who complete five years or ten years out of 100,000, commencing at the given age. In this way we can judge from point to point the relative rates of mortality shown by the two tables over intervals, and we can thus see the changes in the relative rates of mortality as the age of the lives increases. If, instead of taking the numbers who complete each period we take those who die, we shall have the numbers who die within five years or ten years out of 100,000 commencing at each age, and probably this is the most effective way of comparing life tables, and it has been adopted in the present enquiry.

57. English Life Table No. 6 shows the rates of mortality which prevailed during the ten years 1891 to 1900, No. 7 during the ten years 1901 to 1910, and No. 8 during the three years 1910 to 1912. We have thus three periods in chronological order from which good comparisons may be derived. In order, however, that the best results may be obtained, all the tables compared must have been constructed on the same principles, because otherwise the results may be vitiated by the effect of the formulas used on the calculated rates of mortality from point to point, apart from any real difference in the mortality. English Life Tables No. 7 and 8 have been prepared in practically the same way, but other formulas were used for No. 6, as published in the reports of the Registrar-General. English Life Table No. 6 had been recomputed by the same methods as have now been employed for Nos. 7 and 8, the reconstructed table being given in the "Journal of the Institute of Actuaries," Vol. XLIII., page 355, and it is this reconstructed table which has been used in the following comparisons. The difference between the official table and the reconstructed table is hardly appreciable up to about age 70, but at the older ages the reconstructed table shows a rather higher rate of mortality, the methods used in constructing the official table probably overstating the vitality, as mentioned in paragraph 5 above.

58. There is also a fourth table which is available for tracing the progression of the national death rate, namely, the table prepared for the National Insurance Commissioners, and published in the "Report for 1912-13 on the Administration of the National Insurance Act," Part I., pages 578 to 581. That was based on the estimated population on 30th June, 1909, and on the deaths of the three years 1908, 1909, and 1910. The estimate of the population was, however, made eight years after the last preceding census, so that it was difficult to secure accuracy. A new estimate of the population as at the same date was supplied to me, based upon the two Censuses of 1901 and 1911, and therefore much more trustworthy than the original estimate, and were the Insurance Commissioners table to be recalculated on this new estimate, differences of some importance would result. This point is taken up lower down, and for the moment attention is confined to the three National Life Tables, Nos. 6, 7 and 8.

59. Omitting for the moment children under 5, the two following statements afford a means of tracing the changes in the national death rate. They show, for five years and for ten years respectively, the number who die out of 100,000, commencing at each age according to the different life tables.

England and Wales.

Number who die within 5 years out of 100,000 commencing at each age, according to English Life Tables Nos. 6, 7, and 8, respectively.

Age.	Males.			Females.		
	Life Table No. 6.	Life Table No. 7.	Life Table No. 8.	Life Table No. 6.	Life Table No. 7.	Life Table No. 8.
5	2,132	1,656	1,678	2,155	1,730	1,656
10	1,215	1,006	956	1,279	1,063	985
15	1,864	1,533	1,392	1,794	1,431	1,320
20	2,492	2,058	1,857	2,227	1,732	1,554
25	2,947	2,422	2,116	2,781	2,083	1,814
30	3,772	3,119	2,629	3,255	2,651	2,243
35	4,948	3,978	3,430	4,217	3,337	2,844
40	6,332	5,082	4,483	5,221	4,135	3,608
45	7,904	6,737	6,026	6,190	5,291	4,707
50	10,443	9,128	8,272	8,226	7,048	6,393
55	13,732	12,622	11,696	11,082	10,007	9,023
60	19,007	17,419	16,478	15,950	13,740	12,739
65	25,616	23,882	23,188	22,229	19,416	18,560
70	35,728	33,929	32,922	31,887	29,824	27,819
75	47,238	46,302	45,625	43,016	41,160	39,892
80	64,121	59,006	59,342	59,768	54,364	53,976
85	78,546	74,321	72,553	73,530	69,579	66,794
90	89,512	86,624	82,602	84,845	81,801	78,944

England and Wales.

Number who die within 10 years out of 100,000 commencing at each age, according to English Life Tables Nos. 6, 7, and 8, respectively.

Age.	Males.			Females.		
	Life Table No. 6.	Life Table No. 7.	Life Table No. 8.	Life Table No. 6.	Life Table No. 7.	Life Table No. 8.
5	3,321	2,647	2,618	3,406	2,775	2,624
10	3,056	2,523	2,337	3,050	2,476	2,292
15	4,309	3,559	3,226	3,980	3,139	2,853
20	5,365	4,430	3,934	4,946	3,779	3,339
25	6,608	5,466	4,687	5,945	4,681	4,016
30	8,534	6,973	5,969	7,334	5,900	5,023
35	10,967	8,858	7,760	9,218	7,334	6,350
40	13,736	11,476	10,241	11,088	9,207	8,143
45	17,522	15,250	13,799	13,907	11,966	10,799
50	22,741	20,598	18,999	18,396	16,349	14,839
55	30,129	27,843	26,247	25,264	22,372	20,611
60	39,754	37,141	35,847	34,633	30,488	28,934
65	52,192	49,708	48,476	47,028	43,449	41,216
70	66,089	64,521	63,526	61,187	58,709	56,615
75	81,070	77,987	77,892	77,074	73,148	72,336
80	92,303	89,473	88,840	89,351	86,117	84,718
85	97,750	96,565	95,224	95,989	94,464	93,008

60. It will be seen that throughout the whole of life after age 5, Life Table No. 7, based on the deaths of the years 1901 to 1910, shows lighter mortality both for males and females than does Life Table No. 6 based upon the deaths of the years 1891 to 1900. Again, Life Table No. 8, which is of the most recent date, based upon the deaths of the three years 1910, 1911, and 1912, shows a decided improvement on No. 7. In both of the tables Nos. 7 and 8 the year 1910 is included, but No. 7 may be taken to show on the average the mortality of the years 1905 and 1906, and No. 8 that of the year 1911, so that from that point of view No. 8 is of about five or six years later date than No. 7. The Insurance Commissioners' table would be between these two and show the mortality of about the year 1909.

61. The foregoing tables give the deaths that would occur out of 100,000, entering at each age, but that does not represent any actual population, and a further useful comparison may be made by taking the census enumerations of 1911, and finding by each table the number of deaths that would take place in one year in the population as recorded. The following table gives the results:—

The number of deaths that would take place in one year in a population represented by the actual census enumerations of 1911, according to the rates of mortality shown by English Life Tables Nos. 6, 7, and 8, respectively.

Ages last birthday.	Males.			Females.		
	Life Table No. 6.	Life Table No. 7.	Life Table No. 8.	Life Table No. 6.	Life Table No. 7.	Life Table No. 8.
5 to 9	8,877	6,196	6,271	8,956	6,482	6,193
10 " 14	4,301	3,532	3,357	4,528	3,738	3,469
15 " 19	6,210	5,104	4,638	6,097	4,842	4,471
20 " 24	7,578	6,243	5,631	7,537	5,852	5,240
25 " 29	8,705	7,136	6,223	9,156	6,825	5,938
30 " 34	10,544	8,690	7,307	9,907	8,041	6,785
35 " 39	12,768	10,217	8,785	11,621	9,155	7,785
40 " 44	13,974	11,131	9,787	12,360	9,723	8,453
45 " 49	15,211	12,872	11,471	12,751	10,841	9,614
50 " 54	16,805	14,570	13,134	14,223	12,101	10,934
55 " 59	17,857	16,304	15,024	15,670	14,067	12,615
60 " 64	19,885	18,055	16,972	18,662	15,892	14,638
65 " 69	21,515	19,836	19,174	22,019	18,892	17,965
70 " 74	20,582	19,255	18,549	23,980	22,066	20,321
75 " 79	15,838	15,461	15,112	19,973	18,905	18,069
80 " 84	11,138	9,747	9,850	15,478	13,379	13,268
85 " 89	5,411	4,760	4,559	8,232	7,338	6,830
Total 5 to 89	217,199	189,109	175,844	221,150	188,139	172,588

At every age, as before, the tables show a reduction in the mortality according to their chronological order. For males aged from 5 to 89 last birthday there would be 217,199 deaths annually according to Life Table No. 6, 189,109 according to Life Table No. 7, and 175,844 according to Life Table No. 8. Thus, annually, there are 41,355 male lives saved in this section of the population of England and Wales by the fall in the rate of mortality which took place between the period 1891 to 1900 and the period 1910 to 1912. Similarly, for females there are 48,562 lives saved. The improvement in the rate of mortality of males has been 19.04 per cent. in the period, and of females 21.96 per cent.

62. The table of the National Insurance Commissioners shows as far as about age 75 for both males and females a lighter mortality than Life Table No. 7, and a heavier mortality than Life Table No. 8, but above age 75 it shows a heavier mortality than Life Table No. 7. This table, therefore, does not quite fall into line with the others, and forms a break in the chronological order. That, however, is due to the difficulty of forming estimates of population eight years after a census, and when the revised population estimates are used, the Insurance Commissioners' table comes into complete harmony with the others. The following, for males and for females, are the two estimates of population, with the ratio of the original estimate to the revised.

Insurance Commissioners' Table.

Comparison of the original estimate of the Population as on 30 June, 1909, based upon the Census of 1901, and the Revised Estimate based upon the two Censuses of 1901 and 1911.

Ages last birthday.	One tenth Original Estimate.	One tenth Revised Estimate.	Ratio, Original to Revised.
<i>Males.</i>			
15 to 24	318,183	314,342	1.01223
25 " 34	278,745	276,855	1.00682
35 " 44	226,281	226,266	1.00004
45 " 54	165,154	163,991	1.00707
55 " 64	105,237	105,281	.99962
65 " 74	55,602	57,997	.95869
75 " 84	17,750	18,047	.98355
85 and over	2,022	2,187	.92456
ALL AGES	1,168,974	1,164,966	1.00343
<i>Females.</i>			
15 to 24	339,432	334,240	1.01554
25 " 34	311,813	305,983	1.01906
35 " 44	245,300	242,809	1.01024
45 " 54	178,081	177,407	1.00378
55 " 64	118,801	118,075	1.00615
65 " 74	69,619	72,849	.95566
75 " 84	25,176	26,252	.95900
85 and over	3,578	3,935	.90928
ALL AGES	1,291,800	1,281,550	1.00795

It will be seen that the two estimates of population in the aggregate agree very closely, there being a difference of only three per thousand for the males and eight per thousand for the females, but that is not so when the different age intervals are compared. Down to age 55 for males and 65 for females the original estimates are the larger, while at the older ages in each case they are the smaller. The over-estimate at the younger ages is not great, and scarcely affects the rate of mortality,

but at the older ages the under-estimate is sometimes considerable and leads to an over-statement of the rate of mortality. It has not been thought necessary to recompute the table on the new estimates, but an approximate correction has been made, and the following table gives a comparison of the revised values of q_x with those of the other life tables, and it will be seen that the four tables in chronological order show a steady fall in the rate of mortality.

The rate of mortality, q_x , by English Life Tables Nos. 6, 7, and 8, and by the Insurance Commissioners' Table.

Age.	Life Table No. 6.	Life Table No. 7.	Insee. Commrs. Table Revised.	Life Table No. 8.	Age.
<i>Males.</i>					
20	·00460	·00378	·00350	·00348	20
30	·00685	·00566	·00514	·00478	30
40	·01180	·00931	·00837	·00811	40
50	·01936	·01657	·01554	·01482	50
60	·03581	·03262	·03164	·03042	60
70	·07248	·06708	·06588	·06470	70
80	·15523	·14163	·14577	·14299	80
90	·31800	·29566	·28793	·27395	90

Females.

20	·00413	·00325	·00301	·00295	20
30	·00611	·00484	·00445	·00411	30
40	·00989	·00766	·00697	·00660	40
50	·01500	·01267	·01171	·01140	50
60	·02918	·02539	·02465	·02310	60
70	·06283	·05643	·05471	·05259	70
80	·13932	·12429	·12448	·12419	80
90	·27619	·25781	·26093	·23826	90

63. Only persons aged 5 and over have so far been considered, but when the case of children in the first five years of life is looked at, equally favourable features become apparent.

64. We have in English Life Tables Nos. 6 and 7 the mortality for the ten years 1891 to 1900 and 1901 to 1910, respectively, and both these tables, as regards the young children, have been constructed in the same way, the populations as enumerated at the censuses having been redistributed by means of the records of births and deaths. These tables, therefore, are comparable, and the following statement shows the number who die in one year in each year of age out of 100,000 entering on the year.

Modified Census Figures.

Ages last birthday.	Males.		Females.	
	Life Table No. 6.	Life Table No. 7.	Life Table No. 6.	Life Table No. 7.
0	17,186	14,434	14,066	11,743
1	5,319	4,039	4,949	3,764
2	2,083	1,595	2,014	1,526
3	1,318	1,002	1,334	1,005
4	970	740	955	748

65. In paragraph 24 above, the rates of mortality in early childhood according to English Life Table No. 7 are also given as derived from the births and deaths alone to correspond with the similar rates by English Life Table No. 8. English Life Table No. 8 relates to the mortality for the years 1910 to 1912, and similar figures have been taken out for the years 1900 to 1902, so that we have two periods, each of three years, ten years apart, with English Life Table No. 7 practically covering the intervening ten years. This affords a still better test of the improvement in the mortality of childhood. The following statement shows the number dying in each year of age out of 100,000 who enter on the year.

Births and Deaths alone.

Ages last birthday.	Males.			Females.		
	Mortality 1900/1902.	Mortality 1901/1910.	Mortality 1910/1912.	Mortality 1900/1902.	Mortality 1901/1910.	Mortality 1910/1912.
0	16,063	14,009	12,044	13,156	11,412	9,767
1	4,580	3,920	3,424	4,247	3,658	3,193
2	1,797	1,548	1,337	1,746	1,483	1,322
3	1,186	972	818	1,202	977	802
4	889	719	597	893	727	586

66. Corresponding to the table given in paragraph 61 for ages 5 and over, we have the following statement for children under 5:—

The number of deaths of children under 5 which would take place in one year in a population estimated as on 1st July, 1911, by the births and deaths alone.

Ages last birthday.	Males.			Females.		
	Mortality 1900/1902.	Mortality 1901/1910.	Mortality 1910/1912.	Mortality 1900/1902.	Mortality 1901/1910.	Mortality 1910/1912.
0	72,922	63,598	54,677	57,438	49,824	42,642
1	18,539	15,867	13,860	16,977	14,623	12,764
2	7,133	6,145	5,307	6,868	5,834	5,200
3	4,658	3,817	3,213	4,689	3,812	3,129
4	3,425	2,770	2,300	3,422	2,786	2,245
Total	106,677	92,197	79,357	89,394	76,879	65,980

67. It will be seen that according to the mortality in the years 1900 to 1902, 106,677 male children under five years of age would die in a year out of what may be taken to be the population of England and Wales in the middle of 1911, while only 79,357 would die according to the mortality of the years 1910 to 1912. Therefore the improvement in the mortality which took place during the ten years in question leads to the saving annually of the lives of 27,320 males, and, similarly there is a saving of the lives of 23,414 females. In ten years the mortality among males has improved by 25·61 per cent., and among females by 26·19 per cent.

Marital Condition of Females.

68. To compare the relative mortality amongst single, married, and widowed females, respectively, the following table has been prepared. It shows the number who die within 5 years, and also the number who die within 10 years out of 100,000 females commencing at each age in each marital condition.

England and Wales, Females.

The number who die within 5 years, and the number who die within 10 years, out of 100,000 commencing at each age in each marital condition.

Age.	Five Years.			Ten Years.		
	Single.	Married.	Widowed.	Single.	Married.	Widowed.
25	1,667	1,936	2,611	3,766	4,159	5,581
30	2,134	2,267	3,050	4,690	5,084	6,644
35	2,611	2,882	3,708	5,924	6,365	8,137
40	3,402	3,586	4,600	7,970	7,932	10,538
45	4,729	4,507	6,224	10,661	10,331	13,656
50	6,227	6,099	7,925	14,112	14,170	17,651
55	8,410	8,595	10,562	19,386	19,570	23,373
60	11,984	12,007	14,324	27,188	27,419	31,440
65	17,274	17,516	19,978	38,335	38,793	43,641
70	25,458	25,796	29,571	53,441	53,612	58,563
75	37,540	37,486	41,164	70,460	70,209	73,305
80	52,706	52,346	54,628	84,426	84,309	85,045
85	67,069	67,073	67,038	93,170	93,175	93,149
90	79,260	79,271	79,215			

In the earlier years of married life the wives suffer from a heavier mortality than do their spinster sisters, but from about age 45 to 55 the position is reversed, and still later in life there is not much difference between the two classes. Throughout life until old age, widows suffer from a heavy rate of mortality, but above about age 80 all the three classes—single, married, and widowed—are scarcely distinguishable.

Sectional Tables.

69. For the sectional tables similar calculations have been made, and are given in the following two statements. Throughout the greater part of life the County of London shows a lighter mortality than the aggregate of County Boroughs, but these two sections show heavier mortality than the aggregate of Urban Districts, while the aggregate of Rural Districts shows the lightest mortality of all.

The Number who die within 5 years, out of 100,000 commencing at each age in each Section.

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Age.	Males.				Females.			
	County of London.	County Boroughs.	Urban Districts.	Rural Districts.	County of London.	County Boroughs.	Urban Districts.	Rural Districts.
15	1,370	1,592	1,483	1,270	1,172	1,458	1,306	1,329
20	1,746	2,013	1,780	1,687	1,297	1,696	1,495	1,631
25	2,206	2,386	2,010	1,945	1,622	1,934	1,739	1,864
30	3,018	3,076	2,380	2,256	2,114	2,404	2,101	2,202
35	4,197	4,106	3,103	2,663	3,012	3,310	2,647	2,526
40	5,709	5,405	4,000	3,377	4,080	4,153	3,333	2,911
45	7,620	7,377	5,544	4,320	5,468	5,559	4,510	3,639
50	10,141	10,021	7,898	5,909	7,093	7,449	6,077	5,121
55	13,776	13,986	11,235	8,561	9,733	10,519	8,801	7,449
60	18,698	19,455	16,480	12,707	13,200	14,751	12,860	10,608
65	25,005	26,603	23,280	18,814	18,578	20,927	17,963	15,888
70	35,330	38,711	34,658	29,145	27,927	32,069	29,179	25,408
75	47,568	50,092	46,412	42,436	39,261	43,856	40,636	37,609
80	60,807	62,107	58,598	57,724	54,489	57,269	54,191	51,670
85	71,981	74,219	72,833	72,537	68,906	69,411	67,083	67,085
90	84,225	84,607	81,523	85,433	79,401	79,850	78,346	80,406

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The Number who die within 10 years, out of 100,000 commencing at each age in each Section.

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15	3,092	3,573	3,237	2,936	2,454	3,130	2,781	2,938
20	3,914	4,351	3,755	3,599	2,898	3,597	3,208	3,464
25	5,158	5,389	4,342	4,157	3,701	4,292	3,803	4,025
30	7,088	7,056	5,409	4,858	5,062	5,635	4,692	4,672
35	9,666	9,289	6,979	5,950	6,969	7,326	5,891	5,363
40	12,894	12,383	9,322	7,551	9,324	9,481	7,692	6,444
45	16,988	16,659	13,004	9,974	12,173	12,594	10,313	8,574
50	22,520	22,606	18,246	13,964	16,135	17,185	14,344	12,189
55	29,898	30,720	25,864	20,180	21,648	23,718	20,529	17,267
60	39,028	40,882	35,923	29,130	29,326	32,591	28,513	24,810
65	51,501	55,016	49,870	42,476	41,317	46,284	41,901	37,259
70	66,092	69,412	64,935	59,213	56,224	61,861	57,958	53,462
75	79,450	81,088	77,813	75,665	72,357	76,009	72,806	69,846
80	89,019	90,670	88,752	88,390	85,849	86,929	84,921	84,092
85	95,580	96,032	94,980	95,999	93,595	93,836	92,872	93,551

PART IV. A SHORT METHOD OF CONSTRUCTING ABRIDGED LIFE TABLES.

70. Medical Officers of Health and others interested in the Public Health Service of the country, frequently wish to compare the mortality of a particular district with that of other districts or of the general community, without having to go through the labour of constructing a complete mortality table. Also it may be frequently useful to make similar comparisons in the case of the mortality experience of a Life Office at the stage when only the numbers at risk and the deaths age by age are available. The following is a short and simple method of constructing an abridged mortality table for quinquennial points of age, including in the functions tabulated, in addition to p_x and q_x , the probability of living five years, ${}_5p_x$, and the expectation of life, and it will be found to serve with ample accuracy the purposes in view.

71. The short method consists in finding, first, quinquennial values of p_x , the probability of living a year, and hence of $\log p_x$; then quinquennial values of $\log {}_5p_x$, the logarithm of the probability of living five years; then quinquennial values of l_x ; and, finally, quinquennial values of e_x , the expectation of life. The quinquennial values of p_x , and hence of $\log p_x$, are derived from those of m_x , the central death rate, which are calculated by the method explained and illustrated in Appendix II, Section 2, to which reference is made.

72. It will be convenient to begin by demonstrating the mathematical formulas to be used. Their application will become apparent later.

73. Let u be a function of x , and let w be the sum of five values of the function, so that $w_x = u_x + u_{x+1} + u_{x+2} + u_{x+3} + u_{x+4}$. The problem is to find w_5 and w_6 from the four values of u at quinquennial distances, u_0, u_5, u_{10} , and u_{15} . Let the differences of these quinquennial values be represented by the symbol Δ . Then employing the usual formula of finite differences

$$u_n = u_0 + n\Delta u_0 + \frac{n(n-1)}{2}\Delta^2 u_0 + \frac{n(n-1)(n-2)}{6}\Delta^3 u_0,$$

and remembering that the differences are for quinquennial periods, and taking n successively

$$\frac{5}{5}, \frac{6}{5}, \frac{7}{5}, \frac{8}{5}, \frac{9}{5}, \text{ and } \frac{10}{5},$$

we have the following scheme—

$$\begin{aligned} u_5 &= u_0 + 1.0\Delta u_0. \\ u_6 &= u_0 + 1.2\Delta u_0 + .12\Delta^2 u_0 - .032\Delta^3 u_0. \\ u_7 &= u_0 + 1.4\Delta u_0 + .28\Delta^2 u_0 - .056\Delta^3 u_0. \\ u_8 &= u_0 + 1.6\Delta u_0 + .48\Delta^2 u_0 - .064\Delta^3 u_0. \\ u_9 &= u_0 + 1.8\Delta u_0 + .72\Delta^2 u_0 - .048\Delta^3 u_0. \\ u_{10} &= u_0 + 2.0\Delta u_0 + 1.00\Delta^2 u_0. \end{aligned}$$

74. If now we add the first five lines, we have w_5 , the sum of five values of u from u_5 to u_0 inclusive, that is, we have the sum in what may be called "initial form," and if we add the last five lines we have, similarly, w_6 , the sum of five values from u_6 to u_{10} , in what may be called "terminal form." Hence the following equations result:

$$\begin{aligned} w_5 &= 5u_0 + 7\Delta u_0 + 1.6\Delta^2 u_0 - .2\Delta^3 u_0 \quad \dots \quad (i) \\ w_6 &= 5u_0 + 8\Delta u_0 + 2.6\Delta^2 u_0 - .2\Delta^3 u_0 \quad \dots \quad (ii) \end{aligned}$$

75. These formulas are central, there being three groups of five, and the formulas giving the middle group. At the youngest age of the table, however, we cannot use the central method, but, as it happens, with very little loss of accuracy we may find the

corresponding sums for the first group of five values in the set of fifteen. In the formula of finite differences we take n successively as

$$\frac{0}{5}, \frac{1}{5}, \frac{2}{5}, \frac{3}{5}, \frac{4}{5}, \text{ and } \frac{5}{5},$$

and we have the following scheme

$$\begin{aligned} u_0 &= u_0. \\ u_1 &= u_0 + .2\Delta u_0 - .08\Delta^2 u_0 + .048\Delta^3 u_0 \\ u_2 &= u_0 + .4\Delta u_0 - .12\Delta^2 u_0 + .064\Delta^3 u_0 \\ u_3 &= u_0 + .6\Delta u_0 - .12\Delta^2 u_0 + .056\Delta^3 u_0 \\ u_4 &= u_0 + .8\Delta u_0 - .08\Delta^2 u_0 + .032\Delta^3 u_0 \\ u_5 &= u_0 + 1.0\Delta u_0 \end{aligned}$$

whence summing as before we have the initial and terminal forms

$$\begin{aligned} w_0 &= 5u_0 + 2\Delta u_0 - .4\Delta^2 u_0 + .2\Delta^3 u_0 \quad \dots \quad (iii) \\ w_1 &= 5u_0 + 3\Delta u_0 - .4\Delta^2 u_0 + .2\Delta^3 u_0 \quad \dots \quad (iv) \end{aligned}$$

76. In order to get the values of $\log l_x$, and hence of l_x at quinquennial points, we must also have at the same quinquennial points the values of $\log {}_5p_x$, the logarithm of the probability of living five years, because $\log l_{x+5} = \log l_x + \log {}_5p_x$. But $\log {}_5p_x = \log p_x + \log p_{x+1} + \dots + \log p_{x+4}$. Therefore when $\log p_x$ is the function u , $\log {}_5p_x$ is the function w . It is in initial form, and equation (i) is that to be used. The method of applying the formula is fully illustrated in the two examples given later on.

77. If a be the youngest age in the table available from the statistics, formula (i) gives the value of $\log {}_5p_{a+5}$, and in order to obtain $\log {}_5p_a$ we use formula (iii). It will be seen how short the formulas are and how simple are the coefficients.

78. Having thus the values of $\log {}_5p_x$ at quinquennial points from age a onwards, we pass to the values of $\log l_x$, and hence of l_x , by continued addition. We take for l_a a suitable radix, and add to $\log l_a$ successively the values found for $\log {}_5p_x$.

79. As examples of the method it will be convenient to adopt English Life Tables No. 7 and No. 8, Males, and to take No. 8 first. For English Life Table No. 8 the populations and the deaths were grouped in fives, the first group being that for ages 4, 5, 6, 7, and 8. Therefore the first pivotal value of p_x which can be obtained from the data is that for age 11. Also, the last value is that for age 101. Therefore the series gives three orders of difference of the column $\log p_x$ as far as age 86, from which can be obtained by formula (i) the values of $\log {}_5p_x$ as far as age 91. In Table A annexed these values are given. $\log p_x$ is essentially negative, and according to usual custom it is written with a positive mantissa and a negative characteristic. It is, however, more convenient here to use the actual negative form. In working with the pen it will be found to be a great advantage to write positive quantities in black ink and negative quantities in red ink. Thus the positive and negative signs are saved, and algebraical addition of the quantities is much facilitated. It is not easy for printers to have in one table both black and red ink. Therefore, in the illustrative table positive quantities are printed in heavy Ionic type, and negative in light Italic type. The logarithms are taken to five places of decimals, but for convenience the decimal points have been omitted.

80. As mentioned above, the last value of $\log {}_5p_x$ which can be derived from the data is that for age 91, but the table does not end there, and in order to construct the values of e_x we require the values of $\log {}_5p_x$ as far as age 101, which will enable us to obtain the value of l_x at age 106. We must therefore have three orders of differences of $\log p_x$ as far as age 96. At these old ages the statistics are very uncertain, and each case must be treated on its merits, and methods must be devised to meet its special difficulties, and in order that we may carry the table of $\log p_x$ beyond the point to which the original data take it we must arrange to have a final constant difference which is negative, and so to carry on the table by summation until it reaches a natural end.

81. In the case of English Life Table No. 8 it will be observed that the third difference of $\log p_{80}$ is negative, and at age 81 positive. Therefore we can form a negative fourth difference at age 81 which may be used with great convenience to give the required third differences as far as age 96.

82. Formula (i) is then applied to obtain $\log {}_5p_x$ from age 16 to age 101 inclusive. A complete check on this portion of the work is obtained by taking the algebraical sums of the column of $\log p_x$ and its three orders of differences from age 11 to age 96 inclusive, and by applying formula (i) to these sums. The result should be the sum of the calculated values of $\log {}_5p_x$ from age 16 to age 101 inclusive. After applying this check we insert the value of $\log {}_5p_{11}$ by means of formula (iii).

83. The example as printed was worked out on the arithmometer, and shows every figure used. Where, however, an arithmometer is not available the work with very little more trouble can be done by ordinary multiplications. A column is formed by multiplying each value of $\log p_x$ by 5. Then an adjacent column is obtained by multiplying the first differences by 7, and again another column by multiplying the second differences by 1.6, and a final column by multiplying the third differences by $-.2$. These columns are then added together algebraically sidewise to give the column of $\log {}_5p_x$. This applies to the values of $\log {}_5p_x$ from age 16 onwards, and it should be noticed that when the values of $\log p_x$ and its differences at, for instance, age 16 are dealt with the result is $\log {}_5p_x$ at age 21.

84. Having now $\log {}_5p_x$ at quinquennial intervals from age 11 onwards, we select a suitable radix at age 11, in this case the radix 100,000 having been selected, and by adding to the logarithm of that radix successively the values of $\log {}_5p_x$ we obtain the values of $\log l_x$, and hence of l_x . At age 101, l_x is equal to 22, and at age 106 it has no integers and may be treated as 0.

85. The value of the curtate expectation of life e_x (see paragraphs 26 to 28) is derived by dividing by l_x the sum of the column of l_x from age $x+1$ to the oldest age in the table, and that sum may be made in quinquennial sections. The sum of the column from age $x+1$ onwards is denoted by the symbol $N'_{x:5}$, and the sum of a quinquennial section by the symbol $N'_{x:5}$.

86. We already have l_x at quinquennial points, and these constitute the function u , and $N'_{x:5}$ constitutes the function w , which function is in the terminal form, and, therefore, to the quinquennial values of l_x and its differences formulas (ii) and (iv) must be applied, exactly as formulas (i) and (iii) were applied to the column of quinquennial values of $\log p_x$. The last value of $N'_{x:5}$ derived from the statistics is that for age 96, but we must also have it for age 101. l_x at age 101 is equal to 22, and p_x to $.52927$, whence, multiplying, we have the value of l_x at 102, equal to 12. Also the value at age 106 is 0, and by inspection we interpolate the values 6, 3, and 1, for l_{103} , l_{104} , and l_{105} , respectively, and this gives us $N'_{101:5}$ equal to 22. Thus, we have quinquennial values of $N'_{x:5}$ from age 11 onwards, and by adding successively these values from the bottom upwards we form a column of N'_x at the quinquennial points. Lastly, dividing each of the values of N'_x by the corresponding l_x we derive the curtate expectation of life, to which adding $.5$ we have the complete expectation of life at quinquennial points of age. In the example $.5$ has been added to e_x before entering the value in the column.

87. For the second example we take English Life Table No. 7, Males. The original mean numbers living, and the original deaths, were grouped for quinquennial periods, 0 to 4 last birthday, 5 to 9, &c., and the earliest pivotal value of $\log p_x$ that is obtainable is that for age 12, and the last that for age 97. The values of p_x on this basis are given in Table I annexed.

88. In the following Table B the values of $\log p_x$ and its differences are set forth, and it will be observed that the third difference of $\log p_{82}$ is positive. We, therefore, cannot follow the plan which was adopted for English Life Table No. 8, but must seek another. The third difference of $\log p_{77}$ is negative, but only 77, and that is too small to bring the table to a reasonable end. We may, however, go back to age 72 where the third difference of $\log p_x$ is 1366 and negative. We use this third difference as a constant to carry the table of $\log p_x$ down to age 107 as shown in Table C. Formulas (i) and (iii) are then applied in the first part of Table C to the values of $\log p_x$ and its differences to obtain the values of l_x from age 12 to age 102, and again, formulas (ii) and (iv) are applied in the continuation of Table C, just as in Table A for English Life Table No. 8, to obtain the expectation of life. The explanations need not be repeated. The radix in this case has been taken as the value of l_{12} by the fully extended table.

89. English Life Tables Nos. 7 and 8 were selected as examples of the abridged process, partly because they illustrated two methods of dealing with the old ages, it not having been possible to treat both these tables in precisely the same way. These tables are based on very large populations, and yet they present difficulties at the old ages where the facts become comparatively few, and where they are not very trustworthy. If only restricted districts be dealt with the difficulties are accentuated, and sometimes it may even happen that data are altogether absent above say age 80. In such cases we cannot from the data obtain the third or fourth negative difference of $\log p_x$ which is required to complete the table, but it will be quite legitimate to assume one arbitrarily so long as we do so reasonably and with judgment. At these old ages any small error in the assumption will have scarcely appreciable effect on the life table for all the principal period of life, say down to age 75 or 80.

90. The value of the expectation thus found for any particular age group is that for the central *integral age* of the group, but in the Public Health Service it is more usually required for the central *point of age* of the group, that central expectation of life being the mean expectation for the five ages included in the group. We can by second differences very easily and accurately obtain this central expectation, $e_{x+\frac{1}{2}}$. Taking three values of e , which may be written e_0 , e_5 , and e_{10} , and applying the formula of finite differences,

$$e_{\frac{1}{2}} = e_0 + \cdot 1\Delta e_0 - \cdot 045\Delta^2 e_0 \dots \dots \dots (v)$$

$$e_{\frac{5}{2}} = e_0 + 1\cdot 1\Delta e_0 + \cdot 055\Delta^2 e_0 \dots \dots \dots (vi)$$

$$e_{10\frac{1}{2}} = e_0 + 2\cdot 1\Delta e_0 + 1\cdot 155\Delta^2 e_0 \dots \dots \dots (vii)$$

Formula (v) applies to the first value of e in the table, and formula (vii) to the last; while formula (vi) applies to all the intervening values. For short distances the expectations of life do not differ much from an arithmetical progression, and the second difference employed above has very little effect. We might bring in a third difference, but that would not affect the third decimal place in the expectation. To Tables A and C have been added the expectation of life for these central points of age obtained in this way.

91. It will be seen that in Table A we have the e_x and $e_{x+\frac{1}{2}}$ for ages 11, 16, 21, 26, &c., and in Table C for ages 12, 17, 22, 27, &c. Table A relates to English Life Table No. 8, which was constructed from the age grouping 9-14, 14-19, &c., and Table C to English Life Table No. 7, which was constructed from the age grouping 10-15, 15-20, &c. In fact in every case we obtain e_x and $e_{x+\frac{1}{2}}$ centrally in respect of the particular grouping employed in constructing the table. The grouping of Table C, namely, 10-15, 15-20, &c., is that most commonly used in dealing with vital statistics, and is that with which Medical Officers of Health are more particularly familiar. That grouping will always give the mean expectations of life which they generally require. If, however, there should be such a grouping as that in Table A, the mean expectations of life for the groups 10-15, 15-20, &c., can still be obtained by a special application of the formula of finite differences. Instead of equations (v) to (vii) given in paragraph 90, the following equations could be applied to e_x at ages 11, 16, &c. as in Table A, to obtain $e_{x+\frac{1}{2}}$ at ages 12, 17, &c. as in Table C, these expectations corresponding as regards age to expectations e_{11} , e_{16} , e_{21} in Table A.

$$e_{11\frac{1}{2}} = e_0 + \cdot 3\Delta e_0 - \cdot 105\Delta^2 e_0 \dots \dots \dots (v a)$$

$$e_{16\frac{1}{2}} = e_0 + 1\cdot 3\Delta e_0 + \cdot 195\Delta^2 e_0 \dots \dots \dots (vi a)$$

$$e_{21\frac{1}{2}} = e_0 + 2\cdot 3\Delta e_0 + 1\cdot 495\Delta^2 e_0 \dots \dots \dots (vii a)$$

The expectations for the central points of age for any method of grouping the original data may be obtained from the expectations for the central ages according to any other method of grouping, by suitably modifying equations (v) to (vii).

92. The process described above supplies the expectations of life at quinquennial points of age from about 11 or 12, according to the grouping of the original data, to the end of life. If a complete table be required without the other usual columns of a life table, that can easily be constructed by means of osculatory interpolation, fully explained in Appendix II, Section 3, and probably this is a shorter way of obtaining a complete table of expectations than if the life table were constructed in full. We cannot, however, go by these processes to a younger age than 11 or 12, and for infancy and childhood the expectations must be derived in some other way. That can be done by some such means as were employed to obtain the ordinary columns given in English Life Tables Nos. 7 and 8. These are fully explained in the earlier paragraphs of this report.

93. In Table D is given a comparison of the expectations of life derived by the abridged process with those produced by the construction of the life table at full length, and it will be seen that there is scarcely any difference between them. In fact the abridged process gives the expectations almost as exactly as the full length process. It might be said that this result is due to the abridged process being applied to the data grouped in the same way as for the full length table, but the abridged process can also be used for other life tables with equally satisfactory results. An abridged table (the 0^M table) constructed from the experience of healthy male lives assured in British Life Offices was prepared,* and seeing that the construction and graduation of the original full length table was effected by methods totally different from those employed in the abridged process, the test was severe. Nevertheless the expectations of life by the abridged process came out as close to those derived by the full length process as in the case of English Life Tables Nos. 7 and 8. It would thus appear that the abridged process may safely be adopted when only a skeleton table is required, no matter how the original statistics were derived and treated.

I remain, Sir,

Your obedient Servant,

GEORGE KING.

* See The "Journal of the Institute of Actuaries," Vol. xlviii., pp. 299 and 300.

Table A.—ABRIDGED ENGLISH LIFE TABLE No. 8.

MALES.

AGE.	$\log p_x$	Δ	Δ^2	Δ^3	Δ^4	AGE.	$\log {}_5p_x$	$\log l_x$	l_x
11	79	34	12	38	—	11	451	5.00000	100000
16	113	46	26	46	—	16	660	4.99549	98967
21	159	20	20	8	—	21	836	.98889	97474
26	179	40	28	9	—	26	965	.98053	95616
31	219	68	19	26	—	31	1222	.97088	93515
36	287	87	45	11	—	36	1596	.95866	90920
41	374	132	56	60	—	41	2114	.94270	87640
46	506	188	116	28	—	46	2872	.92156	83476
51	694	304	144	62	—	51	4026	.89284	78134
56	998	448	206	198	—	56	5816	.85258	71216
61	1446	654	404	224	—	61	8416	.79442	62290
66	2100	1058	628	77	—	66	12410	.71026	51317
71	3158	1686	705	14	—	71	18895	.58616	38562
76	4844	2391	719	533	—	76	28717	.39721	24958
81	7235	3110	1252	3461	14116	81	42001	.11004	12884
86	10345	4362	2209	10655	14116	86	60640	.3.69003	4898
91	14707	2153	3446	24771	14116	91	76594	.08363	1212
96	15860	10599	33217	38887	—	96	97165	2.31769	208
101	27459	—	—	—	—	101	203863	1.34604	22
						106	—	1.30741	0

AGE.	l_x	Δ	Δ^2	Δ^3	$N'_{x 51}$	N'_x	AGE.	${}^o e_x$	Δ	Δ^2	${}^o e_{x+1}$
11	100000	1033	460	95	497104	5166263	11	52.16	448	17	51.70
16	98967	1493	365	122	490521	4669159	16	47.68	431	10	47.24
21	97474	1858	243	251	481918	4178638	21	43.37	421	3	42.94
26	95616	2101	494	191	471924	3696720	26	39.16	418	11	38.74
31	93515	2595	685	199	460026	3224796	31	34.98	407	13	34.57
36	90920	3280	884	294	445074	2764770	36	30.91	394	15	30.51
41	87640	4164	1178	398	426120	2319696	41	26.97	379	20	26.58
46	83476	5342	1576	432	401905	1893576	46	23.18	359	24	22.81
51	78134	6918	2008	39	370633	1491671	51	19.59	335	31	19.24
56	71216	8926	2047	265	330113	1121038	56	16.24	304	31	15.92
61	62290	10973	1782	933	279297	790925	61	13.20	273	35	12.91
66	51317	12755	849	2379	218846	511628	66	10.47	238	44	10.22
71	38562	13604	1530	2558	151862	292782	71	8.09	194	44	7.88
76	24958	12074	4088	212	87444	140920	76	6.15	150	35	5.98
81	12884	7986	4300	1618	38784	53476	81	4.65	115	34	4.52
86	4898	3686	2682	1864	12036	14692	86	3.50	81	11	3.40
91	1212	1004	818	654	2348	2656	91	2.69	70	21	2.62
96	208	186	164	—	286	308	96	1.99	49	—	1.93
101	22	22	—	—	22	22	101	1.50	—	—	1.46
106	0	—	—	—	—	—					

Table B.—ABRIDGED ENGLISH LIFE TABLE No. 7.

MALES.

AGE.	log p_x	Δ	Δ^2	Δ^3
12	85	49	1	19
17	134	48	20	57
22	182	28	37	25
27	210	65	12	10
32	275	77	22	31
37	352	99	53	19
42	451	152	72	43
47	603	224	115	38
52	827	339	153	40
57	1166	492	193	354
62	1658	685	547	44
67	2343	1232	591	158
72	3575	1823	433	1366
77	5398	2256	1799	77
82	7654	4055	1876	4157
87	11709	5931	2281	—
92	17640	3650	—	—
97	21290	—	—	—

Table C.—ABRIDGED ENGLISH LIFE TABLE No. 7.

MALES.

AGE.	log p_x	Δ	Δ^2	Δ^3	log $s p_x$	AGE.	log l_x	l_x
12	85	49	1	19	520	12	4.89097	77798
17	134	48	20	57	770	17	88577	76872
22	182	28	37	25	963	22	87807	75521
27	210	65	12	10	1170	27	86844	73865
32	275	77	22	31	1522	32	85674	71902
37	352	99	53	19	1943	37	84152	69426
42	451	152	72	43	2534	42	82209	66388
47	603	224	115	38	3426	47	79675	62625
52	827	339	153	40	4759	52	76249	57875
57	1166	492	193	354	6745	57	71490	51868
62	1658	685	547	44	9512	62	64745	44407
67	2343	1232	591	158	13951	67	55233	35672
72	3575	1823	433	1366	21316	72	41232	25871
77	5398	2256	1799	1366	31056	77	19966	15837
82	7654	4055	3165	1366	45387	82	3.88910	7746
87	11709	7220	4531	1366	71446	87	43523	2724
92	18929	11751	5897	1366	1.16061	92	2.72077	526
97	30680	17648	7263	—	1.86064	97	1.56016	36
102	48328	24911	—	—	—	102	1.69952	1
107	73239	—	—	—	—	—	—	—

Table C.—ABRIDGED ENGLISH LIFE TABLE No. 7—continued.

MALES—continued.

AGE.	l_x	Δ	Δ^2	Δ^3	N'_{x+1}	N'_x	AGE.	${}^o e_x$	Δ	Δ^2	${}^o e_{x+1}$
12	77798	926	425	120	386406	3851213	12	50.00	443	20	49.55
17	76872	1351	305	2	380453	3464807	17	45.57	423	10	45.14
22	75521	1656	307	206	372759	3084354	22	41.34	413	8	40.92
27	73865	1963	513	49	363600	2711595	27	37.21	405	14	36.80
32	71902	2476	562	163	352297	2347995	32	33.16	391	13	32.76
37	69426	3033	725	262	338273	1995698	37	29.25	373	15	28.87
42	66388	3763	987	270	320993	1657425	42	25.47	363	21	25.10
47	62625	4750	1257	197	299324	1336432	47	21.84	342	25	21.49
52	57875	6007	1454	180	271896	1037108	52	18.42	317	30	18.09
57	51868	7461	1274	208	237503	765212	57	15.25	287	28	14.95
62	44407	8735	1066	833	196298	527709	62	12.38	259	34	12.11
67	35672	9801	233	2176	149217	331411	67	9.79	225	47	9.55
72	25871	10034	1943	1126	98911	182194	72	7.54	178	31	7.34
77	15837	8091	3069	245	53910	83283	77	5.76	147	21	5.60
82	7746	5022	2824	1116	22485	29373	82	4.29	126	19	4.15
87	2724	2198	1708	1253	6120	6888	87	3.03	107	75	2.91
92	526	490	455	—	727	768	92	1.96	32	—	1.89
97	36	35	—	—	41	41	97	1.64	—	—	1.60
102	1	—	—	—	—	—	—	—	—	—	—

Table D.—COMPARISON OF THE EXPECTATIONS OF LIFE DERIVED BY THE ABRIDGED PROCESS WITH THOSE BY THE EXTENDED TABLE.

English Life Table No. 7. MALES.			English Life Table No. 8. MALES.		
AGE.	Abridged Process.	Extended Table.	AGE.	Abridged Process.	Extended Table.
12	50.00	50.00	11	52.16	52.18
17	45.57	45.57	16	47.68	47.68
22	41.34	41.34	21	43.37	43.37
27	37.21	37.21	26	39.16	39.16
32	33.16	33.15	31	34.98	34.98
37	29.25	29.25	36	30.91	30.90
42	25.47	25.47	41	26.97	26.97
47	21.84	21.84	46	23.18	23.18
52	18.42	18.42	51	19.59	19.59
57	15.25	15.25	56	16.24	16.24
62	12.38	12.38	61	13.20	13.19
67	9.79	9.79	66	10.47	10.47
72	7.54	7.54	71	8.09	8.09
77	5.76	5.74	76	6.15	6.14
82	4.29	4.30	81	4.65	4.64
87	3.03	3.10	86	3.50	3.51
92	1.96	2.32	91	2.69	2.76
97	1.64	1.91	96	1.99	2.32
			101	1.50	1.40

APPENDIX I.

STATISTICAL TABLES ON WHICH THE CONSTRUCTION OF THE LIFE TABLES WAS BASED.

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APPENDIX I.—TABLE 1.

ENGLAND AND WALES.

Census, 31 March, 1901. Populations enumerated.

Age last birthday.	Males.	Females.
0	399,875	396,932
1	363,424	364,371
2	366,824	368,586
3	363,161	366,966
4	362,077	364,492
0 to 4	1,855,361	1,861,347
5 " 9	1,738,993	1,748,298
10 " 14	1,670,970	1,670,770
15 " 19	1,607,522	1,638,621
20 " 24	1,472,644	1,648,278
25 " 29	1,328,288	1,496,221
30 " 34	1,157,666	1,273,665
35 " 39	1,034,459	1,110,924
40 " 44	897,484	953,138
45 " 49	759,955	813,233
50 " 54	636,254	692,749
55 " 59	497,498	555,079
60 " 64	410,447	480,226
65 " 69	282,403	347,270
70 " 74	195,465	250,868
75 " 79	113,096	151,384
80 " 84	52,137	76,631
85 " 89	14,915	24,046
90 " 94	2,687	5,515
95 " 99	322	868
100 and over	47	99
All Ages	15,728,613	16,799,230

APPENDIX I.—TABLE 2.

ENGLAND AND WALES.

Census, 2 April, 1911. Populations Enumerated.

Age last Birthday.	Total Males.	Females.			Age last Birthday.
		Total Females.	Single.	Married.	
0	395,110	386,618	386,618	—	0
1	374,109	368,709	368,709	—	1
2	395,919	393,376	393,376	—	2
3	388,669	388,682	388,682	—	3
4	382,306	380,885	380,885	—	4
5	374,037	373,979	373,979	—	5
6	372,572	372,977	372,977	—	6
7	372,988	373,497	373,497	—	7
8	366,223	367,697	367,697	—	8
9	361,475	361,351	361,351	—	9
10	359,062	359,621	359,621	—	10
11	351,287	352,220	352,220	—	11
12	349,205	350,306	350,306	—	12
13	345,144	345,588	345,588	—	13
14	342,933	344,322	344,322	—	14

Appendix I.—Table 2—*continued.*England and Wales—*continued.*

Census, 2 April, 1911.

Populations Enumerated—*continued.*

Age last Birthday.	Total Males.	Females.				Age last Birthday.
		Total Females.	Single.	Married.	Widowed.	
15	334,241	335,730	335,722	8	—	15
16	335,518	337,451	337,342	106	3	16
17	329,627	336,608	335,694	894	20	17
18	332,615	340,351	335,285	5,044	22	18
19	322,894	331,586	317,483	14,059	44	19
20	308,328	332,427	299,838	32,459	130	20
21	304,131	331,633	277,284	54,114	235	21
22	296,288	333,323	253,215	79,684	424	22
23	297,065	338,083	231,522	105,893	668	23
24	296,840	337,600	204,659	131,911	1,030	24
25	293,303	333,923	180,042	152,527	1,354	25
26	295,846	331,447	157,671	171,920	1,856	26
27	283,389	315,641	134,823	178,616	2,202	27
28	297,058	331,114	126,021	202,036	3,057	28
29	286,187	311,152	106,088	201,336	3,728	29
30	310,023	344,446	108,849	230,537	5,060	30
31	259,993	281,761	78,326	199,053	4,382	31
32	280,370	305,068	80,591	218,694	5,783	32
33	258,479	280,976	69,276	205,660	6,040	33
34	267,007	289,052	68,623	213,023	7,406	34
35	266,475	284,126	66,157	209,640	8,329	35
36	262,107	279,752	60,636	209,881	9,235	36
37	235,420	255,236	52,629	193,163	9,444	37
38	262,913	280,477	56,671	211,700	12,106	38
39	234,517	252,247	48,445	192,006	11,796	39
40	262,690	282,281	55,991	210,087	16,203	40
41	198,344	208,303	37,415	159,311	11,577	41
42	226,889	242,412	42,621	183,545	16,246	42
43	196,204	216,351	36,836	163,960	15,555	43
44	190,949	208,188	35,187	156,554	16,447	44
45	202,458	213,063	37,827	155,950	19,286	45
46	184,881	199,948	33,215	147,554	19,179	46
47	176,713	191,863	30,978	140,990	19,895	47
48	189,271	207,318	33,215	149,850	24,253	48
49	172,779	187,295	29,181	133,951	24,163	49
50	195,197	209,676	34,337	144,141	31,198	50
51	140,883	148,946	22,550	105,225	21,171	51
52	152,954	166,682	24,458	114,611	27,613	52
53	138,587	153,439	21,665	104,302	27,472	53
54	140,610	155,706	21,955	103,404	30,347	54
55	131,885	143,946	20,397	93,961	29,588	55
56	133,063	143,008	19,660	90,556	32,792	56
57	112,207	124,647	16,874	78,038	29,735	57
58	119,821	134,033	17,717	81,760	34,556	58
59	111,029	124,792	16,040	73,919	34,833	59
60	123,732	140,434	18,684	78,411	43,339	60
61	87,050	95,947	12,562	54,164	29,221	61
62	96,341	107,762	13,588	57,801	36,373	62
63	86,264	99,222	12,392	50,956	35,874	63
64	83,764	99,438	12,233	48,783	38,422	64
65	81,605	98,132	12,112	45,491	40,529	65
66	75,785	91,337	10,887	40,995	39,455	66
67	69,027	83,416	10,201	35,382	37,833	67
68	70,989	85,595	10,171	34,476	40,948	68
69	68,490	82,438	9,587	30,752	42,099	69

Appendix I.—Table 2—*continued.*England and Wales—*continued.*

Census, 2 April, 1911.

Populations Enumerated—*continued.*

Age last Birthday.	Total Males.	Females.				Age last Birthday.
		Total Females.	Single.	Married.	Widowed.	
70	61,686	79,137	10,104	27,276	41,757	70
71	47,362	61,057	7,472	20,229	33,356	71
72	48,014	65,860	7,991	19,965	37,904	72
73	41,939	57,750	6,963	16,136	34,651	73
74	37,867	52,881	6,291	13,605	32,985	74
75	34,012	47,351	5,692	11,373	30,286	75
76	29,010	41,855	5,006	9,154	27,695	76
77	24,875	35,185	4,193	7,113	23,879	77
78	22,358	32,584	3,929	5,857	22,798	78
79	17,211	25,488	3,019	4,062	18,407	79
80	16,589	25,465	3,185	3,597	18,683	80
81	12,177	17,893	2,131	2,309	13,453	81
82	11,065	17,271	2,039	1,943	13,289	82
83	8,941	14,338	1,754	1,444	11,140	83
84	7,631	12,794	1,545	1,092	10,157	84
85	5,870	9,769	1,192	733	7,844	85
86	4,571	8,030	980	515	6,535	86
87	3,541	6,194	790	350	5,054	87
88	2,554	4,657	574	240	3,843	88
89	1,921	3,571	438	147	2,986	89
90	1,448	2,897	386	119	2,392	90
91	926	1,936	274	66	1,596	91
92	676	1,486	194	48	1,244	92
93	395	884	112	27	745	93
94	294	618	104	8	506	94
95	213	464	65	8	391	95
96	131	324	43	7	274	96
97	82	195	27	6	162	97
98	50	135	18	6	111	98
99	29	67	12	2	53	99
100	17	45	7	3	35	100
101	10	23	5	—	18	101
102	2	14	4	—	10	102
103	1	3	—	—	3	103
104	1	2	—	—	2	104
105	3	3	1	—	2	105
106	—	—	—	—	—	106
107	—	1	—	—	1	107
108	1	—	—	—	—	108
109	—	—	—	—	—	109
110	—	1	—	—	1	110
111	1	—	—	—	—	111
ALL AGES	17,445,608	18,624,884	10,629,796	6,630,284	1,364,804	ALL AGES.

APPENDIX I.—TABLE 3.

ENGLAND AND WALES.—MALES.

Deaths Registered in each of the Ten Calendar Years 1901 to 1910.

Table with columns for Ages last Birthday (0-99 and ALL AGES) and rows for years 1901-1910. Includes sub-totals for 0 to 4 and 0 to 99.

APPENDIX I.—TABLE 4.

ENGLAND AND WALES.—FEMALES.

Deaths Registered in each of the Ten Calendar Years 1901 to 1910.

Table with columns for Ages last Birthday (0-99 and Forward) and rows for years 1901-1910. Includes sub-totals for 0 to 4 and Forward.

APPENDIX I.—TABLE 4—continued.

England and Wales.—Females—continued.

Deaths Registered in each of the Ten Calendar Years 1901 to 1910.

Table with columns for Ages last Birthday (Forward 0 to 99, 100-111, and ALL AGES) and rows for years 1901-1910. Includes sub-totals for Forward 0 to 99 and ALL AGES.

APPENDIX I.—TABLE 5.

ENGLAND AND WALES.

Deaths registered in each of the three years 1910, 1911, and 1912.

Table comparing MALES and FEMALES deaths by age group (Ages last Birthday) for the years 1910, 1911, 1912, and a Total column.

Appendix I.—Table 5—*continued.*

England and Wales—*continued.*

Deaths Registered in each of the Three Years 1910, 1911, and 1912—*continued.*

Ages last Birthday.	MALES.				Ages last Birthday.	FEMALES.			
	1910.	1911.	1912.	Total.		1910.	1911.	1912.	Total.
25	1,123	1,196	1,162	3,481	25	1,126	1,122	1,097	3,345
6	1,182	1,273	1,190	3,645	6	1,143	1,203	1,118	3,464
7	1,202	1,302	1,198	3,702	7	1,207	1,245	1,164	3,616
8	1,235	1,357	1,370	3,962	8	1,180	1,273	1,211	3,664
9	1,301	1,376	1,254	3,931	9	1,311	1,235	1,271	3,817
30	1,377	1,438	1,378	4,193	30	1,255	1,392	1,287	3,934
1	1,273	1,402	1,345	4,020	1	1,277	1,236	1,244	3,757
2	1,472	1,597	1,535	4,604	2	1,425	1,380	1,382	4,187
3	1,499	1,528	1,438	4,465	3	1,390	1,379	1,341	4,110
4	1,565	1,658	1,584	4,807	4	1,461	1,481	1,390	4,332
35	1,662	1,788	1,717	5,167	35	1,431	1,481	1,474	4,386
6	1,670	1,829	1,731	5,230	6	1,516	1,516	1,472	4,504
7	1,757	1,613	1,700	5,070	7	1,504	1,592	1,557	4,653
8	1,834	1,857	1,847	5,538	8	1,746	1,732	1,666	5,144
9	1,808	1,907	1,920	5,635	9	1,637	1,680	1,772	5,089
40	1,949	2,050	1,994	5,993	40	1,695	1,707	1,596	4,998
1	1,618	1,802	1,879	5,299	1	1,516	1,499	1,521	4,536
2	1,983	2,109	2,167	6,259	2	1,733	1,921	1,866	5,520
3	1,898	2,046	1,941	5,885	3	1,677	1,702	1,701	5,080
4	1,960	1,982	1,976	5,918	4	1,688	1,774	1,718	5,180
45	2,271	2,239	2,273	6,783	45	1,731	1,887	1,850	5,468
6	2,155	2,207	2,183	6,545	6	1,810	1,867	1,782	5,459
7	2,196	2,296	2,300	6,792	7	1,846	1,917	1,846	5,609
8	2,324	2,399	2,408	7,131	8	2,027	2,115	2,091	6,233
9	2,458	2,455	2,611	7,524	9	1,997	2,092	2,219	6,308
50	2,557	2,724	2,689	7,970	50	2,073	2,204	2,083	6,360
1	2,265	2,306	2,422	6,993	1	1,841	2,024	1,957	5,822
2	2,641	2,738	2,860	8,239	2	2,173	2,189	2,445	6,807
3	2,568	2,666	2,643	7,877	3	2,235	2,234	2,251	6,720
4	2,790	2,973	2,842	8,605	4	2,294	2,421	2,332	7,047
55	2,722	2,764	2,780	8,266	55	2,128	2,284	2,293	6,705
6	2,954	2,985	3,126	9,065	6	2,484	2,601	2,615	7,700
7	2,845	2,900	2,995	8,740	7	2,350	2,533	2,591	7,474
8	3,093	3,139	3,209	9,441	8	2,646	2,751	2,675	8,072
9	3,234	3,183	3,186	9,603	9	2,772	2,663	2,678	8,113
60	3,442	3,610	3,364	10,416	60	2,937	2,921	2,862	8,720
1	3,086	3,139	3,331	9,556	1	2,531	2,745	2,759	8,035
2	3,300	3,420	3,665	10,385	2	2,810	3,097	3,152	9,059
3	3,377	3,553	3,575	10,505	3	2,956	3,099	3,098	9,153
4	3,443	3,533	3,698	10,674	4	3,192	3,229	3,262	9,683
65	3,833	3,854	3,824	11,511	65	3,390	3,373	3,438	10,201
6	3,512	3,616	3,570	10,698	6	3,165	3,292	3,349	9,806
7	3,425	3,709	3,705	10,839	7	3,196	3,422	3,622	10,240
8	3,853	3,924	3,966	11,743	8	3,755	3,686	3,827	11,268
9	3,942	4,003	3,923	11,868	9	3,862	3,671	3,669	11,202
70	3,899	4,144	4,082	12,125	70	3,995	4,350	4,197	12,542
1	3,347	3,713	3,969	11,029	1	3,693	4,031	4,087	11,811
2	3,719	3,958	4,296	11,973	2	4,163	4,361	4,724	13,248
3	3,665	3,649	3,882	11,196	3	3,986	4,265	4,435	12,686
4	3,461	3,745	3,860	11,066	4	3,932	4,172	4,360	12,464
75	3,263	3,471	3,625	10,359	75	3,811	3,973	4,231	12,015
6	3,111	3,240	3,414	9,765	6	3,685	3,893	3,998	11,576
7	2,866	3,071	2,982	8,919	7	3,384	3,581	3,786	10,751
8	2,836	2,945	2,989	8,770	8	3,283	3,667	3,670	10,620
9	2,589	2,560	2,702	7,851	9	3,249	3,089	3,349	9,687

Appendix I.—Table 5—*continued.*

England and Wales—*continued.*

Deaths Registered in each of the Three Years 1910, 1911, and 1912—*continued.*

Ages last Birthday.	MALES.				Ages last Birthday.	FEMALES.			
	1910.	1911.	1912.	Total.		1910.	1911.	1912.	Total.
80	2,374	2,406	2,379	7,159	80	3,164	3,199	3,167	9,530
1	1,924	2,113	2,094	6,131	1	2,454	2,809	2,741	8,004
2	1,875	1,990	2,115	5,980	2	2,501	2,749	2,885	8,135
3	1,665	1,664	1,760	5,089	3	2,293	2,371	2,453	7,117
4	1,502	1,551	1,708	4,761	4	2,142	2,206	2,305	6,653
85	1,299	1,319	1,274	3,892	85	1,886	1,839	1,954	5,679
6	1,045	1,141	1,144	3,330	6	1,557	1,594	1,762	4,913
7	826	909	948	2,683	7	1,343	1,390	1,483	4,216
8	670	737	688	2,095	8	1,043	1,142	1,162	3,347
9	563	587	515	1,665	9	871	886	969	2,726
90	418	420	435	1,273	90	783	686	718	2,187
1	322	303	333	958	1	569	597	569	1,735
2	226	255	257	738	2	374	491	529	1,394
3	150	181	193	524	3	316	295	370	981
4	93	108	106	307	4	215	224	229	668
95	67	71	81	219	95	162	147	181	490
6	58	62	68	188	6	97	124	143	364
7	28	26	39	93	7	76	81	89	246
8	9	18	22	49	8	51	56	53	160
9	12	10	15	37	9	36	36	31	103
100 and over	22	18	17	57	100 and over	43	45	50	138
ALL AGES	249,016	272,512	250,232	771,760	ALL AGES	234,231	255,298	236,707	726,236

Centenarians.	
Age.	1912.
100	11
1	1
2	2
3	1
4	2
105	—
6	—
100 and over	17

Centenarians.	
Age.	1912.
100	19
1	15
2	10
3	4
4	—
105	1
6	1
100 and over	50

APPENDIX I.—TABLE 6.

ENGLAND AND WALES.

Deaths of Females registered in the three years 1910 to 1912 according to Marital Condition.

Ages last Birthday.	Single.	Married.	Widowed.	Total.	Ages last Birthday.	Single.	Married.	Widowed.	Total.
0	127,925	—	—	127,925	55	894	4,183	1,628	6,705
1	38,288	—	—	38,288	56	965	4,583	2,152	7,700
2	15,598	—	—	15,598	57	941	4,463	2,070	7,474
3	9,387	—	—	9,387	58	956	4,682	2,434	8,072
4	6,732	—	—	6,732	59	954	4,501	2,658	8,113
5	5,476	—	—	5,476	60	1,120	4,620	2,980	8,720
6	4,112	—	—	4,112	61	923	4,170	2,942	8,035
7	3,160	—	—	3,160	62	1,087	4,492	3,480	9,059
8	2,639	—	—	2,639	63	1,083	4,371	3,699	9,153
9	2,263	—	—	2,263	64	1,150	4,440	4,093	9,683
10	2,126	—	—	2,126	65	1,179	4,324	4,698	10,201
11	1,956	—	—	1,956	66	1,059	4,226	4,521	9,806
12	1,943	—	—	1,943	67	1,116	4,082	5,042	10,240
13	2,178	—	—	2,178	68	1,263	4,326	5,679	11,268
14	2,353	—	—	2,353	69	1,252	3,947	6,003	11,202
15	2,494	1	—	2,495	70	1,395	3,929	7,218	12,542
16	2,631	3	—	2,634	71	1,264	3,511	7,036	11,811
17	2,711	18	—	2,729	72	1,457	3,691	8,100	13,248
18	2,734	114	—	2,848	73	1,318	3,212	8,156	12,686
19	2,617	240	2	2,859	74	1,366	2,906	8,192	12,464
20	2,448	466	—	2,914	75	1,276	2,667	8,072	12,015
21	2,489	675	5	3,169	76	1,275	2,294	8,007	11,576
22	2,148	862	7	3,017	77	1,204	1,969	7,578	10,751
23	2,001	1,253	16	3,270	78	1,154	1,791	7,675	10,620
24	1,881	1,499	19	3,399	79	1,115	1,486	7,086	9,687
25	1,674	1,655	16	3,345	80	1,067	1,284	7,179	9,530
26	1,492	1,944	28	3,464	81	850	891	6,263	8,004
27	1,356	2,218	42	3,616	82	964	824	6,347	8,135
28	1,244	2,375	45	3,664	83	864	658	5,595	7,117
29	1,219	2,525	73	3,817	84	792	539	5,322	6,653
30	1,189	2,671	74	3,934	85	719	410	4,550	5,679
31	1,014	2,666	77	3,757	86	648	272	3,993	4,913
32	1,048	3,040	99	4,187	87	525	228	3,463	4,216
33	989	2,993	128	4,110	88	393	169	2,785	3,347
34	957	3,228	147	4,332	89	374	97	2,255	2,726
35	957	3,263	166	4,386	90	256	60	1,871	2,187
36	888	3,403	213	4,504	91	223	38	1,474	1,735
37	885	3,541	227	4,653	92	200	28	1,166	1,394
38	931	3,933	280	5,144	93	141	16	824	981
39	875	3,907	307	5,089	94	87	4	577	668
40	897	3,740	361	4,998	95	74	7	409	490
41	758	3,457	321	4,536	96	45	5	314	364
42	889	4,170	461	5,520	97	27	3	216	246
43	835	3,793	452	5,080	98	20	—	140	160
44	906	3,716	558	5,180	99	17	3	83	103
45	940	3,867	661	5,468	100 and over	19	3	116	138
46	961	3,821	677	5,459					
47	888	3,912	809	5,609					
48	946	4,329	958	6,233					
49	997	4,250	1,061	6,308					
50	979	4,245	1,136	6,360					
51	887	3,817	1,118	5,822					
52	1,026	4,375	1,406	6,807	ALL AGES	317,847	207,213	201,176	726,236
53	910	4,325	1,485	6,720					
54	949	4,498	1,600	7,047					

Appendix I.—Table 6—continued.

England and Wales—continued.

Deaths of Females registered in the two years 1911 to 1912 according to Marital Condition.

Centenarians, Two Years 1911 and 1912.									
Ages last Birthday.	Single.	Married.	Widowed.	Total.	Ages last Birthday.	Single.	Married.	Widowed.	Total.
100	5	1	30	36	105	—	—	3	3
101	4	—	24	28	106	—	—	2	2
102	2	—	16	18	107	—	—	—	—
103	—	2	4	6	108	1	—	—	1
104	—	—	1	1	TOTAL	12	3	80	95

APPENDIX I.—TABLE 7.

ENGLAND AND WALES.

Births, and Deaths of Infants.

MALES.

Calendar Year.	BIRTHS.	DEATHS.				
		0-1.	1-2.	2-3.	3-4.	4-5.
1894	453,016	67,786	18,107	7,046	4,549	3,220
5	468,886	82,655	21,491	7,463	4,441	3,118
6	465,660	74,966	19,854	7,737	5,075	3,721
7	469,180	79,897	19,649	7,157	4,183	3,028
8	468,920	82,147	19,848	6,954	4,279	2,969
9	473,172	83,565	18,653	7,065	4,297	3,185
1900	471,044	79,458	19,417	7,134	4,492	3,370
1	473,944	78,493	17,515	6,328	4,150	3,095
2	479,144	70,334	16,845	6,509	4,208	3,089
3	482,229	69,723	16,590	5,895	3,587	2,577
4	481,322	67,378	18,776	6,500	3,817	2,749
1905	472,886	66,768	15,761	6,051	3,698	2,632
6	476,939	69,070	15,971	5,929	3,590	2,618
7	467,728	60,926	15,514	6,126	3,907	2,669
8	478,410	63,594	14,895	5,580	3,415	2,450
9	466,463	56,026	14,146	5,941	3,426	2,621
1910	457,266	53,155	13,251	5,020	2,950	2,168
11	448,933	63,874	16,326	5,822	3,449	2,386
12	445,004	47,004	12,000	5,074	3,240	2,341

FEMALES.

1894	437,273	54,013	17,115	6,979	4,568	3,193
5	453,405	65,438	20,032	7,290	4,537	3,174
6	449,671	60,047	19,142	7,809	5,147	3,655
7	452,503	63,692	18,192	6,876	4,330	3,068
8	454,245	65,866	18,662	6,849	4,277	2,914
9	455,474	67,410	17,412	6,703	4,442	3,040
1900	456,018	63,454	17,823	6,839	4,630	3,343
1	455,863	62,155	16,449	6,277	4,184	3,101
2	461,365	54,662	15,562	6,357	4,267	3,191
3	466,042	54,995	15,074	5,731	3,591	2,577
4	464,067	61,014	17,375	6,332	3,950	2,787
1905	456,407	52,323	14,751	5,816	3,811	2,647
6	458,142	54,825	14,985	5,489	3,613	2,591
7	450,314	47,052	14,522	5,862	3,749	2,926
8	461,973	49,660	13,672	5,269	3,338	2,446
9	448,009	43,404	13,190	5,372	3,516	2,622
1910	439,696	41,424	12,139	4,765	2,879	2,095
1	432,205	50,726	15,069	5,733	3,370	2,315
2	427,733	35,775	11,080	5,100	3,138	2,322

APPENDIX I.—TABLE 8.

ENGLAND AND WALES.

Deaths of Infants under 1 year of age registered in the years 1910, 1911, and 1912.

AGE.	MALES.				AGE.	FEMALES.			
	1910.	1911.	1912.	Total, 3 years.		1910.	1911.	1912.	Total, 3 Years.
Under 1 day...	5,950	5,818	5,666	17,434	Under 1 day...	4,400	4,418	4,180	12,998
1 day...	6,464	6,521	6,527	19,512	1 day...	4,784	4,667	4,719	14,170
1 week...	2,725	2,949	2,803	8,477	1 week...	2,151	2,281	2,068	6,500
2 weeks...	2,644	3,015	2,477	8,136	2 weeks...	1,963	2,227	1,874	6,064
3 "...	2,008	2,222	1,875	6,105	3 "...	1,416	1,699	1,358	4,473
Total under 1 month.	19,791	20,525	19,348	59,664	Total under 1 month.	14,714	15,292	14,199	44,205
1 month...	5,806	7,093	5,268	18,167	1 month...	4,396	5,159	3,651	13,206
2 months...	4,391	5,289	3,791	13,471	2 months...	3,375	4,275	2,681	10,331
3 "...	3,493	4,776	2,794	11,063	3 "...	2,878	3,845	2,259	8,982
4 "...	3,082	4,237	2,305	9,624	4 "...	2,442	3,441	1,822	7,705
5 "...	2,799	3,715	2,126	8,640	5 "...	2,145	3,001	1,627	6,773
Total under 6 months.	39,362	45,635	35,632	120,629	Total under 6 months.	29,950	35,013	26,239	91,202
6 months...	2,650	3,582	2,052	8,284	6 months...	2,002	2,943	1,612	6,557
7 "...	2,448	3,310	2,024	7,782	7 "...	2,073	2,778	1,530	6,381
8 "...	2,310	3,013	1,998	7,321	8 "...	1,952	2,747	1,679	6,378
9 "...	2,271	2,972	1,852	7,095	9 "...	1,891	2,452	1,568	5,911
10 "...	2,163	2,737	1,721	6,621	10 "...	1,781	2,350	1,583	5,714
11 "...	1,951	2,625	1,725	6,301	11 "...	1,775	2,443	1,564	5,782
Total under 1 year.	53,155	63,874	47,004	164,033	Total under 1 year.	41,424	50,726	35,775	127,925

APPENDIX I.—TABLE 9.

SECTIONAL LIFE TABLES.

Sums of the Estimated Population in the middle of the Years 1911 and 1912.

MALES.				
Ages last Birthday.	County of London.	County Boroughs.	Urban Districts.	Rural Districts.
0 to 4	468,852	1,221,104	1,376,790	836,642
5 " 9	431,602	1,142,649	1,319,643	830,167
10 " 14	397,791	1,073,164	1,239,744	811,922
15 " 19	386,287	1,001,929	1,172,344	774,963
20 " 24	381,816	923,794	1,070,862	652,535
25 " 29	379,013	916,157	1,039,807	599,765
30 " 34	347,777	876,614	990,787	558,553
35 " 39	315,699	795,827	906,654	524,529
40 " 44	271,846	667,022	762,241	465,907
45 " 49	233,953	566,133	643,913	422,212
50 " 54	193,819	460,432	527,844	366,040
55 " 59	147,892	359,135	416,752	301,195
60 " 64	115,263	274,365	321,730	249,989
65 " 69	84,407	197,577	243,778	211,293
70 " 74	52,002	121,130	157,124	146,921
75 " 79	26,436	58,555	83,467	88,287
80 " 84	11,268	23,807	36,727	41,814
85 and over	4,484	8,567	14,588	18,135
ALL AGES	4,250,207	10,687,961	12,324,795	7,900,869

APPENDIX I.—TABLE 10.

FEMALES.				
Ages last Birthday.	County of London.	County Boroughs.	Urban Districts.	Rural Districts.
0 to 4	465,719	1,212,542	1,364,891	824,645
5 " 9	435,444	1,152,547	1,321,273	819,617
10 " 14	405,945	1,093,271	1,247,189	785,484
15 " 19	424,790	1,084,183	1,212,434	668,349
20 " 24	475,666	1,082,053	1,191,308	623,025
25 " 29	462,207	1,039,581	1,153,513	616,591
30 " 34	402,607	961,352	1,077,880	584,454
35 " 39	358,529	853,555	970,121	542,515
40 " 44	307,769	719,822	822,869	482,630
45 " 49	264,006	615,921	702,610	431,427
50 " 54	217,799	509,490	583,019	371,144
55 " 59	170,196	402,174	467,245	311,088
60 " 64	136,963	316,989	377,868	261,797
65 " 69	107,784	248,563	305,722	226,106
70 " 74	77,414	174,573	218,215	167,721
75 " 79	44,979	93,256	125,040	104,213
80 " 84	22,001	41,932	59,918	52,904
85 and over	11,030	17,827	27,861	26,472
ALL AGES	4,790,848	11,619,631	13,228,976	7,900,182

APPENDIX I.—TABLE 11.

SECTIONAL LIFE TABLES.

Sums of the Deaths in the two Years 1911 and 1912.

MALES.

Ages last Birthday.	County of London.	County Boroughs.	Urban Districts.	Rural Districts.
0 to 4	20,687	60,645	54,888	25,296
5 " 9	1,473	4,417	4,166	2,114
10 " 14	849	2,309	2,294	1,359
15 " 19	1,067	3,216	3,510	1,978
20 " 24	1,350	3,763	3,837	2,230
25 " 29	1,683	4,417	4,230	2,348
30 " 34	2,126	5,466	4,755	2,556
35 " 39	2,697	6,670	5,723	2,819
40 " 44	3,184	7,368	6,189	3,205
45 " 49	3,696	8,654	7,303	3,718
50 " 54	4,119	9,657	8,651	4,436
55 " 59	4,350	10,735	9,828	5,354
60 " 64	4,750	11,818	11,547	6,773
65 " 69	4,779	11,963	12,671	8,681
70 " 74	4,458	11,697	13,177	9,966
75 " 79	3,325	7,941	10,208	9,525
80 " 84	2,059	4,478	6,253	6,990
85 " 89	878	1,817	2,961	3,606
90 " 94	256	487	753	1,095
95 " 99	47	60	132	173
100 " 104	4	3	13	12
105 and over	—	1	1	1
ALL AGES	67,837	177,582	173,090	104,235

APPENDIX I.—TABLE 12.

FEMALES.

Ages last Birthday.	County of London.	County Boroughs.	Urban Districts.	Rural Districts.
0 to 4	17,492	51,131	45,734	20,271
5 " 9	1,373	4,450	4,113	2,048
10 " 14	806	2,489	2,436	1,408
15 " 19	1,005	3,199	3,195	1,787
20 " 24	1,239	3,709	3,580	2,050
25 " 29	1,516	4,057	4,049	2,317
30 " 34	1,707	4,643	4,556	2,606
35 " 39	2,189	5,764	5,212	2,777
40 " 44	2,551	6,063	5,542	2,849
45 " 49	2,967	7,034	6,483	3,182
50 " 54	3,179	7,827	7,258	3,876
55 " 59	3,471	8,883	8,527	4,803
60 " 64	3,860	10,081	10,435	5,848
65 " 69	4,364	11,455	11,814	7,716
70 " 74	5,016	13,346	14,924	9,696
75 " 79	4,371	10,497	12,730	9,639
80 " 84	3,363	6,940	9,108	7,474
85 " 89	1,921	3,218	4,670	4,372
90 " 94	657	963	1,517	1,571
95 " 99	129	178	327	307
100 " 104	8	18	28	35
105 and over	1	—	2	3
ALL AGES	63,185	165,945	166,240	96,635

APPENDIX II.

THE MATHEMATICAL FORMULAS EMPLOYED IN THE CONSTRUCTION OF THE LIFE TABLES.

Section 1.—THE MEAN POPULATION.

The mean population for the interval between two censuses may be taken in various ways. We may have the arithmetical mean of the two enumerations. Let P_1 be the population at one census, and P_2 that at another taken n years later. Then the arithmetical mean is $\frac{1}{2}(P_1 + P_2)$, which is likewise the population at the middle of the period on the assumption of increase in arithmetical progression. Also, on the same assumption, the years lived during the period amount to $\frac{n}{2}(P_1 + P_2)$.

The assumption of arithmetical progression for the increase of population is not, however, natural; and although the formula has sometimes been used, it cannot give accurate results. If, however, the rate of increase in the population be not very rapid, and if the interval between the censuses be not very long, the error is not of great importance. Nevertheless, population begets population, and it is therefore more reasonable to assume that populations increase from census to census in geometrical progression, and to frame the formulas accordingly.

As before, let P_1 be the population at one census, and P_2 that at another, n years later; and let $P_2 = rP_1$. Then, on the assumption of geometrical progression, the geometrical mean is $r^{\frac{n}{2}}P_1$, which is also the population at the middle of the period. Adopting this formula, it has sometimes been assumed that the years lived during the period amount to $nr^{\frac{n}{2}}P_1$, but, again, an error is thereby introduced, because the geometrical mean of the populations at the beginning and the end of the period is not the same thing as the equivalent population constantly living throughout the period. That mean population, which will give the years lived, is the function required for present purposes.

Still assuming geometrical progression, let the population at the first census be P_1 and at the second P_2 , and let $P_2 = rP_1$. Also, let P without suffix represent the true mean population which is required, and let the intercensal period be n years. Then the population at any time, t , after the first census will be $r^t P_1$. To find P we must integrate $r^t P_1$, and take the integral between the limits 0 and 1, the census period being taken as the unit of time. That is

$$P = \int_0^1 P_1 r^t dt = P_1 \frac{r-1}{\lambda r} = P_1 \frac{\kappa(r-1)}{\log r} \dots (1)$$

where " λ " stands for Naperian and " \log " for common logarithms, and where κ is the modulus. The years lived during the n years will then be nP .

Equation (1) would give the true mean population corresponding to the deaths of the n calendar years, only if the censuses were taken on 1 January in each case, so as to have the deaths central to the census period. But if the censuses be taken at a fraction, c , of a year later than 1 January, a correction must be made by integrating between the limits $-\frac{c}{n}$ and $1 - \frac{c}{n}$. We take $\frac{c}{n}$ because that is the fraction of the census period by which the censuses are to be antedated. The effect of the change in the limits of the integral is to multiply the result in equation (1) by $r^{-\frac{c}{n}}$, or to divide it by $r^{\frac{c}{n}}$. Therefore, we have finally,

$$P = P_1 \frac{\kappa(r-1)}{r^{\frac{c}{n}} \log r} \dots (2)$$

The mean population given in equation (2) will, when multiplied by 10 for decennial censuses, give the years lived corresponding to the deaths in the 10 years.

Formula (2) gives the true mean when we apply it to the total population, taking r as the rate of increase of that total population for the intercensal period; or it gives the true mean population for a group when we derive r from the population of that group. But it breaks down when we have a population divided into groups, and when we wish to ascertain the mean of the total population, and of each of the several groups, separately. If we use for the groups the value of r derived from the total population, we do not get the true mean populations of the groups, because they do not all increase in the same ratio; and if we treat each group with its own value of r and take the sum, we do not get the true mean of the total population. By a very ingenious device, the late Mr. A. C. Waters, Chief Clerk, General Register Office, overcame this difficulty. He first published his method in a short and most interesting paper in the *Journal of the Royal Statistical Society*, vol. lxiv, p. 293; and he went again into the matter in Part I. of the Supplement to the 65th Annual Report

of the Registrar-General, p. cxvii. On both occasions he dealt with the populations of districts as compared with the population of the total area; but the method is equally applicable to age groups in the data for the construction of a mortality table, and was used for the London Life Table (see page 3 of Sir Shirley F. Murphy's Report) and also for the more recent tables of the Registrar-General. The following is a demonstration of the formula of Mr. Waters.

Let P_1 be the total population at the first census, and let it increase in geometrical progression to rP_1 at the second, n years later: and let π_1 be the population in any particular group at the first census, and π_2 that at the second, and let

$$\pi_1 = aP_1 \text{ and } \pi_2 = \beta(rP_1)$$

and let a pass to β during the n years in arithmetical progression. Then, after a period, t , the proportion of π_2 to P_2 will be $a + (\beta - a)t$. That is

$$\pi_t = r^t P_1 \{a + (\beta - a)t\}$$

$$= aP_1(1 - t)r^t + (\beta rP_1) \frac{tr^t}{r}$$

But $(aP_1) = \pi_1$, and $(\beta rP_1) = \pi_2$.

Therefore
$$\pi_t = \pi_1(1 - t)r^t + \pi_2 \frac{tr^t}{r} \dots \dots \dots (4)$$

Now to obtain the mean population of the group during any time, say from h to $h + t$, we must integrate, and take the integral within these limits. That is, if π be the mean population of the group,

$$\pi = \pi_1 \int_h^{h+t} r^t dt - \pi_1 \int_h^{h+t} tr^t dt + \frac{\pi_2}{r} \int_h^{h+t} tr^t dt \dots \dots \dots (5)$$

The value of the first integral on the right of equation (5) is $\frac{r^h(r^t - 1)}{\lambda r}$. For the other two terms we must evaluate the integral $\int tr^t dt$. This is easily done by integrating by parts. We have

$$\int tr^t dt = \int t \frac{dr^t}{\lambda r}$$

$$= \frac{1}{\lambda r} (tr^t - \int r^t dt)$$

$$= \frac{tr^t}{\lambda r} - \frac{r^t}{(\lambda r)^2}$$

or between the limits h and $h + t$

$$\int_h^{h+t} tr^t dt = \frac{(h+t)r^{h+t}}{\lambda r} - \frac{hr^h}{\lambda r} - \frac{r^{h+t}}{(\lambda r)^2} + \frac{r^h}{(\lambda r)^2} \\ = \frac{r^h}{\lambda r} \left\{ (h+t)r^t - h - \frac{r^t}{\lambda r} + \frac{1}{\lambda r} \right\} \dots \dots \dots (6)$$

Therefore,

$$\pi = \frac{\pi_1 r^h}{\lambda r} \left\{ (r^t - 1) - (h+t)r^t + h + \frac{r^t}{\lambda r} - \frac{1}{\lambda r} \right\} \\ + \frac{\pi_2 r^h}{r \lambda r} \left\{ (h+t)r^t - h - \frac{r^t}{\lambda r} + \frac{1}{\lambda r} \right\} \dots \dots \dots (7)$$

If now the censuses are taken the fraction c of a year on in the year, we must write $\frac{c}{n}$ for h . Also, we must take $t=1$. We thus have for the mean population of the group for the intercensal period,

$$\pi = \frac{\pi_1}{r^n \lambda r} \left\{ (r - 1) \left(\frac{c}{n} + \frac{1}{\lambda r} \right) - 1 \right\} \\ + \frac{\pi_2}{r^n \lambda r} \left\{ 1 - \frac{r-1}{r} \left(\frac{c}{n} + \frac{1}{\lambda r} \right) \right\} \dots \dots \dots (8)$$

This value must be multiplied by n to give the years lived in the intercensal period. For the purpose of numerical calculation, it is convenient to write $\frac{\log r}{\kappa}$ for λr .

The correctness of formula (8) is evident, because if we substitute P_1 for π_1 and rP_1 for π_2 we at once have formula (2).

The above formula was used by Mr. Finch in constructing English Life Table No. 6, so that in this respect the methods for Tables Nos. 6 and 7 are identical, and the tables are strictly comparable. The late Mr. Waters, however, revised his formula, and the revision was published in the Annual Report of the Registrar-General for 1907, page cxxxii. The original and the revised formulas do not differ much in the results produced, and either may be used without affecting appreciably the life table.

Section 2.—GRADUATED QUINQUENNIAL PIVOTAL VALUES.

The following is a demonstration of the formula used for obtaining the graduated pivotal values employed in the construction of all the Life Tables embodied in this report.

Let there be a series of fifteen values of u , the function to be dealt with, from u_0 to u_{14} . To find the graduated value of u , the central term of the series.

Let y be the finite integral of the function u , so that $y_x = \sum_0^{x-1} u$; and let Δy , $\Delta^2 y$, etc., be the differences of y for quinquennial intervals, so that $\Delta y_0 = \sum_0^4 u$, $\Delta y_5 = \sum_5^9 u$, etc.

Then
$$u_7 = y_8 - y_7$$

But
$$y_8 = y_0 + \frac{8}{5} \Delta y_0 + \frac{24}{50} \Delta^2 y_0 - \frac{8}{125} \Delta^3 y_0$$

$$y_7 = y_0 + \frac{7}{5} \Delta y_0 + \frac{14}{50} \Delta^2 y_0 - \frac{7}{125} \Delta^3 y_0$$

$$u_7 = \frac{1}{5} \Delta y_0 + \frac{1}{5} \Delta^2 y_0 - \frac{1}{125} \Delta^3 y_0 \\ = \cdot 2 \Delta y_0 - \cdot 008 \Delta^3 y_0$$

The differences, Δ , of y are the sums of five values of the function u , and may be represented by the symbol w , so that

$$w_x = u_x + u_{x+1} + \dots + u_{x+4}$$

Making this change in notation, we have

$$u_7 = \cdot 2w_5 - \cdot 008 \Delta^2 w_0$$

In the case of Life Tables constructed from Census Returns and Records of Deaths, the function u_x of the formula is the population or the deaths as the case may be at age x , and the function w_x is the sum of five values of the population or deaths for ages x to $x+4$, and it will be observed that the graduated function is that for an age seven years older than the first age in the series of fifteen values embraced in the formula.

The following is an example of the application of the formula. It relates to the populations of the Life Table for the County of London Males given in Table 9 of Appendix I. For ages under 5 the formula does not apply, because of the rapid change in the law of mortality in infancy and early childhood, and the first group that can be employed is that for ages 5 to 9 last birthday, giving the earliest available pivotal value at age 12.

In the example the differences have been placed centrally with regard to the original groups, so as to bring $\Delta^2 w_0$ against the group w_5 , as by this arrangement the arithmetical work is made much more easy.

Where the pivotal value comes out with fewer than five integral places, it is well to bring in decimal places, and for the purposes of verification it is well to retain all the three decimal places which the formula produces.

To check the pivotal values we sum the columns of estimated population, and of second differences, and apply the formula to the sums. The result should be the sum of the graduated populations. Thus, in the example, the sum of the estimated populations for the groups 10-14 to 70-74 inclusive is 3,307,565, and the algebraical sum of the second differences is +8245. By applying the formula we have 661,447. The actual sum of the corresponding portion of the column of graduated population is 661,446, the difference of unity being due to the neglected decimal places.

Again, the sum of the column of estimated populations for the groups 75-79 to 95-99 inclusive is 42,178, and the sum of the second differences is +25462, and the result of applying the formula is 8231.904, which is the exact sum of this portion of the column of graduated populations. The check is applied separately to the integral and the decimal portions of the column of graduated population, or otherwise there would be differences in the decimals.

In the example, positive quantities are printed in Ionic type, and negative in Italic type. In actual working positive quantities would be written in black ink, and negative in red ink.

COUNTY OF LONDON—MALES.

POPULATION.

GRADUATED QUINQUENNIAL PIVOTAL VALUES.

Ages.	Estimated Population.	Δ	Δ^2	Age.	Graduated Population.
	w_x	Δw_x	$\Delta^2 w_x$		
5- 9	431602	33811	22307	12	79380
10- 14	397791	11504	7033	17	77201
15- 19	386287	4471	1668	22	76350
20- 24	381816	2803	28433	27	76030
25- 29	379013	31236	842	32	69562
30- 34	347777	32078	11775	37	63234
35- 39	315699	43853	5960	42	54322
40- 44	271846	37893	2241	47	46809
45- 49	233953	40134	5793	52	38808
50- 54	193819	45927	13298	57	29472
55- 59	147892	32629	1773	62	23038
60- 64	115263	30856	1549	67	16894
65- 69	84407	32405	6839	72	10346
70- 74	52002	25566	10398	77	5204·016
75- 79	26436	15168	7524	82	2193·408
80- 84	11268	7644	4760	87	686·720
85- 89	3624	2884	2254	92	129·968
90- 94	740	630	526	97	17·792
95- 99	110	104			
100-104	6				

Section 3.—OSCULATORY INTERPOLATION.

In the process of constructing a life table by the method employed in this report we first find the values at quinquennial intervals of a function such as q_x , see Appendix II, Section 2, and then by interpolation we insert four intervening values in each of the spaces. Were the ordinary formula of finite differences used

$$u_x = u_0 + x\Delta u_0 + \frac{x(x-1)}{2}\Delta^2 u_0 + \frac{x(x-1)(x-2)}{6}\Delta^3 u_0$$

to fill in the interval u_1 to u_2 by means of the four values $u_0, u_1, u_2,$ and u_3 , and were the process repeated to fill in the interval u_2 to u_3 by means of the four values $u_1, u_2, u_3,$ and u_4 , there would be a break in the resulting curves at the point u_2 , and were the process to be repeated down the table there would be a similar break at each quinquennial point, and the life table would have a very rough and unsatisfactory graduation. To overcome this difficulty Dr. Thomas Bond Sprague devised the method of Osculatory Interpolation, and published it in a remarkable paper in the *Journal of the Institute of Actuaries*, vol. xxii, page 270. He used five orders of differences, and, taking six consecutive equidistant values $u_0, u_1, u_2, u_3, u_4,$ and u_5 , he solved the problem by arranging that the

two curves of the fifth order which meet at the point u_2 should have at that point the same first differential coefficient and also the same second differential coefficient; that is that they should have at the point of junction the same gradient and the same radius of curvature.

Five orders of differences may prove of advantage for curves other than mortality curves, but it is found by experience that for the purpose of constructing life tables three orders of differences are quite sufficient. The curves are of the third order instead of the fifth, and the two curves which meet at any particular point will have at that point the same gradient, but not necessarily the same radius of curvature, because we must leave out of account the second differential coefficient.

Retaining then only three orders of differences, the following is Dr. Sprague's method (somewhat simplified) of deducing the formula.

We have four points, $u_0, u_1, u_2,$ and u_3 , and the problem is, to interpolate by third differences between the points u_1 and u_2 in such a way as to obtain a smooth junction when the series is continued in each direction by interpolation in like manner between the points u_0 and u_1 , and between the points u_2 and u_3 . To solve the problem we arrange that the two curves of the third order which meet at the point u_1 shall have the same first differential coefficient at that point; and we find the value of that differential coefficient by means of a curve of the second order passing through the points $u_0, u_1,$ and u_2 ; and similarly for the point u_2 .

In the analysis we use the symbol Δ for the differences when the intervals are quinquennial, and the symbol δ when the intervals are annual.

The required equation to the interpolation curve of the third order between the points u_1 and u_2 may be written,

$$u_{1+x} = u_1 + ax + bx^2 + cx^3 \dots \dots \dots (1)$$

whence

$$u_2 = u_1 + a + b + c$$

$$a + b + c = u_2 - u_1 = \Delta u_1 = \Delta u_0 + \Delta^2 u_0 \dots \dots \dots (2)$$

Differentiating equation (1),

$$\frac{du_{1+x}}{dx} = a + 2bx + 3cx^2$$

whence

$$\frac{du_1}{dx} = a, \text{ and } \frac{du_2}{dx} = a + 2b + 3c \dots \dots \dots (3)$$

The curve of the second order passing through the points $u_0, u_1,$ and u_2 may be written

$$u_x = u_0 + x\Delta u_0 + \frac{1}{2}(x^2 - x)\Delta^2 u_0$$

whence

$$\frac{du_x}{dx} = \Delta u_0 + \frac{1}{2}(2x - 1)\Delta^2 u_0$$

and

$$\frac{du_1}{dx} = \Delta u_0 + \frac{1}{2}\Delta^2 u_0;$$

and therefore from equation (3)

$$a = \Delta u_0 + \frac{1}{2}\Delta^2 u_0 \dots \dots \dots (4)$$

Similarly, from the curve of the second order passing through the points $u_1, u_2,$ and u_3 ,

$$\frac{du_2}{dx} = \Delta u_1 + \frac{1}{2}\Delta^2 u_1$$

$$= \Delta u_0 + \frac{3}{2}\Delta^2 u_0 + \frac{1}{2}\Delta^3 u_0$$

and from equation (3)

$$a + 2b + 3c = \Delta u_0 + \frac{3}{2}\Delta^2 u_0 + \frac{1}{2}\Delta^3 u_0 \dots \dots \dots (5)$$

By means of equations (2), (4), and (5) we find

$$a = \Delta u_0 + \frac{1}{2}\Delta^2 u_0$$

$$b = \frac{1}{2}\Delta^2 u_0 - \frac{1}{2}\Delta^3 u_0$$

$$c = \frac{1}{2}\Delta^3 u_0.$$

and after reduction, equation (1) becomes

$$u_{1+x} = u_1 + x\Delta u_1 + \frac{x+x^2}{2}\Delta^2 u_1 - \frac{x^3-x^2}{2}\Delta^3 u_1$$

By differencing this last equation for the interval $\frac{1}{t}$, we have the scheme

$$\delta u_1 = \frac{\Delta u_1}{t} + \frac{t+1}{2} \cdot \frac{\Delta^2 u_1}{t^2} - \frac{t-1}{2} \cdot \frac{\Delta^3 u_1}{t^3}$$

$$\delta^2 u_1 = \frac{\Delta^2 u_1}{t^2} - (t-3) \frac{\Delta^3 u_1}{t^3}$$

$$\delta^3 u_1 = \frac{3\Delta^3 u_1}{t^3}$$

When t is taken equal to 5, the differences become

$$\begin{aligned} \delta u_1 &= \frac{\Delta u_0}{5} + 3 \frac{\Delta^2 u_0}{25} - 2 \frac{\Delta^3 u_0}{125} \\ \delta^2 u_1 &= \frac{\Delta^2 u_0}{25} - 2 \frac{\Delta^3 u_0}{125} \\ \delta^3 u_1 &= \frac{3 \Delta^3 u_0}{125} \end{aligned}$$

or

$$\begin{aligned} \delta u_1 &= (\cdot 2) \Delta u_0 + 3(\cdot 04) \Delta^2 u_0 - 2(\cdot 008) \Delta^3 u_0 \\ \delta^2 u_1 &= (\cdot 04) \Delta^2 u_0 - 2(\cdot 008) \Delta^3 u_0 \\ \delta^3 u_1 &= 3(\cdot 008) \Delta^3 u_0 \end{aligned}$$

The second form of the differences is convenient when an arithmometer is not available. The quinquennial differences are modified by multiplying all the way down the table Δ by $(\cdot 2)$, Δ^2 by $(\cdot 04)$, and Δ^3 by $(\cdot 008)$; and the multiplication by the remaining coefficients can be done mentally with great ease.

The work can be done very rapidly on an arithmometer if we write the differences as follows

$$\begin{aligned} \delta u_1 &= \cdot 2 \Delta u_0 + \cdot 12 \Delta^2 u_0 - \cdot 016 \Delta^3 u_0 \\ \delta^2 u_1 &= \cdot 04 \Delta^2 u_0 - \cdot 016 \Delta^3 u_0 \\ \delta^3 u_1 &= \cdot 024 \Delta^3 u_0 \end{aligned}$$

Other methods of applying the principle of osculatory interpolation have been devised which some people think reduce the amount of arithmetical work. In mathematical theory, however, they are certainly less simple, and therefore it has been thought better to adhere to Dr. Sprague's original plan.

A numerical example is appended to illustrate the practical application of the method of osculatory interpolation. It is taken from the construction of the life table for the County of London Males. Table A gives the calculation of the osculatory differences, and Table B the actual interpolation. Positive quantities are printed in Ionic type and negative in Italic type. In actual working positive quantities would be written in black ink, and negative in red ink.

In Table B for convenience the differences are written in reverse order and at the age points 17, 22, etc. they are of course the same as in Table A. They are carried out to eight decimal places although only five are to be retained. This is in order that a complete check may be obtained at every fifth age, because when from age 17, for instance, we come down by summation of difference to age 22, if the work be done correctly $\log(q_{22} + \cdot 1)$ is exactly reproduced.

It may be mentioned that in the case of some of the life tables the transitions from positive differences to negative, and *vice versa* are much more marked than in the example chosen.

TABLE A.

CALCULATION OF OSCULATORY DIFFERENCES.

COUNTY OF LONDON—MALES.

Age.	$\log(q_x + \cdot 1)$.	Δ	Δ^2	Δ^3	Age.	δ	δ^2	δ^3
12	$\bar{1}\cdot 00881$	297	27	21	17	62304	744	504
17	$\cdot 01178$	324	48	269	22	66256	2384	6456
22	$\cdot 01502$	372	317	22	27	112792	13032	528
27	$\cdot 01874$	689	295	40	32	173840	12440	960
32	$\cdot 02363$	984	255	46	37	226664	9464	1104
37	$\cdot 03547$	1239	301	126	42	281904	10024	3024
42	$\cdot 04786$	1540	427	389	47	353016	10556	9336
47	$\cdot 06326$	1967	816	102	52	439688	31008	2448
52	$\cdot 08293$	2783	918	312	57	571752	41712	7288
57	$\cdot 11076$	3701	606	2296	62	776184	12496	55104
62	$\cdot 14777$	4307	2902	2105	67	1243320	149760	50520
67	$\cdot 19084$	7909	797	254	72	1533376	27816	6096
72	$\cdot 26293$	3006	1051	2734	77	1771064	85784	65616
77	$\cdot 34299$	9057	1682	4982	82	1529728	147032	119568
82	$\cdot 43856$	7374	3299	8184	87	2001624	262904	196416
87	$\cdot 50780$	10673	4365					
92	$\cdot 61403$	5788						
97	$\cdot 67191$							

TABLE B.

EXAMPLE OF OSCULATORY INTERPOLATION.

Age.	δ^3	δ^2	δ	$\log(q_x + \cdot 1)$.
17	504	744	62304	$\bar{1}\cdot 01178000$
18		1248	63048	$\cdot 01240304$
19		1752	64296	$\cdot 01303352$
20		2256	66048	$\cdot 01367648$
21			68304	$\cdot 01433696$
22	6456	2384	66256	$\cdot 01502000$
23		4072	63872	$\cdot 01568256$
24		10528	67944	$\cdot 01632128$
25		16984	78472	$\cdot 01700072$
26			95456	$\cdot 01778544$
27	528	13032	112792	$\cdot 01874000$
28		12504	125824	$\cdot 01986792$
29		11976	138328	$\cdot 02112616$
30		11448	150304	$\cdot 02250944$
31			161752	$\cdot 02401248$
32	960	12440	173840	$\cdot 02563000$
33		11480	186280	$\cdot 02736840$
34		10520	197760	$\cdot 02923120$
35		9560	208280	$\cdot 03120880$
36			217840	$\cdot 03329160$
37	1104	9464	226664	$\cdot 03547000$
38		10568	236128	$\cdot 03773664$
39		11672	246696	$\cdot 04009792$
40		12776	258368	$\cdot 04256488$
41			271144	$\cdot 04514856$
42	3024	10024	281904	$\cdot 04786000$
etc.	etc.	etc.	etc.	etc.

Section 4.—LAGRANGE'S METHOD OF INTERPOLATION.

The object of Lagrange's method of interpolation is to supply missing terms of a series when the given terms are not equidistant.

Let $u_a, u_b, u_c, \dots, u_n$ be the n given terms, and let it be assumed that the function is rational and integral and of the degree $(n-1)$. We may then assume that

$$\begin{aligned} u_x &= A(x-b)(x-c) \dots (x-n) \\ &+ B(x-a)(x-c) \dots (x-n) \\ &+ C(x-a)(x-b) \dots (x-n) \\ &+ \text{etc.} \end{aligned}$$

to n terms; each of the n terms in the right-hand member having $(n-1)$ of the factors $(x-a), (x-b), \dots$, and wanting one of these factors; and there being n of the co-efficients A, B, C, etc., the values of which have to be found. If the right-hand member were developed in powers of x , it is evident that it would be of the degree $(n-1)$, and that each power of x would have a constant co-efficient, thus fulfilling the hypothesis.

Making $x=a$, we have

$$u_a = A(a-b)(a-c) \dots (a-n).$$

Therefore

$$A = \frac{u_a}{(a-b)(a-c) \dots (a-n)}$$

Similarly, making $x=b$, we have

$$B = \frac{u_b}{(b-a)(b-c) \dots (b-n)},$$

and so on.

Hence finally,

$$u_x = u_a \frac{(x-b)(x-c) \dots (x-n)}{(a-b)(a-c) \dots (a-n)} + u_b \frac{(x-a)(x-c) \dots (x-n)}{(b-a)(b-c) \dots (b-n)} + \dots$$

$$\dots + u_n \frac{(x-a)(x-b)(x-c) \dots}{(n-a)(n-b)(n-c) \dots}$$

Any individual values of the function may be found approximately by means of this equation, but the process is a little tedious, and if many values were required the direct application of the formula would involve a great deal of labour. It is better in such case to calculate the values which will supply the leading differences, and then to complete the series by summation of differences.

For instance (see paragraph 22 of the report) in the case of English Life Table No. 7 at the young ages the values of q_x were available for ages 3, 4, 12, 17, and 18, supplying four orders of differences. The values for ages 5, 6, and 7 were therefore calculated by direct application of the formula; and then from the values at ages 3 to 7 inclusive the four orders of leading differences were obtained. In order that the values at ages 17 and 18 may be reproduced accurately, a considerable number of decimal places must be employed.

It may be noticed that as an efficient check on the work, the algebraical sum of the coefficients of u_a, u_b, \dots , etc. in calculating u_x must always be equal to unity. Also, when the leading differences have been formed, they can be checked by the formula

$$u_n = u_0 + n\delta + \frac{n(n-1)}{2}\delta_2 + \text{etc.}$$

KEY TO THE NOTATION.

m_x = the central death rate, being the ratio of deaths to population in the year of age x to $x+1$. The term "central death rate" is that in use amongst actuaries. In the Reports of the Registrar-General this function has been known by various names, such as the "rate of mortality," the "death rate," and the "mean annual death rate."

q_x = the rate of mortality, or the probability of dying in a year. It is the ratio of the number of deaths in the year of age x to $x+1$ to the number entering on the year.

p_x = the probability of living a year, or the ratio of the number completing the year of age x to $x+1$ to the number entering on the year.

${}_5p_x$ = the probability of living five years.

l_x = the number according to the life table surviving to exact age x .

d_x = the deaths in the year of age x to $x+1$ among l_x persons who enter on that year.

L_x = the population according to the life table, or the years of life lived, in the year of age x to $x+1$. This function in the Reports of the Registrar-General has been denoted by the symbol P_x .

T_x = the population, or the years of life lived, above the moment of age x . This function in the Reports of the Registrar-General has been denoted by the symbol Q_x .

e_x = the curtate expectation of life, or the number of years which on the average will be completed by persons aged exactly x .

e_x^o = the complete expectation of life, or the total future lifetime which on the average will be passed through by persons aged exactly x . This function in the Reports of the Registrar-General has been denoted by the symbol E_x .

On the expectations of life see paragraphs 26 and 27 of the Report.

N'_x = the sum of the column of l_x of the life table from age $x+1$ to the oldest age.

$N'_{x:5}$ = the sum of five values of the column l_x from age $x+1$ to age $x+5$ inclusive.

The accent is added to the symbol N above in order to distinguish the functions from the corresponding functions which involve the rate of interest.

N.B.—It will be observed from the above Key that the notation used in this Report departs in some respects from that formerly used in the Reports of the Registrar-General. The reason is that the notation of the Registrar-General differed from that which had been employed by actuaries for very many years, and that the actuaries' notation has been adopted at various International Congresses as the universal notation to be employed throughout the civilized world.

Table I.—ENGLISH LIFE TABLE No. 7.—MALES.

Table with columns: AGE. x, l_x, d_x, p_x, q_x, L_x, T_x, e_x, AGE. x. Rows range from age 0 to 99.

Table I.—English Life Table No. 7.—Males—cont.

Table with columns: AGE. x, l_x, d_x, p_x, q_x, L_x, T_x, e_x, AGE. x. Rows range from age 60 to 100.

Table II.—ENGLISH LIFE TABLE No. 7.—FEMALES.

AGE. <i>x</i>	<i>l_x</i>	<i>d_x</i>	<i>p_x</i>	<i>q_x</i>	<i>L_x</i>	<i>T_x</i>	<i>e_x</i>	AGE. <i>x</i>
0	1000000	117435	.8825654	.1174346	916277	52381962	52.38	0
1	882565	33222	.9623575	.0376425	865954	51465685	58.31	1
2	849343	12965	.9847351	.0152649	842861	50599731	59.58	2
3	836378	8405	.9899502	.0100498	832175	49756870	59.49	3
4	827973	6191	.9925226	.0074774	824878	48924695	59.09	4
5	821782	4549	.9944661	.0055339	819507	48099817	58.53	5
6	817233	3364	.9958826	.0041174	815551	47280310	57.85	6
7	813869	2551	.9968654	.0031346	812593	46464759	57.09	7
8	811318	2029	.9974991	.0025009	810303	45652166	56.27	8
9	809289	1733	.9978594	.0021406	808423	44841863	55.41	9
10	807556	1604	.9980133	.0019867	806754	44033440	54.53	10
1	805952	1597	.9980191	.0019809	805153	43226686	53.64	1
2	804355	1668	.9979265	.0020735	803521	42421533	52.74	2
3	802687	1785	.9977762	.0022238	801795	41618012	51.85	3
4	800902	1922	.9976003	.0023997	799941	40816217	50.96	4
15	798980	2060	.9974221	.0025779	797950	40016276	50.08	15
6	796920	2186	.9972563	.0027437	795827	39218326	49.21	6
7	794734	2298	.9971088	.0028912	793585	38422499	48.35	7
8	792436	2396	.9969766	.0030234	791238	37628914	47.49	8
9	790040	2482	.9968581	.0031419	788799	36837676	46.63	9
20	787558	2563	.9967462	.0032538	786276	36048877	45.77	20
1	784995	2643	.9966334	.0033666	783674	35262601	44.92	1
2	782352	2729	.9965120	.0034880	780987	34478927	44.07	2
3	779623	2815	.9963887	.0036113	778216	33697940	43.22	3
4	776808	2899	.9962685	.0037315	775358	32919724	42.38	4
25	773909	2986	.9961414	.0038586	772416	32144366	41.54	25
6	770923	3086	.9959978	.0040022	769380	31371950	40.69	6
7	767837	3203	.9958280	.0041720	766236	30602570	39.86	7
8	764634	3344	.9956271	.0043729	762962	29836334	39.02	8
9	761290	3501	.9954014	.0045986	759539	29073372	38.19	9
30	757789	3669	.9951578	.0048422	755955	28313833	37.36	30
1	754120	3844	.9949031	.0050969	752198	27557878	36.54	1
2	750276	4018	.9946442	.0053558	748267	26800560	35.73	2
3	746258	4194	.9943807	.0056193	744161	26057413	34.92	3
4	742064	4372	.9941079	.0058921	739878	25313252	34.11	4
35	737692	4555	.9938264	.0061736	735414	24573374	33.31	35
6	733137	4739	.9935363	.0064637	730768	23837960	32.52	6
7	728398	4925	.9932384	.0067616	725935	23107192	31.72	7
8	723473	5107	.9929413	.0070587	720920	22381257	30.94	8
9	718366	5284	.9926448	.0073552	715724	21660337	30.15	9
40	713082	5465	.9923354	.0076646	710349	20944613	29.37	40
1	707617	5661	.9919996	.0080004	704787	20234264	28.59	1
2	701956	5880	.9916237	.0083763	699016	19529477	27.82	2
3	696076	6117	.9912121	.0087879	693017	18830461	27.05	3
4	689959	6366	.9907737	.0092263	686776	18137444	26.29	4
45	683593	6631	.9903006	.0096994	680278	17450668	25.53	45
6	676962	6915	.9897847	.0102153	673504	16770390	24.77	6
7	670047	7225	.9892180	.0107820	666435	16096886	24.02	7
8	662822	7540	.9886239	.0113761	659052	15430451	23.28	8
9	655282	7858	.9880071	.0119929	651353	14771399	22.54	9
50	647424	8204	.9873306	.0126694	643322	14120046	21.81	50
1	639220	8593	.9865560	.0134440	634923	13476724	21.08	1
2	630627	9053	.9856444	.0143556	626101	12841801	20.36	2
3	621574	9593	.9845682	.0154318	616777	12215700	19.65	3
4	611981	10190	.9833485	.0166515	606886	11598923	18.95	4
55	601791	10822	.9820177	.0179823	596380	10992037	18.27	55
6	590969	11459	.9806097	.0193903	585240	10395657	17.59	6
7	579510	12077	.9791599	.0208401	573471	9810417	16.93	7
8	567433	12655	.9776973	.0223027	561106	9236946	16.28	8
9	554778	13206	.9761965	.0238035	548175	8675840	15.64	9

Table II.—English Life Table No. 7.—Females—cont.

AGE. <i>x</i>	<i>l_x</i>	<i>d_x</i>	<i>p_x</i>	<i>q_x</i>	<i>L_x</i>	<i>T_x</i>	<i>e_x</i>	AGE. <i>x</i>
60	541572	13751	.9746095	.0253905	534696	8127665	15.01	60
1	527821	14311	.9728858	.0271142	520666	7592969	14.39	1
2	513510	14907	.9709717	.0290283	506056	7072303	13.77	2
3	498603	15466	.9689792	.0310208	490870	6566247	13.17	3
4	483137	15974	.9669387	.0330613	475150	6075377	12.58	4
65	467163	16507	.9646639	.0353361	458910	5600227	11.99	65
6	450656	17146	.9619551	.0380449	442083	5141317	11.41	6
7	433510	17949	.9585945	.0414055	424535	4699234	10.84	7
8	415561	18975	.9543388	.0456612	406074	4274699	10.29	8
9	396586	20127	.9492504	.0507496	386522	3868625	9.76	9
70	376459	21243	.9435715	.0564285	365838	3482103	9.25	70
1	355216	22172	.9375823	.0624177	344130	3116265	8.77	1
2	333044	22777	.9316083	.0683917	321655	2772135	8.32	2
3	310267	23039	.9257445	.0742555	298748	2450480	7.90	3
4	287228	23044	.9197716	.0802284	275706	2151732	7.49	4
75	264184	22834	.9135692	.0864308	252767	1876026	7.10	75
6	241350	22445	.9070004	.0929996	230127	1623259	6.73	6
7	218905	21911	.8999094	.1000906	207950	1393132	6.36	7
8	196994	21211	.8923242	.1076758	186388	1185182	6.02	8
9	175783	20338	.8843037	.1156963	165614	998794	5.68	9
80	155445	19320	.8757094	.1242906	145785	833180	5.36	80
1	136125	18189	.8663829	.1336171	127031	687395	5.05	1
2	117936	16966	.8561417	.1438583	109453	560364	4.75	2
3	100970	15687	.8443320	.1553680	93126	450911	4.47	3
4	85283	14345	.8318061	.1681939	78111	357785	4.20	4
85	70938	12913	.8179674	.1820326	64481	279674	3.94	85
6	58025	11402	.8034946	.1965054	52324	215193	3.71	6
7	46623	9844	.7888546	.2111454	41701	162869	3.49	7
8	36779	8317	.7738715	.2261285	32621	121168	3.30	8
9	28462	6882	.7582049	.2417951	25021	88547	3.11	9
90	21580	5563	.7421932	.2578068	18798	63526	2.94	90
1	16017	4385	.7262414	.2737586	13825	44728	2.79	1
2	11632	3364	.7108224	.2891776	9950	30903	2.66	2
3	8268	2512	.6961691	.3038309	7012	20953	2.53	3
4	5756	1829	.6823001	.3176999	4841	13941	2.42	4
95	3927	1299	.6690405	.3309595	3278	9100	2.32	95
6	2628	904	.6560401	.3439599	2176	5822	2.22	6
7	1724	616	.6427910	.3572090	1416	3646	2.12	7
8	1108	411	.6286470	.3713530	902	2230	2.01	8
9	697	270	.6128485	.3871515	562	1328	1.91	9
100	427	173	.5945607	.4054393	341	766	1.80	100
1	254	109	.5729269	.4270731	199	425	1.68	1
2	145	65	.5471430	.4528570	113	226	1.56	2
3	80	39	.5165540	.4834460	60	113	1.44	3
4	41	21	.4807661	.5192339	31	53	1.32	4
105	20	11	.4397653	.5602347	14	22	1.20	105
6	9	6	.3940204	.6059796	6	8	1.08	6
7	3	2	.3445435	.6554565	2	2	.98	7
8	1	1	.2928802	.7071198	1	1	.88	8
9	0	0	.2410043	.7589957	0	0	.81	9

Table III.—ENGLISH LIFE TABLE No. 8.—MALES.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
0	1000000	120441	.8795586	.1204414	911428	51495315	51.50	0
1	879559	30115	.9657618	.0342382	864501	50583887	57.51	1
2	849444	11353	.9866350	.0133650	843768	49719386	58.53	2
3	838091	6856	.9918190	.0081810	834663	48875618	58.32	3
4	831235	4959	.9940345	.0059655	828755	48040955	57.80	4
5	826276	4038	.9951125	.0048875	824257	47212200	57.14	5
6	822238	3262	.9960331	.0039669	820607	46387943	56.42	6
7	818976	2630	.9967889	.0032111	817661	45567336	55.64	7
8	816346	2141	.9973774	.0026226	815276	44749675	54.82	8
9	814205	1791	.9978011	.0021989	813309	43934399	53.96	9
10	812414	1570	.9980677	.0019323	811629	43121090	53.08	10
1	810844	1468	.9981895	.0018105	810110	42309461	52.18	1
2	809376	1469	.9981841	.0018159	808642	41499351	51.27	2
3	807907	1556	.9980739	.0019261	807129	40690709	50.37	3
4	806351	1705	.9978863	.0021137	805498	39883580	49.46	4
15	804646	1888	.9976538	.0023462	803702	39078082	48.57	15
6	802758	2077	.9974132	.0025868	801720	38274380	47.68	6
7	800681	2236	.9972077	.0027923	799563	37472660	46.80	7
8	798445	2414	.9969754	.0030246	797238	36673097	45.93	8
9	796031	2596	.9967383	.0032617	794733	35875859	45.07	9
20	793435	2762	.9965187	.0034813	792054	35081126	44.21	20
1	790673	2895	.9963390	.0036610	789225	34289072	43.37	1
2	787778	2980	.9962169	.0037831	786288	33499847	42.53	2
3	784798	3031	.9961378	.0038622	783283	32713559	41.68	3
4	781767	3068	.9960754	.0039246	780233	31930276	40.84	4
25	778699	3112	.9960032	.0039968	777143	31150043	40.00	25
6	775587	3184	.9958949	.0041051	773995	30372900	39.16	6
7	772403	3280	.9957532	.0042468	770763	29598905	38.32	7
8	769123	3388	.9955956	.0044044	767429	28828142	37.48	8
9	765735	3508	.9954178	.0045822	763981	28060713	36.65	9
30	762227	3647	.9952151	.0047849	760403	27296732	35.81	30
1	758580	3806	.9949831	.0050169	756677	26536329	34.98	1
2	754774	3987	.9947172	.0052828	752781	25779652	34.16	2
3	750787	4190	.9944198	.0055802	748692	25026871	33.33	3
4	746597	4406	.9940977	.0059023	744394	24278179	32.52	4
35	742191	4653	.9937574	.0062426	739874	23533785	31.71	35
6	737558	4864	.9934056	.0065944	735126	22793911	30.90	6
7	732694	5091	.9930513	.0069487	730149	22058785	30.11	7
8	727603	5319	.9926898	.0073102	724943	21328636	29.31	8
9	722284	5557	.9923075	.0076925	719506	20603693	28.53	9
40	716727	5813	.9918900	.0081100	713820	19884187	27.74	40
1	710914	6097	.9914231	.0085769	707866	19170367	26.97	1
2	704817	6408	.9909086	.0090914	701613	18462501	26.20	2
3	698409	6736	.9903554	.0096446	695041	17760888	25.43	3
4	691673	7083	.9897591	.0102409	688131	17065847	24.67	4
45	684590	7452	.9891149	.0108851	680864	16377716	23.92	45
6	677138	7842	.9884185	.0115815	673217	15696852	23.18	6
7	669296	8242	.9876859	.0123141	665175	15023635	22.45	7
8	661054	8647	.9869192	.0130808	656731	14358460	21.72	8
9	652407	9074	.9860915	.0139085	647870	13701729	21.00	9
50	643333	9537	.9851752	.0148248	638564	13053859	20.29	50
1	633796	10051	.9841417	.0158583	628771	12415295	19.59	1
2	623745	10610	.9829900	.0170100	618440	11786524	18.90	2
3	613135	11199	.9817349	.0182651	607535	11168084	18.22	3
4	601936	11816	.9803700	.0196300	596028	10560549	17.55	4
55	590120	12458	.9788889	.0211111	583891	9964521	16.89	55
6	577662	13122	.9772843	.0227157	571101	9380630	16.24	6
7	564540	13798	.9755596	.0244404	557641	8809529	15.61	7
8	550742	14477	.9737127	.0262873	543504	8251888	14.98	8
9	536265	15162	.9717267	.0282733	528684	7708384	14.37	9

Table III.—English Life Table No. 8.—Males—cont.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
60	521103	15850	.9695835	.0304165	513178	7179700	13.78	60
1	505253	16540	.9672635	.0327365	496983	6665522	13.19	1
2	488713	17206	.9647940	.0352060	480110	6169539	12.62	2
3	471507	17834	.9621769	.0378231	462590	5689429	12.07	3
4	453673	18441	.9593505	.0406495	444452	5226839	11.52	4
65	435232	19043	.9562477	.0437523	425711	4782387	10.99	65
6	416189	19646	.9527954	.0472046	406366	4356676	10.47	6
7	396543	20232	.9489792	.0510208	386427	3950310	9.96	7
8	376311	20766	.9448156	.0551844	365928	3563883	9.47	8
9	355545	21237	.9402699	.0597301	344926	3197955	9.00	9
70	334308	21629	.9353033	.0646967	323494	2853029	8.53	70
1	312679	21927	.9298722	.0701278	301715	2529535	8.09	1
2	290752	22134	.9238740	.0761260	279685	2227820	7.66	2
3	268618	22223	.9172708	.0827292	257507	1948135	7.25	3
4	246395	22146	.9101198	.0898802	235322	1690628	6.86	4
75	224249	21866	.9024896	.0975104	213316	1455306	6.49	75
6	202383	21359	.8944632	.1055368	191703	1241990	6.14	6
7	181024	20647	.8859412	.1140588	170701	1050287	5.80	7
8	160377	19758	.8768040	.1231960	150498	879586	5.49	8
9	140619	18684	.8671277	.1328723	131277	729088	5.19	9
80	121935	17436	.8570061	.1429939	113217	597811	4.90	80
1	104499	16035	.8465532	.1534468	96481	484594	4.64	1
2	88464	14526	.8358072	.1641928	81201	388113	4.39	2
3	73938	12963	.8246708	.1753292	67457	306912	4.15	3
4	60975	11397	.8130619	.1869381	55276	239455	3.93	4
85	49578	9873	.8008864	.1991136	44642	184179	3.72	85
6	39705	8416	.7880358	.2119632	35497	139537	3.51	6
7	31289	7079	.7737433	.2262567	27749	104040	3.33	7
8	24210	5861	.7579161	.2420839	21280	76291	3.15	8
9	18349	4741	.7415991	.2584009	15978	55011	3.00	9
90	13608	3728	.7260488	.2739512	11744	39033	2.87	90
1	9880	2838	.7127280	.2872720	8461	27289	2.76	1
2	7042	2097	.7022923	.2977077	5994	18828	2.67	2
3	4945	1510	.6946787	.3053213	4190	12834	2.60	3
4	3435	1067	.6891593	.3108407	2901	8644	2.52	4
95	2368	748	.6843579	.3156421	1994	5743	2.43	95
6	1620	521	.6782587	.3217413	1360	3749	2.32	6
7	1099	365	.6682471	.3317529	916	2389	2.18	7
8	734	256	.6512558	.3487442	606	1473	2.01	8
9	478	180	.6240841	.3759159	388	867	1.82	9
100	298	124	.5839522	.4160478	236	479	1.61	100
1	174	82	.5292748	.4707252	133	243	1.40	1
2	92	50	.4605145	.5394855	67	110	1.20	2
3	42	26	.3808145	.6191855	29	43	1.02	3
4	16	11	.2960075	.7039925	11	14	.87	4
105	5	4	.2136899	.7863101	3	3	.75	105
6	1	1	.1414135	.8585865			.65	6

Table IV.—ENGLISH LIFE TABLE No. 8.—FEMALES.

AGE. x	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. x
0	1000000	97670	.9023303	.0976697	930368	55347553	55.35	0
1	902330	28808	.9680731	.0319269	887926	54417185	60.31	1
2	873522	11546	.9867825	.0132175	867749	53529259	61.28	2
3	861976	6913	.9919795	.0080205	858519	52661510	61.09	3
4	855063	5008	.9941438	.0058562	852559	51802991	60.58	4
5	850055	4079	.9952011	.0047989	848016	50950432	59.94	5
6	845976	3298	.9961014	.0038986	844327	50102416	59.22	6
7	842678	2667	.9968357	.0031643	841344	49258089	58.46	7
8	840011	2183	.9974006	.0025994	838920	48416745	57.64	8
9	837828	1845	.9977991	.0022009	836905	47577825	56.79	9
10	835983	1638	.9980401	.0019599	835164	46740920	55.91	10
1	834345	1554	.9981383	.0018617	833568	45905756	55.02	1
2	832791	1569	.9981147	.0018853	832007	45072188	54.12	2
3	831222	1666	.9979963	.0020037	830389	44240181	53.22	3
4	829556	1812	.9978158	.0021842	828650	43409792	52.33	4
15	827744	1976	.9976122	.0023878	826756	42581142	51.44	15
6	825768	2122	.9974300	.0025700	824707	41754386	50.56	6
7	823646	2207	.9973208	.0026792	822542	40929679	49.69	7
8	821439	2280	.9972250	.0027750	820299	40107137	48.83	8
9	819159	2345	.9971370	.0028630	817987	39286838	47.96	9
20	816814	2409	.9970508	.0029492	815609	38468851	47.10	20
1	814405	2475	.9969606	.0030394	813168	37653242	46.23	1
2	811930	2541	.9968713	.0031287	810659	36840074	45.37	2
3	809389	2600	.9967869	.0032131	808089	36029415	44.51	3
4	806789	2663	.9966999	.0033001	805458	35221326	43.66	4
25	804126	2731	.9966029	.0033971	802760	34415868	42.80	25
6	801395	2815	.9964883	.0035117	799988	33613108	41.94	6
7	798580	2908	.9963574	.0036426	797126	32813120	41.09	7
8	795672	3012	.9962150	.0037850	794166	32015994	40.24	8
9	792660	3124	.9960593	.0039407	791098	31221828	39.39	9
30	789536	3246	.9958884	.0041116	787913	30430730	38.54	30
1	786290	3381	.9957005	.0042995	784599	29642817	37.70	1
2	782909	3528	.9954931	.0045069	781145	28858218	36.86	2
3	779381	3689	.9952674	.0047326	777537	28077073	36.03	3
4	775692	3857	.9950267	.0049733	773763	27299536	35.19	4
35	771835	4034	.9947745	.0052255	769818	26525773	34.37	35
6	767801	4211	.9945142	.0054858	765696	25755955	33.55	6
7	763590	4390	.9942515	.0057485	761395	24990259	32.73	7
8	759200	4567	.9939842	.0060158	756916	24228864	31.91	8
9	754633	4752	.9937033	.0062967	752257	23471948	31.10	9
40	749881	4949	.9934000	.0066000	747407	22719691	30.30	40
1	744932	5166	.9930650	.0069350	742349	21972284	29.50	1
2	739766	5398	.9927033	.0072967	737067	21229935	28.70	2
3	734368	5639	.9923208	.0076792	731548	20492868	27.91	3
4	728729	5896	.9919090	.0080910	725781	19761320	27.12	4
45	722833	6173	.9914598	.0085402	719747	19035539	26.34	45
6	716660	6476	.9909645	.0090355	713422	18315792	25.56	6
7	710184	6792	.9904365	.0095635	706788	17602370	24.79	7
8	703392	7118	.9898807	.0101193	699833	16895582	24.02	8
9	696274	7466	.9892758	.0107242	692541	16195749	23.26	9
50	688808	7853	.9885993	.0114007	684881	15503208	22.51	50
1	680955	8288	.9878288	.0121712	676811	14818327	21.76	1
2	672667	8770	.9869622	.0130378	668282	14141516	21.02	2
3	663897	9287	.9860117	.0139883	659254	13473234	20.29	3
4	654610	9835	.9849757	.0150243	649692	12813980	19.58	4
55	644775	10412	.9838523	.0161477	639569	12164288	18.87	55
6	634363	11013	.9826390	.0173610	628857	11524719	18.17	6
7	623350	11625	.9813505	.0186495	617537	10895862	17.48	7
8	611725	12244	.9799843	.0200157	605603	10278325	16.80	8
9	599481	12882	.9785119	.0214881	593040	9672722	16.14	9

Table IV.—English Life Table No. 8.—Females—cont.

AGE. x	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. x
60	586599	13548	.9769037	.0230963	579825	9079682	15.48	60
1	573051	14253	.9751277	.0248723	565925	8499857	14.83	1
2	558798	14954	.9732403	.0267597	551321	7933932	14.20	2
3	543844	15632	.9712555	.0287445	536028	7382611	13.58	3
4	528212	16336	.9690726	.0309274	520044	6846583	12.96	4
65	511876	17106	.9665831	.0334169	503323	6326539	12.36	65
6	494770	17975	.9636697	.0363303	485782	5823216	11.77	6
7	476795	18952	.9602511	.0397489	467319	5337434	11.19	7
8	457843	19978	.9563638	.0436362	447854	4870115	10.64	8
9	437865	20990	.9520626	.0479374	427370	4422261	10.10	9
70	416875	21924	.9474084	.0525916	405913	3994891	9.58	70
1	394951	22722	.9424709	.0575291	383590	3588978	9.09	1
2	372229	23352	.9372625	.0627375	360553	3205388	8.61	2
3	348877	23829	.9316998	.0683002	336963	2844835	8.15	3
4	325048	24148	.9257096	.0742904	312974	2507872	7.72	4
75	300900	24310	.9192095	.0807905	288745	2194898	7.29	75
6	276590	24310	.9121061	.0878939	264435	1906153	6.89	6
7	252280	24185	.9041354	.0958646	240187	1641718	6.51	7
8	228095	23893	.8952495	.1047505	216149	1401531	6.14	8
9	204202	23339	.8857051	.1142949	192532	1185382	5.81	9
80	180863	22461	.8758134	.1241866	169633	992850	5.49	80
1	158402	21234	.8659487	.1340513	147785	823217	5.20	1
2	137168	19707	.8563268	.1436732	127314	675432	4.92	2
3	117461	18003	.8467374	.1532626	108460	548118	4.67	3
4	99458	16218	.8369346	.1630654	91349	439658	4.42	4
85	83240	14430	.8266345	.1733655	76025	348309	4.19	85
6	68810	12696	.8154963	.1845037	62462	272284	3.96	6
7	56114	11040	.8032726	.1967274	50594	209822	3.74	7
8	45074	9462	.7900803	.2099197	40343	159228	3.53	8
9	35612	7971	.7761460	.2238540	31626	118885	3.34	9
90	27641	6586	.7617445	.2382555	24348	87259	3.16	90
1	21055	5322	.7472045	.2527955	18394	62911	2.99	1
2	15733	4206	.7326566	.2673434	13630	44517	2.83	2
3	11527	3250	.7180512	.2819488	9902	30887	2.68	3
4	8277	2457	.7031753	.2968247	7049	20985	2.54	4
95	5820	1818	.6876691	.3123309	4911	13936	2.39	95
6	4002	1317	.6710510	.3289490	3343	9025	2.26	6
7	2685	932	.6527389	.3472611	2219	5682	2.12	7
8	1753	645	.6320844	.3679156	1431	3463	1.98	8
9	1108	434	.6084189	.3915811	891	2032	1.83	9
100	674	282	.5811105	.4188895	533	1141	1.69	100
1	392	177	.5496368	.4503632	303	608	1.55	1
2	215	104	.5136685	.4863315	163	305	1.42	2
3	111	59	.4731568	.5268432	82	142	1.29	3
4	52	30	.4284139	.5715861	37	60	1.16	4
105	22	13	.3801683	.6198317	15	23	1.05	105
6	9	6	.3295763	.6704237	6	8	.95	6
7	3	2	.2781720	.7218280	2	2	.85	7
8	1	1	.2277481	.7722519	—	—	.77	8

Table V.—LIFE TABLE FOR ENGLAND AND WALES.—
UNMARRIED FEMALES (SPINSTERS).

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
15	102783	246	·99760	·00240	102660	5369727	52·25	15
6	102537	262	·99744	·00256	102406	5267067	51·37	6
7	102275	270	·99736	·00264	102140	5164661	50·50	7
8	102005	275	·99730	·00270	101867	5062521	49·64	8
9	101730	278	·99726	·00274	101591	4960654	48·76	9
20	101452	282	·99722	·00278	101311	4859063	47·89	20
1	101170	287	·99717	·00283	101027	4757752	47·02	1
2	100883	289	·99712	·00288	100738	4656725	46·16	2
3	100594	294	·99707	·00293	100447	4555987	45·29	3
4	100300	300	·99702	·00298	100150	4455540	44·42	4
25	100000	306	·99694	·00306	99847	4355390	43·55	25
6	99694	316	·99683	·00317	99536	4255543	42·69	6
7	99378	329	·99668	·00332	99214	4156007	41·82	7
8	99049	348	·99649	·00351	98875	4056793	40·95	8
9	98701	368	·99627	·00373	98517	3957918	40·11	9
30	98333	386	·99606	·00394	98140	3859401	39·25	30
1	97947	405	·99586	·00414	97744	3761261	38·40	1
2	97542	422	·99568	·00432	97331	3663517	37·57	2
3	97120	435	·99551	·00449	96903	3566186	36·72	3
4	96685	451	·99534	·00466	96459	3469283	35·88	4
35	96234	466	·99516	·00484	96001	3372824	35·05	35
6	95768	484	·99495	·00505	95526	3276823	34·22	6
7	95284	501	·99473	·00527	95034	3181297	33·39	7
8	94783	520	·99451	·00549	94523	3086263	32·56	8
9	94263	541	·99427	·00573	93992	2991740	31·75	9
40	93722	564	·99398	·00602	93440	2897748	30·92	40
1	93158	594	·99362	·00638	92861	2804308	30·10	1
2	92564	633	·99317	·00683	92248	2711447	29·29	2
3	91931	675	·99265	·00735	91593	2619199	28·48	3
4	91256	722	·99209	·00791	90895	2527606	27·70	4
45	90534	768	·99150	·00850	90150	2436711	26·92	45
6	89766	817	·99092	·00908	89358	2346561	26·15	6
7	88949	858	·99036	·00964	88520	2257203	25·37	7
8	88091	898	·98980	·01020	87642	2168683	24·63	8
9	87193	941	·98922	·01078	86722	2081041	23·87	9
50	86252	981	·98861	·01139	85762	1994319	23·12	50
1	85271	1029	·98794	·01206	84756	1908557	22·39	1
2	84242	1073	·98725	·01275	83706	1823801	21·65	2
3	83169	1121	·98654	·01346	82608	1740095	20·92	3
4	82048	1166	·98578	·01422	81465	1657487	20·19	4
55	80882	1220	·98491	·01509	80272	1576022	19·48	55
6	79662	1283	·98389	·01611	79021	1495750	18·78	6
7	78379	1354	·98272	·01728	77702	1416729	18·08	7
8	77025	1432	·98142	·01858	76309	1339027	17·39	8
9	75593	1513	·97998	·02002	74836	1262718	16·71	9
60	74080	1598	·97842	·02158	73281	1187882	16·04	60
1	72482	1687	·97672	·02328	71639	1114601	15·39	1
2	70795	1776	·97492	·02508	69907	1042962	14·73	2
3	69019	1864	·97300	·02700	68087	973055	14·10	3
4	67155	1953	·97092	·02908	66178	904968	13·47	4
65	65202	2048	·96860	·03140	64178	838790	12·86	65
6	63154	2147	·96599	·03401	62081	774612	12·27	6
7	61007	2254	·96308	·03692	59880	712531	11·68	7
8	58753	2355	·95991	·04009	57575	652651	11·11	8
9	56398	2459	·95641	·04359	55169	595076	10·55	9

Table V.—Life Table for England and Wales.—Unmarried Females
(Spinsters)—*cont.*

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
70	53939	2561	·95254	·04746	52658	539907	10·01	70
1	51378	2660	·94822	·05178	50048	487249	9·48	1
2	48718	2756	·94344	·05656	47340	437201	8·97	2
3	45962	2841	·93819	·06181	44542	389861	8·48	3
4	43121	2914	·93242	·06758	41664	345319	8·01	4
75	40207	2973	·92606	·07394	38720	303655	7·55	75
6	37234	3014	·91905	·08095	35727	264935	7·12	6
7	34220	3040	·91115	·08885	32700	229208	6·70	7
8	31180	3047	·90229	·09771	29657	196508	6·30	8
9	28133	3020	·89265	·10735	26623	166851	5·93	9
80	25113	2951	·88249	·11751	23637	140228	5·58	80
1	22162	2835	·87209	·12791	20745	116591	5·26	1
2	19327	2677	·86147	·13853	17988	95846	4·96	2
3	16650	2491	·85039	·14961	15405	77858	4·68	3
4	14159	2282	·83885	·16115	13018	62453	4·41	4
85	11877	2056	·82687	·17313	10849	49435	4·16	85
6	9821	1822	·81445	·18555	8910	38586	3·93	6
7	7999	1588	·80153	·19847	7205	29676	3·71	7
8	6411	1359	·78807	·21193	5731	22471	3·51	8
9	5052	1141	·77414	·22586	4482	16740	3·31	9
90	3911	939	·75985	·24015	3441	12258	3·13	90
1	2972	757	·74532	·25468	2594	8817	2·97	1
2	2215	597	·73058	·26942	1916	6223	2·81	2
3	1618	460	·71563	·28437	1388	4307	2·66	3
4	1158	347	·70044	·29956	985	2919	2·52	4
95	811	255	·68487	·31513	683	1934	2·38	95
6	556	184	·66882	·33118	464	1251	2·25	6
7	372	130	·65185	·34815	307	787	2·12	7
8	242	89	·63315	·36685	198	480	1·98	8
9	153	59	·61135	·38865	123	282	1·84	9
100	94	39	·58468	·41532	75	159	1·69	100
1	55	25	·55126	·44874	42	84	1·54	1
2	30	15	·50945	·49055	23	42	1·38	2
3	15	8	·45831	·54169	11	19	1·22	3
4	7	4	·39819	·60181	5	8	1·07	4
105	3	2	·33111	·66889	2	3	·94	105
6	1	1	·26086	·73914	1	1	·82	6
7	0	0	·19255	·80745	0	0	·72	7

Table VI.—LIFE TABLE FOR ENGLAND AND WALES.—
MARRIED FEMALES (WIVES).

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
25	100000	377	·99624	·00376	99811	4326850	43·27	25
6	99623	380	·99618	·00382	99433	4227039	42·42	6
7	99243	385	·99611	·00389	99051	4127606	41·59	7
8	98858	393	·99603	·00397	98661	4028555	40·76	8
9	98465	401	·99593	·00407	98265	3929894	39·91	9
30	98064	410	·99581	·00419	97859	3831629	39·08	30
1	97654	424	·99565	·00435	97442	3733770	38·24	1
2	97230	442	·99546	·00454	97009	3636328	37·40	2
3	96788	463	·99523	·00477	96556	3539319	36·57	3
4	96325	484	·99497	·00503	96083	3442763	35·74	4
35	95841	507	·99471	·00529	95588	3346680	34·91	35
6	95334	529	·99444	·00556	95069	3251092	34·10	6
7	94805	553	·99417	·00583	94529	3156023	33·29	7
8	94252	576	·99390	·00610	93964	3061494	32·48	8
9	93676	597	·99362	·00638	93377	2967530	31·68	9
40	93079	622	·99333	·00667	92768	2874153	30·88	40
1	92457	645	·99302	·00698	92135	2781385	30·09	1
2	91812	668	·99272	·00728	91478	2689250	29·29	2
3	91144	690	·99242	·00758	90799	2597772	28·50	3
4	90454	713	·99210	·00790	90097	2506973	27·72	4
45	89741	741	·99175	·00825	89371	2416876	26·93	45
6	89000	771	·99133	·00867	88614	2327505	26·15	6
7	88229	807	·99086	·00914	87826	2238891	25·38	7
8	87422	844	·99036	·00964	87000	2151065	24·61	8
9	86578	882	·98981	·01019	86137	2064065	23·84	9
50	85696	928	·98917	·01083	85232	1977928	23·08	50
1	84768	980	·98844	·01156	84278	1892696	22·33	1
2	83788	1040	·98759	·01241	83268	1808418	21·58	2
3	82748	1105	·98665	·01335	82195	1725150	20·85	3
4	81643	1174	·98561	·01439	81056	1642955	20·12	4
55	80469	1246	·98451	·01549	79846	1561899	19·41	55
6	79223	1317	·98337	·01663	78565	1482053	18·71	6
7	77906	1385	·98222	·01778	77213	1403488	18·01	7
8	76521	1450	·98104	·01896	75796	1326275	17·33	8
9	75071	1518	·97979	·02021	74312	1250479	16·66	9
60	73553	1590	·97838	·02162	72758	1176167	15·99	60
1	71963	1672	·97676	·02324	71127	1103409	15·33	1
2	70291	1763	·97493	·02507	69410	1032282	14·69	2
3	68528	1855	·97293	·02707	67600	962872	14·05	3
4	66673	1951	·97073	·02927	65698	895272	13·43	4
65	64722	2053	·96828	·03172	63695	829574	12·82	65
6	62669	2160	·96555	·03445	61589	765879	12·22	6
7	60509	2268	·96253	·03747	59375	704290	11·64	7
8	58241	2375	·95922	·04078	57054	644915	11·07	8
9	55866	2481	·95559	·04441	54625	587861	10·52	9
70	53385	2583	·95161	·04839	52094	533236	9·99	70
1	50802	2679	·94726	·05274	49462	481142	9·47	1
2	48123	2766	·94252	·05748	46740	431680	8·97	2
3	45357	2841	·93737	·06263	43937	384940	8·49	3
4	42516	2902	·93175	·06825	41065	341003	8·02	4
75	39614	2948	·92558	·07442	38140	299938	7·57	75
6	36666	2978	·91880	·08120	35177	261798	7·14	6
7	33688	2991	·91121	·08879	32192	226621	6·73	7
8	30697	2984	·90278	·09722	29205	194429	6·33	8
9	27713	2948	·89361	·10639	26239	165224	5·96	9

Table VI.—Life Table for England and Wales.—Married Females
(Wives)—cont.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
80	24765	2877	·88385	·11615	23327	138985	5·61	80
1	21888	2764	·87369	·12631	20506	115658	5·28	1
2	19124	2620	·86302	·13698	17814	95152	4·98	2
3	16504	2449	·85163	·14837	15279	77338	4·69	3
4	14055	2254	·83964	·16036	12928	62059	4·42	4
85	11801	2039	·82720	·17280	10782	49131	4·16	85
6	9762	1811	·81445	·18555	8856	38349	3·93	6
7	7951	1580	·80139	·19861	7161	29493	3·71	7
8	6371	1351	·78791	·21209	5696	22332	3·51	8
9	5020	1134	·77403	·22597	4453	16636	3·31	9
90	3886	933	·75982	·24018	3419	12183	3·14	90
1	2953	752	·74532	·25468	2577	8764	2·97	1
2	2201	593	·73055	·26945	1905	6187	2·81	2
3	1608	458	·71553	·28447	1379	4282	2·66	3
4	1150	345	·70025	·29975	977	2903	2·52	4
95	805	253	·68468	·31532	679	1926	2·39	95
6	552	183	·66882	·33118	460	1247	2·26	6
7	369	128	·65236	·34764	305	787	2·13	7
8	241	88	·63464	·36536	197	482	2·00	8
9	153	59	·61440	·38560	124	285	1·87	9
100	94	39	·58993	·41007	74	161	1·72	100
1	55	24	·55932	·44068	43	87	1·57	1
2	31	15	·52076	·47924	24	44	1·42	2
3	16	8	·47302	·52698	12	20	1·26	3
4	8	5	·41596	·58404	5	8	1·11	4
105	3	2	·35103	·64897	2	3	·97	105
6	1	1	·28152	·71848	1	1	·85	6
7	0	0	·21222	·78778	0	0	·75	7

Table VII.—LIFE TABLE FOR ENGLAND AND WALES.—
WIDOWED FEMALES (WIDOWS).

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	${}^o e_x$	AGE. <i>x</i>
25	100000	508	.99492	.00508	99746	4046440	40.45	25
6	99492	514	.99484	.00516	99235	3946694	39.67	6
7	98978	520	.99474	.00526	98718	3847459	38.87	7
8	98458	529	.99462	.00538	98193	3748741	38.07	8
9	97929	540	.99448	.00552	97659	3650548	37.28	9
30	97389	555	.99430	.00570	97112	3552889	36.48	30
1	96834	571	.99410	.00590	96548	3455777	35.69	1
2	96263	590	.99386	.00614	95968	3359229	34.89	2
3	95673	615	.99358	.00642	95366	3263261	34.10	3
4	95058	639	.99328	.00672	94738	3167895	33.33	4
35	94419	663	.99298	.00702	94088	3073157	32.55	35
6	93756	686	.99269	.00731	93413	2979069	31.78	6
7	93070	702	.99245	.00755	92719	2885656	31.01	7
8	92368	719	.99223	.00777	92008	2792937	30.24	8
9	91649	731	.99201	.00799	91284	2700929	29.47	9
40	90918	753	.99172	.00828	90541	2609645	28.70	40
1	90165	783	.99131	.00869	89774	2519104	27.94	1
2	89382	828	.99075	.00925	88968	2429330	27.17	2
3	88554	880	.99006	.00994	88114	2340362	26.42	3
4	87674	938	.98931	.01069	87205	2252248	25.69	4
45	86736	993	.98855	.01145	86239	2165043	24.96	45
6	85743	1044	.98783	.01217	85221	2078804	24.25	6
7	84699	1085	.98719	.01281	84157	1993583	23.54	7
8	83614	1120	.98659	.01341	83054	1909426	22.83	8
9	82494	1157	.98598	.01402	81915	1826372	22.14	9
50	81337	1193	.98532	.01468	80741	1744457	21.44	50
1	80144	1238	.98455	.01545	79525	1663716	20.76	1
2	78906	1287	.98369	.01631	78262	1584191	20.08	2
3	77619	1337	.98277	.01723	76951	1505929	19.40	3
4	76282	1391	.98177	.01823	75586	1428978	18.73	4
55	74891	1448	.98066	.01934	74167	1353392	18.07	55
6	73443	1511	.97943	.02057	72688	1279225	17.41	6
7	71932	1578	.97806	.02194	71143	1206537	16.78	7
8	70354	1650	.97655	.02345	69529	1135394	16.13	8
9	68704	1723	.97493	.02507	67842	1065865	15.52	9
60	66981	1796	.97320	.02680	66083	998023	14.90	60
1	65185	1865	.97138	.02862	64253	931940	14.30	1
2	63320	1927	.96958	.03042	62356	867687	13.71	2
3	61393	1977	.96779	.03221	60405	805331	13.12	3
4	59416	2029	.96584	.03416	58401	744926	12.54	4
65	57387	2093	.96353	.03647	56341	686525	11.96	65
6	55294	2175	.96065	.03935	54206	630184	11.40	6
7	53119	2282	.95705	.04295	51978	575978	10.84	7
8	50837	2400	.95280	.04720	49637	524000	10.31	8
9	48437	2515	.94806	.05194	47180	474363	9.79	9
70	45922	2618	.94300	.05700	44613	427183	9.30	70
1	43304	2693	.93780	.06220	41957	382570	8.83	1
2	40611	2741	.93253	.06747	39241	340613	8.39	2
3	37870	2762	.92705	.07295	36489	301372	7.96	3
4	35108	2766	.92123	.07877	33725	264883	7.55	4
75	32342	2750	.91495	.08505	30967	231158	7.15	75
6	29592	2721	.90804	.09196	28231	200191	6.77	6
7	26871	2681	.90025	.09975	25531	171960	6.40	7
8	24190	2622	.89158	.10842	22879	146429	6.05	8
9	21568	2539	.88228	.11772	20298	123550	5.73	9

Table VII.—Life Table for England and Wales.—Widowed
Females (Widows)—cont.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	${}^o e_x$	AGE. <i>x</i>
80	19029	2423	.87266	.12734	17818	103252	5.43	80
1	16606	2274	.86309	.13691	15469	85434	5.14	1
2	14332	2095	.85382	.14618	13284	69965	4.88	2
3	12237	1901	.84465	.15535	11287	56681	4.63	3
4	10336	1702	.83528	.16472	9485	45394	4.39	4
85	8634	1508	.82534	.17466	7880	35909	4.16	85
6	7126	1322	.81445	.18555	6465	28029	3.93	6
7	5804	1148	.80226	.19774	5230	21564	3.71	7
8	4656	983	.78894	.21106	4164	16334	3.51	8
9	3673	827	.77475	.22525	3260	12170	3.31	9
90	2846	683	.76006	.23994	2504	8910	3.13	90
1	2163	551	.74532	.25468	1888	6406	2.96	1
2	1612	434	.73067	.26933	1395	4518	2.80	2
3	1178	335	.71608	.28392	1010	3123	2.65	3
4	843	252	.70125	.29875	717	2113	2.51	4
95	591	185	.68569	.31431	499	1396	2.36	95
6	406	135	.66882	.33118	338	897	2.21	6
7	271	95	.64968	.35032	224	559	2.06	7
8	176	65	.62700	.37300	143	335	1.91	8
9	111	45	.59911	.40089	89	192	1.74	9
100	66	29	.56421	.43579	51	103	1.58	100
1	37	18	.52073	.47927	28	52	1.41	1
2	19	10	.46784	.53216	14	24	1.24	2
3	9	5	.40599	.59401	7	10	1.09	3
4	4	3	.33730	.66270	2	3	.95	4
105	1	1	.26561	.73439	1	1	.83	105
6	0	0	.19607	.80393	0	0	.72	6

Table VIII.—COUNTY OF LONDON, 1911-12.—MALES.

AGE. <i>x</i>	<i>l_x</i>	<i>d_x</i>	<i>p_x</i>	<i>q_x</i>	<i>L_x</i>	<i>T_x</i>	$\overset{\circ}{e}_x$	AGE. <i>x</i>
12	100000	205	·99795	·00205	99897	4943121	49·43	12
3	99795	218	·99782	·00218	99686	4843224	48·53	3
4	99577	229	·99769	·00231	99463	4743538	47·63	4
15	99348	244	·99755	·00245	99226	4644075	46·74	15
6	99104	258	·99740	·00260	98975	4544849	45·86	6
7	98846	273	·99725	·00275	98709	4445874	44·98	7
8	98573	285	·99710	·00290	98431	4347165	44·11	8
9	98288	301	·99695	·00305	98137	4248734	43·23	9
20	97987	313	·99680	·00320	97831	4150597	42·35	20
1	97674	328	·99664	·00336	97510	4052766	41·50	1
2	97346	342	·99648	·00352	97175	3955256	40·63	2
3	97004	357	·99632	·00368	96825	3858081	39·77	3
4	96647	371	·99617	·00383	96462	3761256	38·92	4
25	96276	385	·99601	·00399	96083	3664794	38·06	25
6	95891	401	·99582	·00418	95691	3568711	37·21	6
7	95490	421	·99559	·00441	95279	3473020	36·37	7
8	95069	445	·99532	·00468	94847	3377741	35·53	8
9	94624	472	·99501	·00499	94388	3282894	34·70	9
30	94152	502	·99468	·00532	93901	3188506	33·87	30
1	93650	531	·99432	·00568	93384	3094605	33·04	1
2	93119	566	·99392	·00608	92836	3001221	32·23	2
3	92553	603	·99349	·00651	92252	2908385	31·43	3
4	91950	640	·99304	·00696	91630	2816133	30·63	4
35	91310	680	·99255	·00745	90970	2724503	29·84	35
6	90630	724	·99203	·00797	90268	2633533	29·06	6
7	89906	764	·99149	·00851	89524	2543265	28·29	7
8	89142	810	·99092	·00908	88737	2453741	27·52	8
9	88332	854	·99033	·00967	87905	2365004	26·77	9
40	87478	901	·98970	·01030	87027	2277099	26·03	40
1	86577	950	·98904	·01096	86102	2190072	25·30	1
2	85627	998	·98835	·01165	85128	2103970	24·57	2
3	84629	1048	·98762	·01238	84105	2018842	23·86	3
4	83581	1097	·98686	·01314	83033	1934737	23·15	4
45	82484	1149	·98607	·01393	81909	1851704	22·45	45
6	81335	1202	·98522	·01478	80734	1769795	21·76	6
7	80133	1256	·98432	·01568	79505	1689061	21·08	7
8	78877	1311	·98338	·01662	78222	1609556	20·41	8
9	77566	1367	·98239	·01761	76882	1531334	19·74	9
50	76199	1422	·98135	·01865	75488	1454452	19·09	50
1	74777	1479	·98021	·01979	74038	1378964	18·44	1
2	73298	1543	·97896	·02104	72526	1304926	17·80	2
3	71755	1608	·97759	·02241	70951	1232400	17·18	3
4	70147	1675	·97611	·02389	69310	1161449	16·56	4
55	68472	1745	·97452	·02548	67599	1092139	15·95	55
6	66727	1816	·97280	·02720	65819	1024540	15·35	6
7	64911	1885	·97095	·02905	63969	958721	14·77	7
8	63026	1957	·96894	·03106	62047	894752	14·20	8
9	61069	2030	·96677	·03323	60054	832705	13·64	9
60	59039	2099	·96445	·03555	57990	772651	13·09	60
1	56940	2163	·96202	·03798	55858	714661	12·55	1
2	54777	2220	·95947	·04053	53667	658803	12·03	2
3	52557	2264	·95694	·04306	51425	605136	11·51	3
4	50293	2293	·95440	·04560	49147	553711	11·01	4
65	48000	2320	·95167	·04833	46840	504564	10·51	65
6	45680	2350	·94855	·05145	44505	457724	10·02	6
7	43330	2391	·94482	·05518	42134	413219	9·54	7
8	40939	2443	·94031	·05969	39718	371085	9·06	8
9	38496	2499	·93511	·06489	37246	331367	8·61	9

Table VIII.—County of London, 1911-12.—Males—cont.

AGE. <i>x</i>	<i>l_x</i>	<i>d_x</i>	<i>p_x</i>	<i>q_x</i>	<i>L_x</i>	<i>T_x</i>	$\overset{\circ}{e}_x$	AGE. <i>x</i>
70	35997	2544	·92934	·07066	34725	294121	8·17	70
1	33453	2569	·92318	·07682	32169	259396	7·75	1
2	30884	2570	·91680	·08320	29599	227227	7·36	2
3	28314	2542	·91022	·08978	27043	197628	6·98	3
4	25772	2493	·90327	·09673	24525	170585	6·62	4
75	23279	2423	·89591	·10409	22068	146060	6·28	75
6	20856	2334	·88808	·11192	19689	123992	5·95	6
7	18522	2228	·87971	·12029	17408	104303	5·63	7
8	16294	2110	·87054	·12946	15239	86895	5·33	8
9	14184	1978	·86052	·13948	13195	71656	5·05	9
80	12206	1832	·84994	·15006	11290	58461	4·79	80
1	10374	1668	·83917	·16083	9540	47171	4·55	1
2	8706	1492	·82863	·17137	7960	37631	4·32	2
3	7214	1307	·81890	·18110	6561	29671	4·11	3
4	5907	1123	·80981	·19019	5345	23110	3·91	4
85	4784	954	·80061	·19939	4307	17765	3·71	85
6	3830	802	·79046	·20954	3429	13458	3·51	6
7	3028	671	·77841	·22159	2693	10029	3·31	7
8	2357	558	·76324	·23676	2078	7336	3·11	8
9	1799	459	·74522	·25478	1569	5258	2·92	9
90	1340	367	·72566	·27434	1157	3689	2·75	90
1	973	286	·70620	·29380	830	2532	2·60	1
2	687	214	·68882	·31118	580	1702	2·48	2
3	473	154	·67437	·32563	396	1122	2·37	3
4	319	108	·66269	·33731	265	726	2·28	4
95	211	73	·65278	·34722	174	461	2·19	95
6	138	49	·64282	·35718	114	287	2·08	6
7	89	33	·63020	·36980	72	173	1·96	7
8	56	22	·61186	·38814	45	101	1·82	8
9	34	14	·58453	·41547	27	56	1·66	9
100	20	9	·54534	·45466	15	29	1·48	100
1	11	6	·49254	·50746	8	14	1·30	1
2	5	3	·42641	·57359	4	6	1·12	2
3	2	1	·34999	·65001	1	2	·96	3
4	1	1	·26904	·73096	1	1	·83	4

Table IX.—COUNTY OF LONDON, 1911-12.—FEMALES.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	${}^o e_x$	AGE. <i>x</i>
12	100000	191	.99808	.00192	99904	5381285	53.81	12
3	99809	202	.99797	.00203	99708	5281381	52.92	3
4	99607	213	.99787	.00213	99501	5181673	52.02	4
15	99394	222	.99778	.00222	99283	5082172	51.13	15
6	99172	228	.99770	.00230	99058	4982889	50.25	6
7	98944	234	.99763	.00237	98827	4883831	49.36	7
8	98710	239	.99758	.00242	98590	4785004	48.48	8
9	98471	242	.99755	.00245	98350	4686414	47.59	9
20	98229	242	.99753	.00247	98108	4588064	46.71	20
1	97987	245	.99749	.00251	97865	4489956	45.82	1
2	97742	252	.99742	.00258	97616	4392091	44.94	2
3	97490	262	.99732	.00268	97359	4294475	44.05	3
4	97228	273	.99719	.00281	97091	4197116	43.17	4
25	96955	285	.99705	.00295	96813	4100025	42.29	25
6	96670	300	.99689	.00311	96520	4003212	41.41	6
7	96370	315	.99673	.00327	96212	3906692	40.54	7
8	96055	329	.99657	.00343	95891	3810480	39.67	8
9	95726	343	.99642	.00358	95554	3714589	38.80	9
30	95383	360	.99624	.00376	95203	3619035	37.94	30
1	95023	375	.99604	.00396	94836	3523832	37.08	1
2	94648	398	.99579	.00421	94449	3428996	36.23	2
3	94250	427	.99548	.00452	94036	3334547	35.38	3
4	93823	457	.99512	.00488	93595	3240511	34.54	4
35	93366	493	.99472	.00528	93119	3146916	33.71	35
6	92873	529	.99431	.00569	92609	3053797	32.88	6
7	92344	564	.99390	.00610	92062	2961188	32.07	7
8	91780	596	.99350	.00650	91482	2869126	31.26	8
9	91184	630	.99309	.00691	90869	2777644	30.46	9
40	90554	662	.99268	.00732	90223	2686775	29.67	40
1	89892	699	.99223	.00777	89542	2596552	28.89	1
2	89193	736	.99175	.00825	88825	2507010	28.11	2
3	88457	777	.99122	.00878	88069	2418185	27.34	3
4	87680	820	.99064	.00936	87270	2330116	26.58	4
45	86860	866	.99004	.00996	86427	2242846	25.82	45
6	85994	910	.98942	.01058	85539	2156419	25.08	6
7	85084	952	.98880	.01120	84608	2070880	24.34	7
8	84132	992	.98821	.01179	83636	1986272	23.61	8
9	83140	1029	.98763	.01237	82625	1902636	22.88	9
50	82111	1065	.98703	.01297	81579	1820011	22.17	50
1	81046	1107	.98634	.01366	80492	1738432	21.45	1
2	79939	1156	.98553	.01447	79361	1657940	20.74	2
3	78783	1215	.98457	.01543	78176	1578579	20.04	3
4	77568	1281	.98350	.01650	76927	1500403	19.34	4
55	76287	1349	.98232	.01768	75613	1423476	18.66	55
6	74938	1419	.98107	.01893	74228	1347863	17.99	6
7	73519	1488	.97977	.02023	72775	1273635	17.32	7
8	72031	1554	.97844	.02156	71254	1200860	16.67	8
9	70477	1615	.97707	.02293	69670	1129606	16.03	9
60	68862	1679	.97561	.02439	68022	1059936	15.39	60
1	67183	1747	.97401	.02599	66310	991914	14.76	1
2	65436	1818	.97221	.02779	64527	925604	14.15	2
3	63618	1889	.97030	.02970	62673	861077	13.54	3
4	61729	1957	.96830	.03170	60751	798404	12.93	4
65	59772	2028	.96608	.03392	58758	737653	12.34	65
6	57744	2107	.96349	.03651	56690	678895	11.76	6
7	55637	2205	.96038	.03962	54535	622205	11.18	7
8	53432	2319	.95659	.04341	52272	567670	10.62	8
9	51113	2445	.95217	.04783	49891	515398	10.08	9

Table IX.—County of London, 1911-12.—Females—cont.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	${}^o e_x$	AGE. <i>x</i>
70	48668	2567	.94726	.05274	47384	465507	9.57	70
1	46101	2672	.94204	.05796	44765	418123	9.07	1
2	43429	2750	.93668	.06332	42054	373358	8.60	2
3	40679	2794	.93133	.06867	39282	331304	8.14	3
4	37885	2809	.92585	.07415	36481	292022	7.71	4
75	35076	2805	.92002	.07998	33673	255541	7.29	75
6	32271	2789	.91359	.08641	30877	221868	6.88	6
7	29482	2763	.90628	.09372	28100	190991	6.48	7
8	26719	2731	.89779	.10221	25354	162891	6.10	8
9	23988	2683	.88816	.11184	22646	137537	5.73	9
80	21305	2608	.87761	.12239	20001	114891	5.39	80
1	18697	2497	.86644	.13356	17449	94890	5.08	1
2	16200	2349	.85500	.14500	15025	77441	4.78	2
3	13851	2173	.84306	.15694	12765	62416	4.51	3
4	11678	1982	.83032	.16968	10687	49651	4.25	4
85	9696	1773	.81710	.18290	8809	38964	4.02	85
6	7923	1555	.80380	.19620	7146	30155	3.81	6
7	6368	1331	.79087	.20913	5702	23009	3.61	7
8	5037	1112	.77908	.22092	4481	17307	3.44	8
9	3924	909	.76833	.23167	3469	12826	3.27	9
90	3015	731	.75765	.24235	2650	9357	3.10	90
1	2284	580	.74597	.25403	1994	6707	2.94	1
2	1704	457	.73207	.26793	1475	4713	2.77	2
3	1247	355	.71537	.28463	1070	3238	2.60	3
4	892	271	.69594	.30406	756	2168	2.43	4
95	621	202	.67434	.32566	520	1412	2.27	95
6	419	146	.65164	.34836	346	892	2.13	6
7	273	101	.62926	.37074	223	546	2.00	7
8	172	68	.60773	.39227	138	323	1.88	8
9	104	43	.58684	.41316	82	185	1.77	9
100	61	26	.56576	.43424	48	103	1.66	100
1	35	16	.54314	.45686	27	55	1.56	1
2	19	9	.51729	.48271	15	28	1.45	2
3	10	5	.48636	.51364	7	13	1.33	3
4	5	3	.44871	.55129	4	6	1.22	4
105	2	1	.40330	.59670	1	2	1.10	105
6	1	1	.35020	.64980	1	1	.98	6

Table X.—AGGREGATE OF COUNTY BOROUGHS, 1911-12.—
MALES.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
12	100000	205	.99796	.00204	99897	4895101	48.96	12
3	99795	232	.99768	.00232	99679	4795204	48.05	3
4	99563	256	.99743	.00257	99435	4695525	47.16	4
15	99307	279	.99720	.00280	99168	4596090	46.28	15
6	99028	298	.99698	.00302	98879	4496922	45.42	6
7	98730	318	.99678	.00322	98571	4398043	44.55	7
8	98412	334	.99659	.00341	98245	4299472	43.69	8
9	98078	352	.99641	.00359	97902	4201227	42.84	9
20	97726	368	.99624	.00376	97542	4103325	41.99	20
1	97358	383	.99608	.00392	97166	4005783	41.14	1
2	96975	394	.99593	.00407	96778	3908617	40.31	2
3	96581	406	.99579	.00421	96378	3811839	39.46	3
4	96175	416	.99567	.00433	95967	3715461	38.64	4
25	95759	427	.99555	.00445	95546	3619494	37.80	25
6	95332	438	.99541	.00459	95113	3523948	36.97	6
7	94894	453	.99522	.00478	94667	3428835	36.13	7
8	94441	473	.99499	.00501	94205	3334168	35.30	8
9	93968	494	.99474	.00526	93721	3239963	34.48	9
30	93474	520	.99445	.00555	93214	3146242	33.66	30
1	92954	544	.99414	.00586	92682	3053028	32.85	1
2	92410	573	.99380	.00620	92123	2960346	32.03	2
3	91837	602	.99343	.00657	91536	2868223	31.23	3
4	91235	637	.99302	.00698	90917	2776687	30.44	4
35	90598	671	.99258	.00742	90262	2685770	29.65	35
6	89927	710	.99212	.00788	89572	2595508	28.86	6
7	89217	744	.99165	.00835	88845	2505936	28.09	7
8	88473	781	.99118	.00882	88083	2417091	27.32	8
9	87692	814	.99071	.00929	87285	2329008	26.56	9
40	86878	850	.99021	.00979	86453	2241723	25.80	40
1	86028	889	.98966	.01034	85583	2155270	25.06	1
2	85139	934	.98903	.01097	84672	2069687	24.31	2
3	84205	985	.98831	.01169	83713	1985015	23.57	3
4	83220	1037	.98753	.01247	82701	1901302	22.85	4
45	82183	1094	.98668	.01332	81636	1818601	22.13	45
6	81089	1153	.98577	.01423	80513	1736965	21.42	6
7	79936	1213	.98482	.01518	79329	1656452	20.73	7
8	78723	1273	.98384	.01616	78087	1577123	20.04	8
9	77450	1330	.98283	.01717	76785	1499036	19.36	9
50	76120	1389	.98175	.01825	75425	1422251	18.69	50
1	74731	1452	.98057	.01943	74005	1346826	18.02	1
2	73279	1521	.97924	.02076	72519	1272821	17.37	2
3	71758	1595	.97777	.02223	70960	1200302	16.73	3
4	70163	1671	.97617	.02383	69328	1129342	16.10	4
55	68492	1751	.97443	.02557	67616	1060014	15.48	55
6	66741	1833	.97254	.02746	65825	992398	14.87	6
7	64908	1914	.97050	.02950	63951	926573	14.28	7
8	62994	1998	.96827	.03173	61995	862622	13.69	8
9	60996	2083	.96584	.03416	59954	800627	13.13	9
60	58913	2165	.96325	.03675	57831	740673	12.57	60
1	56748	2241	.96051	.03949	55627	682842	12.03	1
2	54507	2308	.95765	.04235	53353	627215	11.51	2
3	52199	2358	.95484	.04516	51020	573862	11.00	3
4	49841	2389	.95205	.04795	48647	522842	10.49	4
65	47452	2419	.94904	.05096	46242	474195	9.99	65
6	45033	2454	.94551	.05449	43806	427953	9.50	6
7	42579	2505	.94115	.05885	41327	384147	9.02	7
8	40074	2581	.93559	.06441	38783	342820	8.56	8
9	37493	2665	.92893	.07107	36161	304037	8.11	9

Table X.—Aggregate of County Boroughs, 1911-12.—Males—*cont.*

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
70	34828	2733	.92153	.07847	33461	267876	7.69	70
1	32095	2765	.91385	.08615	30713	234415	7.31	1
2	29330	2745	.90643	.09357	27957	203702	6.95	2
3	26585	2672	.89947	.10053	25249	175745	6.61	3
4	23913	2567	.89265	.10735	22630	150496	6.29	4
75	21346	2439	.88577	.11423	20126	127866	5.99	75
6	18907	2295	.87860	.12140	17760	107740	5.70	6
7	16612	2145	.87087	.12913	15539	89980	5.42	7
8	14467	1989	.86255	.13745	13473	74441	5.15	8
9	12478	1825	.85375	.14625	11565	60968	4.89	9
80	10653	1657	.84446	.15554	9825	49403	4.64	80
1	8996	1487	.83467	.16533	8252	39578	4.39	1
2	7509	1319	.82435	.17565	6850	31326	4.17	2
3	6190	1155	.81340	.18660	5612	24476	3.95	3
4	5035	998	.80178	.19822	4536	18864	3.75	4
85	4037	850	.78954	.21046	3612	14328	3.55	85
6	3187	711	.77673	.22327	2832	10716	3.36	6
7	2476	586	.76343	.23657	2183	7884	3.18	7
8	1890	474	.74946	.25054	1653	5701	3.02	8
9	1416	375	.73475	.26525	1228	4048	2.86	9
90	1041	292	.71945	.28055	895	2820	2.71	90
1	749	222	.70382	.29618	638	1925	2.57	1
2	527	164	.68813	.31187	445	1287	2.44	2
3	363	119	.67250	.32750	304	842	2.32	3
4	244	84	.65690	.34310	202	538	2.20	4
95	160	57	.64117	.35883	131	336	2.09	95
6	103	39	.62506	.37494	84	205	1.99	6
7	64	25	.60818	.39182	51	121	1.88	7
8	39	16	.58956	.41044	31	70	1.77	8
9	23	10	.56770	.43230	18	39	1.65	9
100	13	6	.54077	.45923	10	21	1.52	100
1	7	3	.50689	.49311	6	11	1.39	1
2	4	2	.46455	.53545	3	5	1.25	2
3	2	1	.41312	.58688	1	2	1.11	3
4	1	1	.35340	.64660	1	1	.98	4

Table XI.—AGGREGATE OF COUNTY BOROUGHS, 1911-12.—FEMALES.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	$^o e_x$	AGE. <i>x</i>
12	100000	219	.99782	.00218	99890	5228006	52.28	12
3	99781	236	.99763	.00237	99663	5128116	51.39	3
4	99545	252	.99746	.00254	99419	5028453	50.52	4
15	99293	267	.99731	.00269	99160	4929034	49.64	15
6	99026	280	.99717	.00283	98886	4829874	48.77	6
7	98746	290	.99705	.00295	98601	4730988	47.91	7
8	98456	302	.99694	.00306	98305	4632387	47.05	8
9	98154	309	.99684	.00316	97999	4534082	46.19	9
20	97845	317	.99675	.00325	97687	4436083	45.34	20
1	97528	325	.99667	.00333	97365	4338396	44.48	1
2	97203	333	.99658	.00342	97037	4241031	43.63	2
3	96870	338	.99650	.00350	96701	4143994	42.78	3
4	96532	346	.99642	.00358	96359	4047293	41.93	4
25	96186	352	.99634	.00366	96010	3950934	41.08	25
6	95834	361	.99624	.00376	95653	3854924	40.22	6
7	95473	371	.99612	.00388	95288	3759271	39.38	7
8	95102	382	.99598	.00402	94911	3663983	38.53	8
9	94720	394	.99584	.00416	94523	3569072	37.68	9
30	94326	408	.99567	.00433	94122	3474549	36.84	30
1	93918	425	.99547	.00453	93705	3380427	35.99	1
2	93493	449	.99521	.00479	93269	3286722	35.15	2
3	93044	476	.99488	.00512	92806	3193453	34.32	3
4	92568	510	.99448	.00552	92313	3100647	33.50	4
35	92058	548	.99406	.00594	91784	3008334	32.68	35
6	91510	584	.99363	.00637	91218	2916550	31.87	6
7	90926	615	.99324	.00676	90618	2825332	31.07	7
8	90311	640	.99292	.00708	89991	2734714	30.28	8
9	89671	661	.99264	.00736	89341	2644723	29.49	9
40	89010	680	.99236	.00764	88670	2555382	28.71	40
1	88330	703	.99204	.00796	87978	2466712	27.93	1
2	87627	733	.99164	.00836	87261	2378734	27.15	2
3	86894	769	.99114	.00886	86509	2291473	26.37	3
4	86125	811	.99058	.00942	85720	2204964	25.60	4
45	85314	856	.98996	.01004	84886	2119244	24.84	45
6	84458	903	.98931	.01069	84006	2034358	24.09	6
7	83555	951	.98863	.01137	83080	1950352	23.34	7
8	82604	995	.98796	.01204	82106	1867272	22.61	8
9	81609	1038	.98728	.01272	81090	1785166	21.88	9
50	80571	1083	.98655	.01345	80030	1704076	21.15	50
1	79488	1134	.98573	.01427	78921	1624046	20.43	1
2	78354	1193	.98478	.01522	77757	1545125	19.72	2
3	77161	1260	.98368	.01632	76531	1467368	19.02	3
4	75901	1332	.98245	.01755	75235	1390837	18.32	4
55	74569	1408	.98112	.01888	73865	1315602	17.64	55
6	73161	1487	.97967	.02033	72418	1241737	16.97	6
7	71674	1569	.97812	.02188	70889	1169319	16.32	7
8	70105	1649	.97648	.02352	69281	1098430	15.67	8
9	68456	1731	.97473	.02527	67590	1029149	15.03	9
60	66725	1811	.97285	.02715	65820	961559	14.41	60
1	64914	1894	.97083	.02917	63967	895739	13.80	1
2	63020	1975	.96865	.03135	62032	831772	13.20	2
3	61045	2049	.96643	.03357	60021	769740	12.61	3
4	58996	2113	.96418	.03582	57939	709719	12.03	4
65	56883	2179	.96169	.03831	55794	651780	11.46	65
6	54704	2257	.95874	.04126	53575	595986	10.90	6
7	52447	2356	.95507	.04493	51269	542411	10.34	7
8	50091	2484	.95040	.04960	48849	491142	9.81	8
9	47607	2628	.94480	.05520	46293	442293	9.29	9

Table XI.—Aggregate of County Boroughs, 1911-12.—Females—cont.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	$^o e_x$	AGE. <i>x</i>
70	44979	2764	.93855	.06145	43597	396000	8.80	70
1	42215	2871	.93198	.06802	40780	352403	8.35	1
2	39344	2932	.92548	.07452	37878	311623	7.92	2
3	36412	2942	.91920	.08080	34941	273745	7.52	3
4	33470	2915	.91289	.08711	32012	238804	7.13	4
75	30555	2861	.90637	.09363	29125	206792	6.77	75
6	27694	2785	.89943	.10057	26301	177667	6.42	6
7	24909	2694	.89185	.10815	23562	151366	6.08	7
8	22215	2590	.88339	.11661	20920	127804	5.75	8
9	19625	2470	.87413	.12587	18390	106884	5.45	9
80	17155	2329	.86427	.13573	15991	88494	5.16	80
1	14826	2164	.85405	.14595	13744	72503	4.89	1
2	12662	1978	.84377	.15623	11673	58759	4.64	2
3	10684	1779	.83352	.16648	9794	47086	4.41	3
4	8905	1575	.82313	.17687	8118	37292	4.19	4
85	7330	1374	.81249	.18751	6643	29174	3.98	85
6	5956	1182	.80150	.19850	5365	22531	3.78	6
7	4774	1003	.79000	.21000	4272	17166	3.60	7
8	3771	838	.77768	.22232	3352	12894	3.42	8
9	2933	691	.76456	.23544	2588	9542	3.25	9
90	2242	558	.75108	.24892	1963	6954	3.10	90
1	1684	441	.73776	.26224	1463	4991	2.96	1
2	1243	342	.72516	.27484	1072	3528	2.84	2
3	901	258	.71351	.28649	772	2456	2.73	3
4	643	191	.70281	.29719	548	1684	2.62	4
95	452	139	.69282	.30718	382	1136	2.51	95
6	313	99	.68306	.31694	264	754	2.41	6
7	214	70	.67284	.32716	179	490	2.29	7
8	144	49	.66074	.33926	119	311	2.16	8
9	95	34	.64473	.35527	78	192	2.02	9
100	61	23	.62233	.37767	50	114	1.85	100
1	38	15	.59089	.40911	30	64	1.67	1
2	23	11	.54816	.45184	18	34	1.49	2
3	12	6	.49292	.50708	9	16	1.30	3
4	6	3	.42577	.57423	4	7	1.12	4
105	3	2	.34968	.65032	2	3	.96	105
6	1	1	.26997	.73003	1	1	.83	6

Table XII.—AGGREGATE OF URBAN DISTRICTS, 1911-12.—
MALES.

AGE. x	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. x
12	100000	175	.99825	.00175	99912	5170125	51.70	12
3	99825	204	.99795	.00205	99723	5070213	50.79	3
4	99621	232	.99767	.00233	99505	4970490	49.90	4
15	99389	258	.99741	.00259	99260	4870985	49.01	15
6	99131	280	.99718	.00282	98991	4771725	48.14	6
7	98851	298	.99698	.00302	98702	4672734	47.27	7
8	98553	313	.99682	.00318	98397	4574032	46.41	8
9	98240	325	.99670	.00330	98077	4475635	45.56	9
20	97915	333	.99660	.00340	97749	4377558	44.71	20
1	97582	341	.99651	.00349	97411	4279809	43.86	1
2	97241	349	.99642	.00358	97067	4182398	43.01	2
3	96892	356	.99632	.00368	96714	4085331	42.16	3
4	96536	364	.99624	.00376	96354	3988617	41.31	4
25	96172	371	.99615	.00385	95986	3892263	40.48	25
6	95801	376	.99606	.00394	95613	3796277	39.63	6
7	95425	386	.99595	.00405	95232	3700664	38.78	7
8	95039	396	.99584	.00416	94841	3605432	37.94	8
9	94643	404	.99572	.00428	94441	3510591	37.09	9
30	94239	416	.99559	.00441	94031	3416150	36.25	30
1	93823	427	.99544	.00456	93610	3322119	35.41	1
2	93396	444	.99524	.00476	93174	3228509	34.57	2
3	92952	465	.99499	.00501	92719	3135335	33.73	3
4	92487	491	.99469	.00531	92242	3042616	32.90	4
35	91996	517	.99437	.00563	91737	2950374	32.07	35
6	91479	546	.99404	.00596	91206	2858637	31.25	6
7	90933	572	.99370	.00630	90647	2767431	30.44	7
8	90361	597	.99338	.00662	90063	2676784	29.62	8
9	89764	622	.99308	.00692	89453	2586721	28.82	9
40	89142	647	.99276	.00724	88818	2497268	28.02	40
1	88495	674	.99239	.00761	88158	2408450	27.21	1
2	87821	707	.99194	.00806	87468	2320292	26.42	2
3	87114	747	.99142	.00858	86740	2232824	25.63	3
4	86367	791	.99084	.00916	85972	2146084	24.85	4
45	85576	838	.99021	.00979	85157	2060112	24.07	45
6	84738	889	.98951	.01049	84293	1974955	23.31	6
7	83849	944	.98873	.01127	83377	1890662	22.55	7
8	82905	1006	.98788	.01212	82402	1807285	21.80	8
9	81899	1068	.98696	.01304	81365	1724883	21.06	9
50	80831	1134	.98596	.01404	80264	1643518	20.33	50
1	79697	1206	.98488	.01512	79094	1563254	19.62	1
2	78491	1276	.98373	.01627	77853	1484160	18.91	2
3	77215	1349	.98253	.01747	76541	1406307	18.21	3
4	75866	1419	.98130	.01870	75156	1329766	17.53	4
55	74447	1491	.97996	.02004	73702	1254610	16.85	55
6	72956	1572	.97845	.02155	72170	1180908	16.19	6
7	71384	1662	.97671	.02329	70553	1108738	15.53	7
8	69722	1764	.97469	.02531	68840	1038185	14.89	8
9	67958	1875	.97241	.02759	67020	969345	14.26	9
60	66083	1987	.96992	.03008	65090	902325	13.66	60
1	64096	2096	.96730	.03270	63043	837235	13.06	1
2	62000	2195	.96460	.03540	60902	774187	12.49	2
3	59805	2274	.96196	.03804	58668	713285	11.93	3
4	57531	2339	.95935	.04065	56362	654617	11.38	4
65	55192	2399	.95654	.04346	53992	598255	10.84	65
6	52798	2466	.95328	.04672	51560	544263	10.31	6
7	50327	2551	.94931	.05069	49052	492703	9.79	7
8	47776	2658	.94436	.05564	46447	443651	9.29	8
9	45118	2774	.93852	.06148	43731	397204	8.80	9

Table XII.—Aggregate of Urban Districts, 1911-12.—Males—cont.

AGE. x	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. x
70	42344	2878	.93203	.06797	40905	353473	8.35	70
1	39466	2951	.92522	.07478	37990	312568	7.92	1
2	36515	2978	.91844	.08156	35026	274578	7.52	2
3	33537	2960	.91174	.08826	32057	239552	7.14	3
4	30577	2909	.90488	.09512	29123	207495	6.79	4
75	27668	2827	.89782	.10218	26254	178372	6.45	75
6	24841	2720	.89051	.10949	23481	152118	6.12	6
7	22121	2590	.88290	.11710	20826	128637	5.82	7
8	19531	2438	.87519	.12481	18312	107811	5.52	8
9	17093	2266	.86742	.13258	15960	89499	5.24	9
80	14827	2087	.85926	.14074	13784	73539	4.96	80
1	12740	1907	.85033	.14967	11786	59755	4.69	1
2	10833	1731	.84021	.15979	9968	47969	4.43	2
3	9102	1564	.82819	.17181	8320	38001	4.18	3
4	7538	1399	.81431	.18569	6838	29681	3.94	4
85	6139	1232	.79934	.20066	5523	22843	3.72	85
6	4907	1059	.78419	.21581	4378	17320	3.53	6
7	3848	885	.77000	.23000	3405	12942	3.36	7
8	2963	721	.75674	.24326	2603	9537	3.22	8
9	2242	574	.74379	.25621	1955	6934	3.09	9
90	1668	448	.73160	.26840	1444	4979	2.98	90
1	1220	341	.72065	.27935	1049	3535	2.90	1
2	879	253	.71147	.28853	753	2486	2.83	2
3	626	185	.70437	.29563	533	1733	2.77	3
4	441	133	.69933	.30067	375	1200	2.72	4
95	308	93	.69615	.30385	261	825	2.68	95
6	215	66	.69438	.30562	182	564	2.62	6
7	149	46	.69337	.30663	126	382	2.56	7
8	103	32	.69167	.30833	87	256	2.47	8
9	71	22	.68704	.31296	60	169	2.35	9
100	49	16	.67655	.32345	41	109	2.19	100
1	33	11	.65683	.34317	28	68	2.00	1
2	22	8	.62448	.37552	18	40	1.79	2
3	14	6	.57690	.42310	11	22	1.56	3
4	8	4	.51319	.48681	6	11	1.34	4
105	4	2	.43516	.56484	3	5	1.13	105
6	2	1	.34778	.65222	1	2	.96	6
7	1	1	.25871	.74129	1	1	.81	7

Table XIII.—AGGREGATE OF URBAN DISTRICTS, 1911-12.—FEMALES.

Table with columns for AGE, lx, dx, px, qx, Lx, Tx, ex, AGE. Data rows for ages 12, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65.

Table XIII.—Aggregate of Urban Districts, 1911-12.—Females—cont.

Table with columns for AGE, lx, dx, px, qx, Lx, Tx, ex, AGE. Data rows for ages 70, 75, 80, 85, 90, 95, 100, 105.

Table XIV.—AGGREGATE OF RURAL DISTRICTS, 1911-12.—
MALES.

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
12	100000	161	·99840	·00160	99919	5416589	54·16	12
3	99839	177	·99822	·00178	99751	5316670	53·25	3
4	99662	197	·99803	·00197	99563	5216919	52·35	4
15	99465	215	·99784	·00216	99358	5117356	51·45	15
6	99250	235	·99764	·00236	99132	5017998	50·56	6
7	99015	253	·99744	·00256	98889	4918866	49·68	7
8	98762	272	·99725	·00275	98626	4819977	48·81	8
9	98490	288	·99707	·00293	98346	4721351	47·94	9
20	98202	305	·99689	·00311	98049	4623005	47·08	20
1	97897	322	·99672	·00328	97736	4524956	46·23	1
2	97575	334	·99657	·00343	97408	4427220	45·37	2
3	97241	344	·99645	·00355	97069	4329812	44·52	3
4	96897	352	·99636	·00364	96721	4232743	43·68	4
25	96545	359	·99628	·00372	96366	4136022	42·84	25
6	96186	365	·99620	·00380	96003	4039656	42·00	6
7	95821	374	·99610	·00390	95634	3943653	41·15	7
8	95447	384	·99598	·00402	95255	3848019	40·32	8
9	95063	396	·99585	·00415	94865	3752764	39·48	9
30	94667	404	·99572	·00428	94465	3657899	38·64	30
1	94263	416	·99558	·00442	94055	3563434	37·80	1
2	93847	427	·99544	·00456	93634	3469379	36·97	2
3	93420	440	·99530	·00470	93200	3375745	36·13	3
4	92980	448	·99517	·00483	92756	3282545	35·30	4
35	92532	459	·99503	·00497	92302	3189789	34·47	35
6	92073	474	·99486	·00514	91836	3097487	33·64	6
7	91599	490	·99466	·00534	91354	3005651	32·82	7
8	91109	509	·99441	·00559	90855	2914297	31·99	8
9	90600	532	·99413	·00587	90334	2823442	31·16	9
40	90068	556	·99382	·00618	89790	2733108	30·35	40
1	89512	584	·99349	·00651	89220	2643318	29·53	1
2	88928	610	·99315	·00685	88623	2554098	28·72	2
3	88318	634	·99282	·00718	88001	2465475	27·92	3
4	87684	658	·99249	·00751	87355	2377474	27·11	4
45	87026	684	·99213	·00787	86684	2290119	26·31	45
6	86342	715	·99173	·00827	85984	2203435	25·52	6
7	85627	748	·99126	·00874	85253	2117451	24·73	7
8	84879	786	·99073	·00927	84486	2032198	23·94	8
9	84093	827	·99016	·00984	83680	1947712	23·16	9
50	83266	873	·98952	·01048	82829	1864032	22·39	50
1	82393	923	·98881	·01119	81932	1781203	21·62	1
2	81470	978	·98799	·01201	80981	1699271	20·86	2
3	80492	1041	·98708	·01292	79971	1618290	20·10	3
4	79451	1104	·98609	·01391	78899	1538319	19·36	4
55	78347	1175	·98500	·01500	77760	1459420	18·63	55
6	77172	1251	·98378	·01622	76546	1381660	17·91	6
7	75921	1336	·98241	·01759	75253	1305114	17·19	7
8	74585	1426	·98089	·01911	73872	1229861	16·49	8
9	73159	1520	·97922	·02078	72399	1155989	15·80	9
60	71639	1618	·97741	·02259	70830	1083590	15·13	60
1	70021	1720	·97543	·02457	69161	1012760	14·46	1
2	68301	1824	·97329	·02671	67389	943599	13·82	2
3	66477	1923	·97107	·02893	65516	876210	13·18	3
4	64554	2018	·96875	·03125	63545	810694	12·56	4
65	62536	2113	·96621	·03379	61479	747149	11·95	65
6	60423	2219	·96328	·03672	59314	685670	11·35	6
7	58204	2339	·95982	·04018	57034	626356	10·76	7
8	55865	2475	·95569	·04431	54628	569322	10·19	8
9	53390	2620	·95094	·04906	52080	514694	9·64	9

Table XIV.—Aggregate of Rural Districts, 1911-12.—Males—*cont.*

AGE. <i>x</i>	l_x	d_x	p_x	q_x	L_x	T_x	e_x	AGE. <i>x</i>
70	50770	2758	·94566	·05434	49391	462614	9·11	70
1	48012	2884	·93993	·06007	46570	413223	8·61	1
2	45128	2985	·93385	·06615	43635	366653	8·13	2
3	42143	3060	·92739	·07261	40613	323018	7·67	3
4	39083	3110	·92043	·07957	37528	282405	7·23	4
75	35973	3132	·91293	·08707	34407	244877	6·81	75
6	32841	3124	·90488	·09512	31279	210470	6·41	6
7	29717	3083	·89624	·10376	28176	179191	6·03	7
8	26634	3013	·88686	·11314	25127	151015	5·67	8
9	23621	2913	·87667	·12333	22165	125888	5·33	9
80	20708	2780	·86576	·13424	19318	103723	5·01	80
1	17928	2613	·85427	·14573	16621	84405	4·71	1
2	15315	2414	·84235	·15765	14108	67784	4·43	2
3	12901	2192	·83012	·16988	11805	53676	4·16	3
4	10709	1955	·81745	·18255	9732	41871	3·91	4
85	8754	1714	·80412	·19588	7897	32139	3·67	85
6	7040	1479	·78992	·21008	6300	24242	3·44	6
7	5561	1254	·77454	·22546	4934	17942	3·23	7
8	4307	1046	·75705	·24295	3784	13008	3·02	8
9	3261	857	·73736	·26264	2833	9224	2·83	9
90	2404	681	·71661	·28339	2063	6391	2·66	90
1	1723	523	·69622	·30378	1462	4328	2·51	1
2	1200	387	·67795	·32205	1006	2866	2·39	2
3	813	274	·66257	·33743	676	1860	2·29	3
4	539	189	·65000	·35000	445	1184	2·20	4
95	350	126	·63946	·36054	287	739	2·11	95
6	224	83	·62949	·37051	182	452	2·03	6
7	141	54	·61797	·38203	114	270	1·92	7
8	87	35	·60230	·39770	70	156	1·80	8
9	52	22	·57948	·42052	41	86	1·66	9
100	30	13	·54664	·45336	23	45	1·50	100
1	17	9	·50157	·49843	13	22	1·34	1
2	8	4	·44358	·55642	6	9	1·17	2
3	4	3	·37425	·62575	2	3	1·01	3
4	1	1	·29781	·70219	1	1	·87	4

Table XV.—AGGREGATE OF RURAL DISTRICTS, 1911-12.—
 FEMALES.

AGE. x	l_x	d_x	p_x	q_x	L_x	T_x	$^{\circ}e_x$	AGE. x
12	100000	173	.99827	.00173	99913	5576300	55.76	12
3	99827	192	.99807	.00193	99731	5476387	54.86	3
4	99635	214	.99787	.00213	99528	5376656	53.97	4
15	99421	231	.99767	.00233	99306	5277128	53.08	15
6	99190	250	.99748	.00252	99065	5177822	52.20	6
7	98940	267	.99731	.00269	98806	5078757	51.33	7
8	98673	281	.99716	.00284	98533	4979951	50.47	8
9	98392	292	.99704	.00296	98246	4881418	49.61	9
20	98100	302	.99692	.00308	97949	4783172	48.76	20
1	97798	313	.99681	.00319	97641	4685223	47.91	1
2	97485	320	.99671	.00329	97325	4587582	47.06	2
3	97165	328	.99661	.00339	97001	4490257	46.21	3
4	96837	336	.99653	.00347	96669	4393256	45.37	4
25	96501	342	.99645	.00355	96330	4296587	44.52	25
6	96159	349	.99636	.00364	95985	4200257	43.68	6
7	95810	359	.99626	.00374	95630	4104272	42.84	7
8	95451	369	.99613	.00387	95267	4008642	42.00	8
9	95082	380	.99599	.00401	94892	3913375	41.16	9
30	94702	394	.99584	.00416	94505	3818483	40.32	30
1	94308	407	.99569	.00431	94104	3723978	39.49	1
2	93901	419	.99555	.00445	93692	3629874	38.66	2
3	93482	427	.99542	.00458	93268	3536182	37.83	3
4	93055	438	.99529	.00471	92836	3442914	37.00	4
35	92617	449	.99516	.00484	92393	3350078	36.17	35
6	92168	457	.99503	.00497	91939	3257685	35.35	6
7	91711	468	.99489	.00511	91477	3165746	34.52	7
8	91243	478	.99476	.00524	91004	3074269	33.69	8
9	90765	487	.99463	.00537	90522	2983265	32.87	9
40	90278	498	.99449	.00551	90029	2892743	32.04	40
1	89780	509	.99433	.00567	89525	2802714	31.22	1
2	89271	525	.99413	.00587	89009	2713189	30.39	2
3	88746	540	.99391	.00609	88476	2624180	29.57	3
4	88206	556	.99368	.00632	87928	2535704	28.75	4
45	87650	578	.99341	.00659	87361	2447776	27.93	45
6	87072	601	.99309	.00691	86771	2360415	27.11	6
7	86471	633	.99269	.00731	86155	2273644	26.29	7
8	85838	669	.99221	.00779	85503	2187489	25.48	8
9	85169	709	.99167	.00833	84815	2101986	24.68	9
50	84460	755	.99106	.00894	84082	2017171	23.88	50
1	83705	806	.99038	.00962	83302	1933089	23.09	1
2	82899	860	.98963	.01037	82469	1849787	22.31	2
3	82039	920	.98879	.01121	81579	1767318	21.54	3
4	81119	984	.98787	.01213	80627	1685739	20.78	4
55	80135	1053	.98687	.01313	79609	1605112	20.03	55
6	79082	1122	.98580	.01420	78521	1525503	19.29	6
7	77960	1196	.98467	.01533	77362	1446982	18.56	7
8	76764	1265	.98352	.01648	76131	1369620	17.84	8
9	75499	1334	.98233	.01767	74832	1293489	17.13	9
60	74165	1404	.98106	.01894	73463	1218657	16.43	60
1	72761	1482	.97963	.02037	72020	1145194	15.74	1
2	71279	1570	.97799	.02201	70494	1073174	15.06	2
3	69709	1660	.97619	.02381	68879	1002680	14.38	3
4	68049	1751	.97428	.02572	67174	933801	13.72	4
65	66298	1847	.97214	.02786	65374	866627	13.07	65
6	64451	1958	.96962	.03038	63472	801253	12.43	6
7	62493	2087	.96660	.03340	61450	737781	11.81	7
8	60406	2239	.96295	.03705	59286	676331	11.20	8
9	58167	2402	.95870	.04130	56966	617045	10.61	9

Table XV.—Aggregate of Rural Districts, 1911-12.—Females—cont.

AGE. x	l_x	d_x	p_x	q_x	L_x	T_x	$^{\circ}e_x$	AGE. x
70	55765	2568	.95396	.04604	54481	560079	10.04	70
1	53197	2722	.94883	.05117	51836	505598	9.50	1
2	50475	2855	.94342	.05658	49048	453762	8.99	2
3	47620	2967	.93770	.06230	46136	404714	8.50	3
4	44653	3057	.93153	.06847	43125	358578	8.03	4
75	41596	3123	.92493	.07507	40034	315453	7.58	75
6	38473	3158	.91790	.08210	36894	275419	7.16	6
7	35315	3162	.91046	.08954	33734	238525	6.75	7
8	32153	3132	.90259	.09741	30587	204791	6.37	8
9	29021	3069	.89425	.10575	27487	174204	6.00	9
80	25952	2975	.88536	.11464	24464	146717	5.65	80
1	22977	2853	.87584	.12416	21551	122253	5.32	1
2	20124	2704	.86563	.13437	18772	100702	5.00	2
3	17420	2534	.85456	.14544	16153	81930	4.70	3
4	14886	2343	.84258	.15742	13714	65777	4.42	4
85	12543	2135	.82978	.17022	11476	52063	4.15	85
6	10408	1913	.81624	.18376	9451	40587	3.90	6
7	8495	1681	.80211	.19789	7655	31136	3.67	7
8	6814	1453	.78679	.21321	6087	23481	3.45	8
9	5361	1233	.77005	.22995	4745	17394	3.24	9
90	4128	1021	.75268	.24732	3617	12649	3.06	90
1	3107	821	.73566	.26434	2697	9032	2.91	1
2	2286	640	.72016	.27984	1966	6335	2.77	2
3	1646	483	.70671	.29329	1404	4369	2.65	3
4	1163	354	.69528	.30472	986	2965	2.55	4
95	809	255	.68538	.31462	682	1979	2.45	95
6	554	179	.67602	.32398	464	1297	2.34	6
7	375	125	.66579	.33421	313	833	2.22	7
8	250	87	.65262	.34738	206	520	2.08	8
9	163	60	.63388	.36612	133	314	1.93	9
100	103	40	.60671	.39329	83	181	1.75	100
1	63	27	.56841	.43159	50	98	1.56	1
2	36	18	.51718	.48282	27	48	1.37	2
3	18	10	.45291	.54709	13	21	1.19	3
4	8	5	.37789	.62211	5	8	1.02	4
105	3	2	.29702	.70298	2	3	.87	105
6	1	1	.21720	.78280	1	1	.75	6

